

BASIC ARRAY PROCESSING CONCEPTS (from „shift-and-sum“ to „frequency wavenumber spectra“) and related things...

Matthias Ohrnberger

with contributions by Cécile Cornou, Marc Wathelet
and the SESAME partners

OVERVIEW

- Basic Array Method Principles (general)
- Array geometry → Limitations (general)
- Array Analysis of Microtremor Wavefields
Applying basic principles (general) to
a special problem domain
- Difficulties and attempts for solution

Lectures

Exercises

OVERVIEW: Basic Array Method Principles (general)

- Definition: what is a seismic array?
- What are the benefits of seismic arrays?
- Seismic arrays: historical context and developments
- Basic assumption for array processing:
the need for a wave propagation model
- Plane wave parameter determination
- Delay-and-sum beamforming
- Frequency-wavenumber spectrum

OVERVIEW: Array Geometry → Limitations (general)

- Parameters used to describe array geometries
- Starting simple: 1D layouts
- Relation of parameters with array behaviour
- Discrete sampling of wavefield and implications
- Generalization to planar 2D-geometries
- Directional dependence of array behaviour
- The quest for an optimal array geometry – an old and (maybe) endless story...

OVERVIEW: Array Analysis of Microtremor Wavefields Applying basic principles (general) to a special problem domain

- What is special with microtremor wavefields?
 - What is to be changed from the viewpoint of analysis?
 - What is to be changed from the viewpoint of geometries?
- Complications and attempts to deal with them

BASIC ARRAY METHOD PRINCIPLES

Basic Array Method Principles (general)

seismic network!

Definition: what is a ,seismic array‘ ?

{ set of seismograph stations with common time base

AND

sensors located closely enough in space

so that arriving seismic signal waveforms can be correlated between adjacent sensors

seismic array!

to be defined later

Basic Array Method Principles (general)

We can conclude from the definition:

set of seismograph stations with common time base

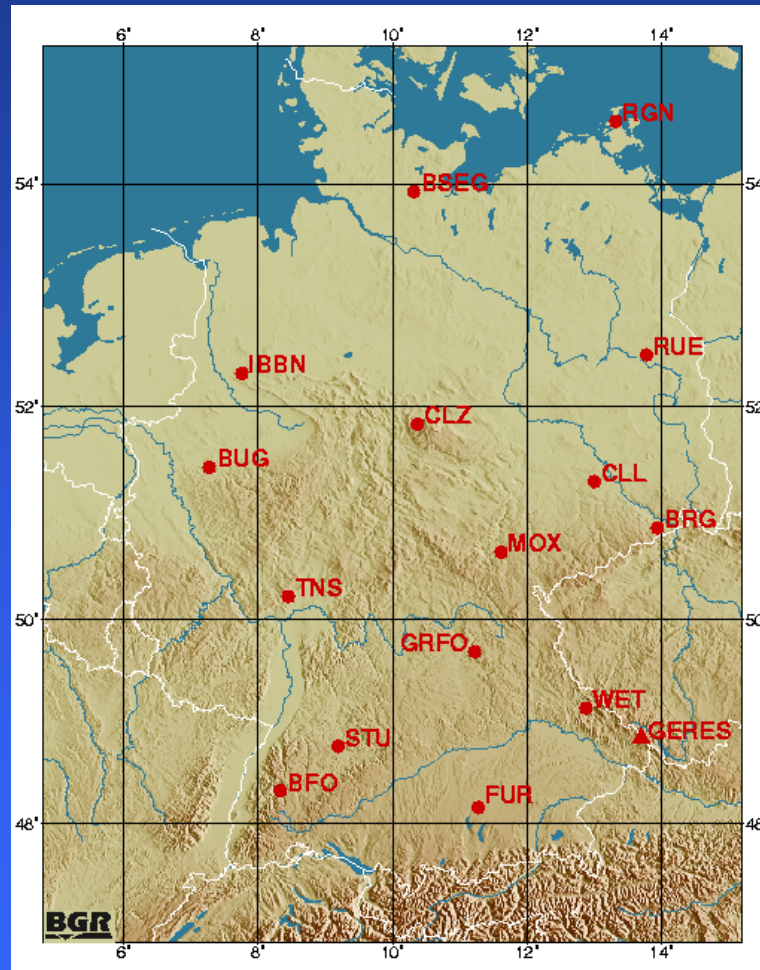
may act

BOTH as ,seismic array‘ **AND** ,seismic network‘

depends on application / wavefield properties of interest

Using Ambient Vibration Array Techniques for Site Characterisation

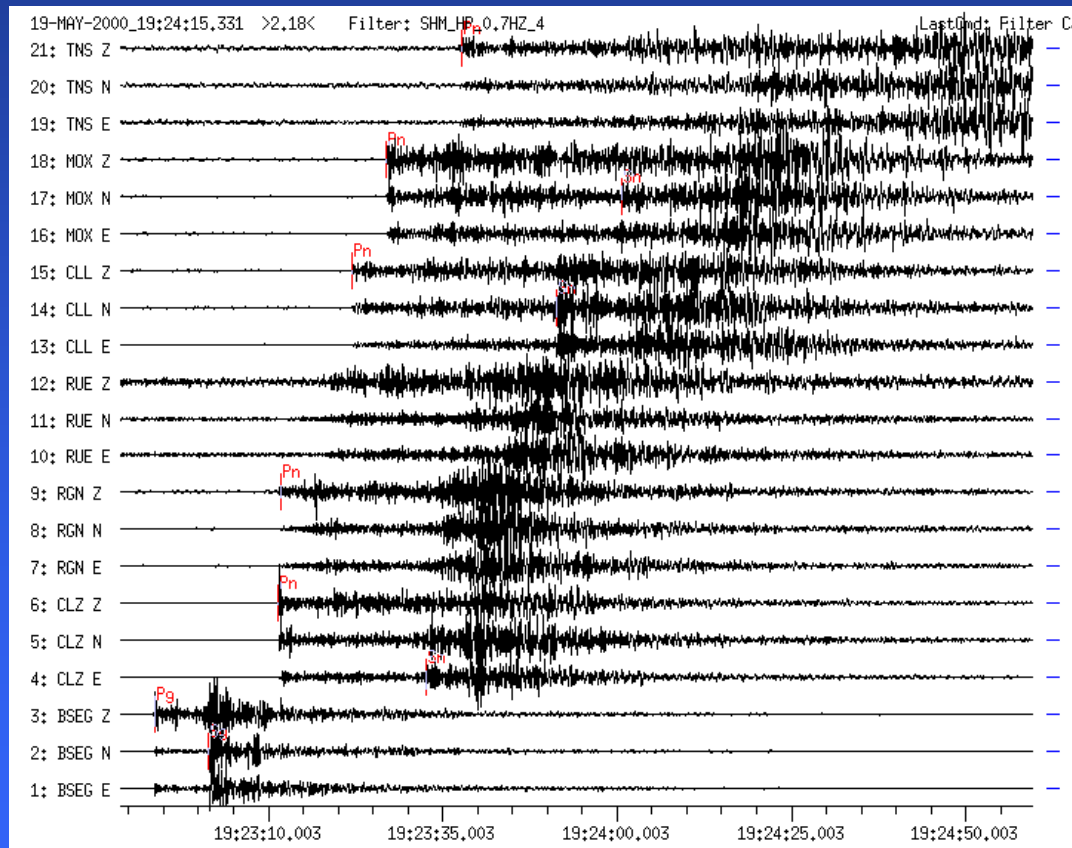
German Regional Seismic Network: array **AND** network!



German Regional Seismic Network: network operation

2000-05-19 OT 19:22:40.8(UTC) 53.47N 11.10E MI 3.4

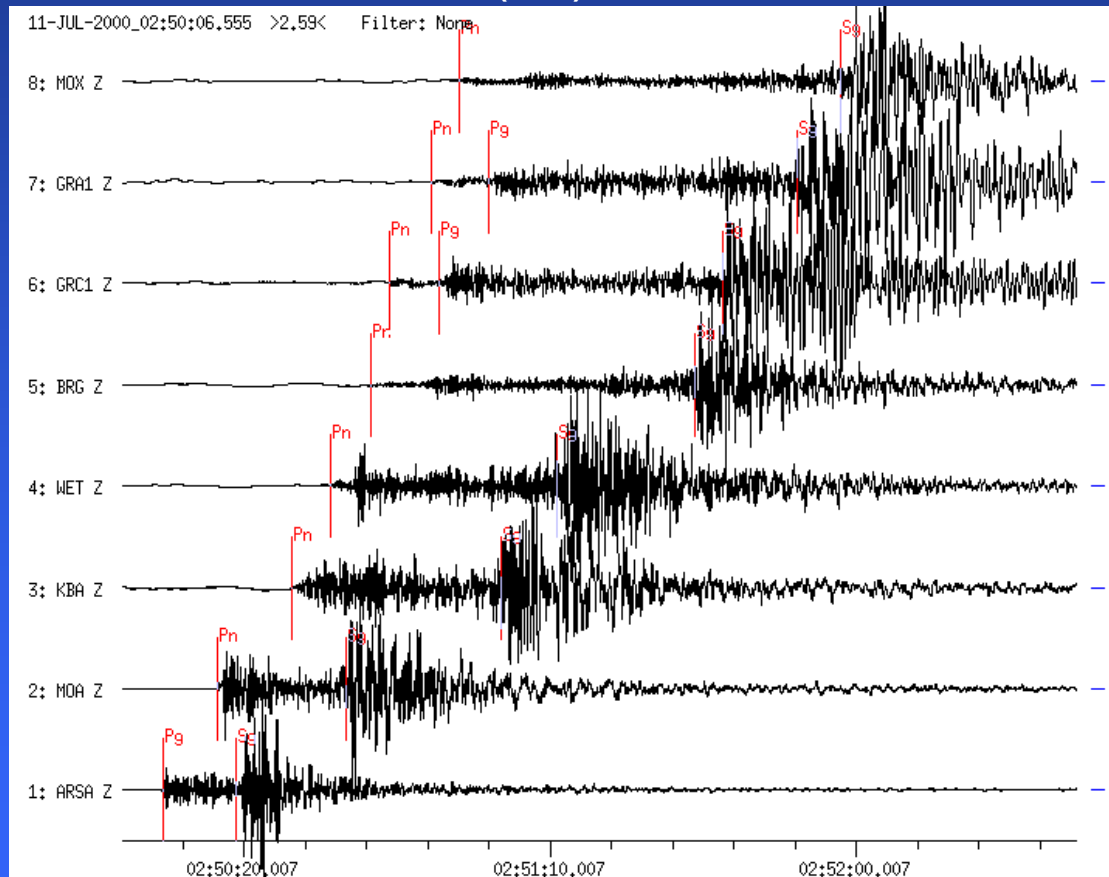
Wittenburg (W-Mecklenburg). Local earthquake recorded at 7 GRSN 3C-stations.



From http://www.szgrf.bgr.de/seismo_examples.html

German Regional Seismic Network: network operation

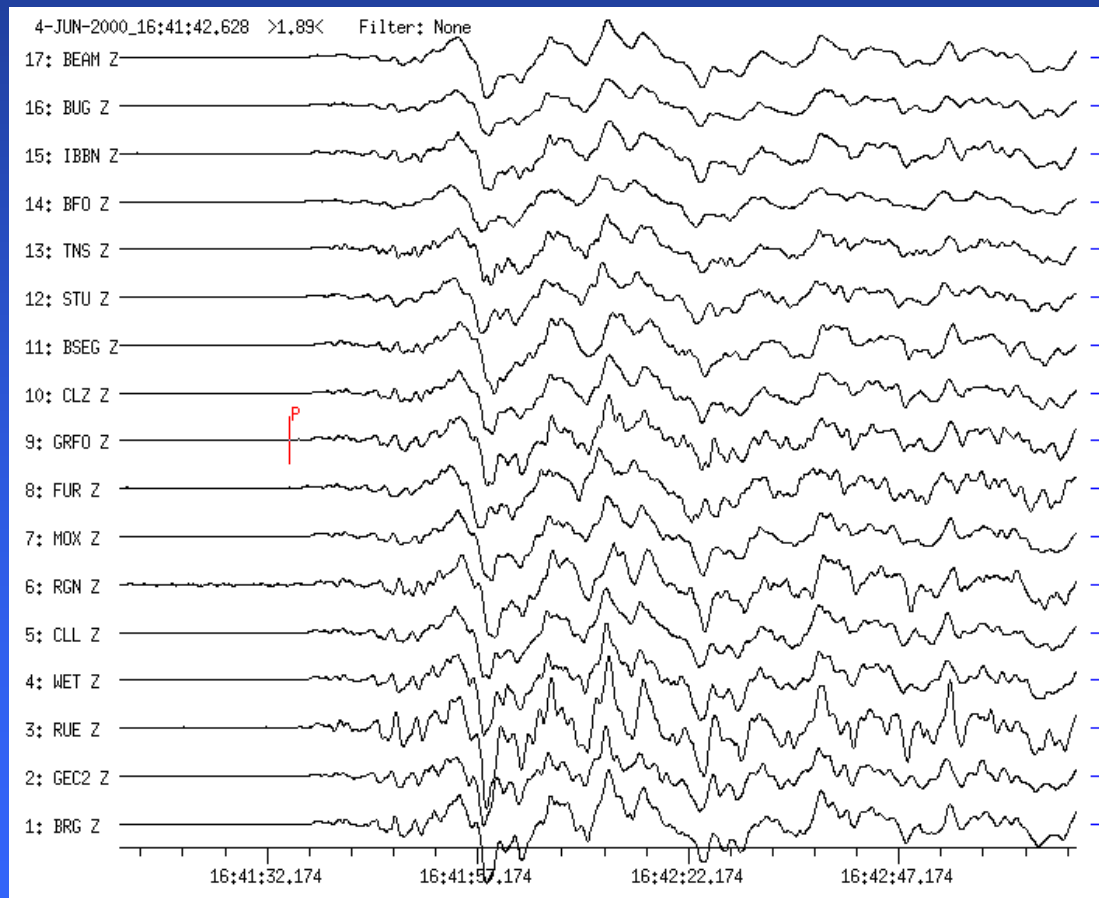
Regional earthquake south of Wien (MI 5.2)
2000-07-11 OT 2:49:51(UTC) 48.10 N 16.40 E MI 5.2



http://www.szgrf.bgr.de/seismo_examples.html

German Regional Seismic Network: **array operation**

Earthquake in Southern Sumatera Region (distance 94.1° to GRF site, az. 92.5°, depth 33km)
 USGS NEIC-data: 2000-06-04 OT 16:28:25.8 4.773 S 102.050 E depth 33km mb 6.8 Ms 8.0

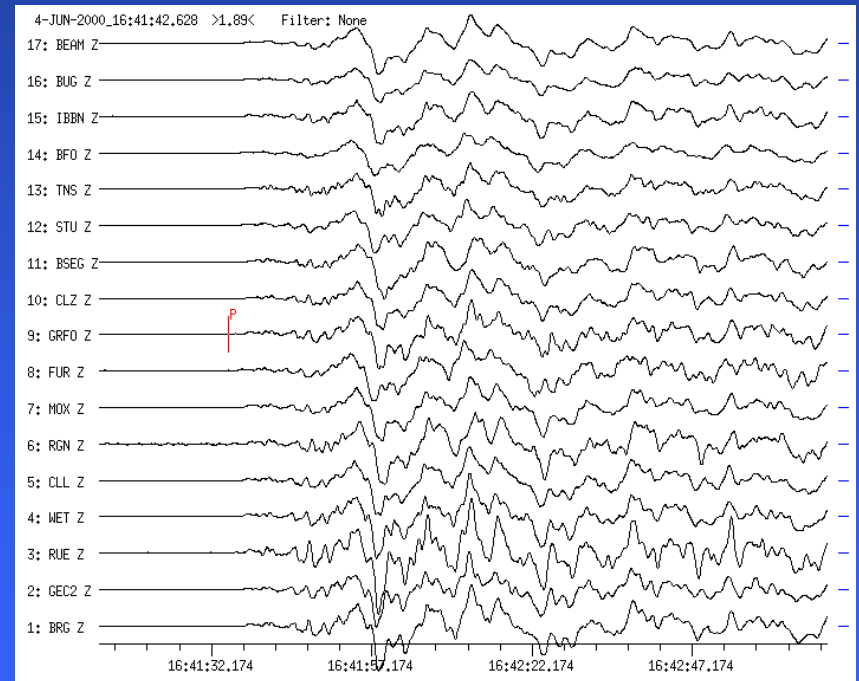
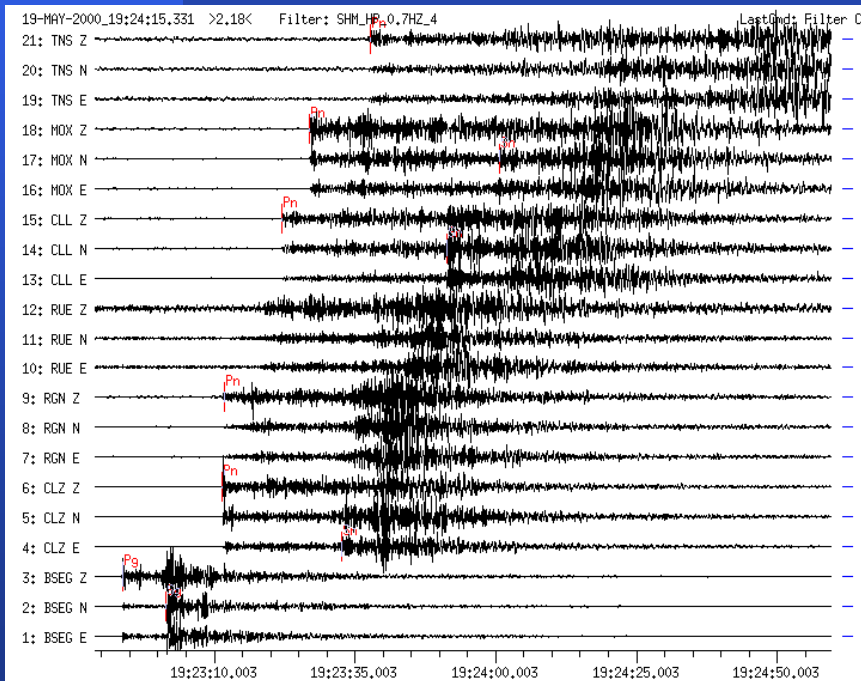


Using Ambient Vibration Array Techniques for Site Characterisation

German Regional Seismic Network:

network operation

array operation



Note the difference?

Benefits of seismic arrays

The **benefit of seismic arrays** can be immediately recognized by considering the **information content of seismic observations** for various settings:

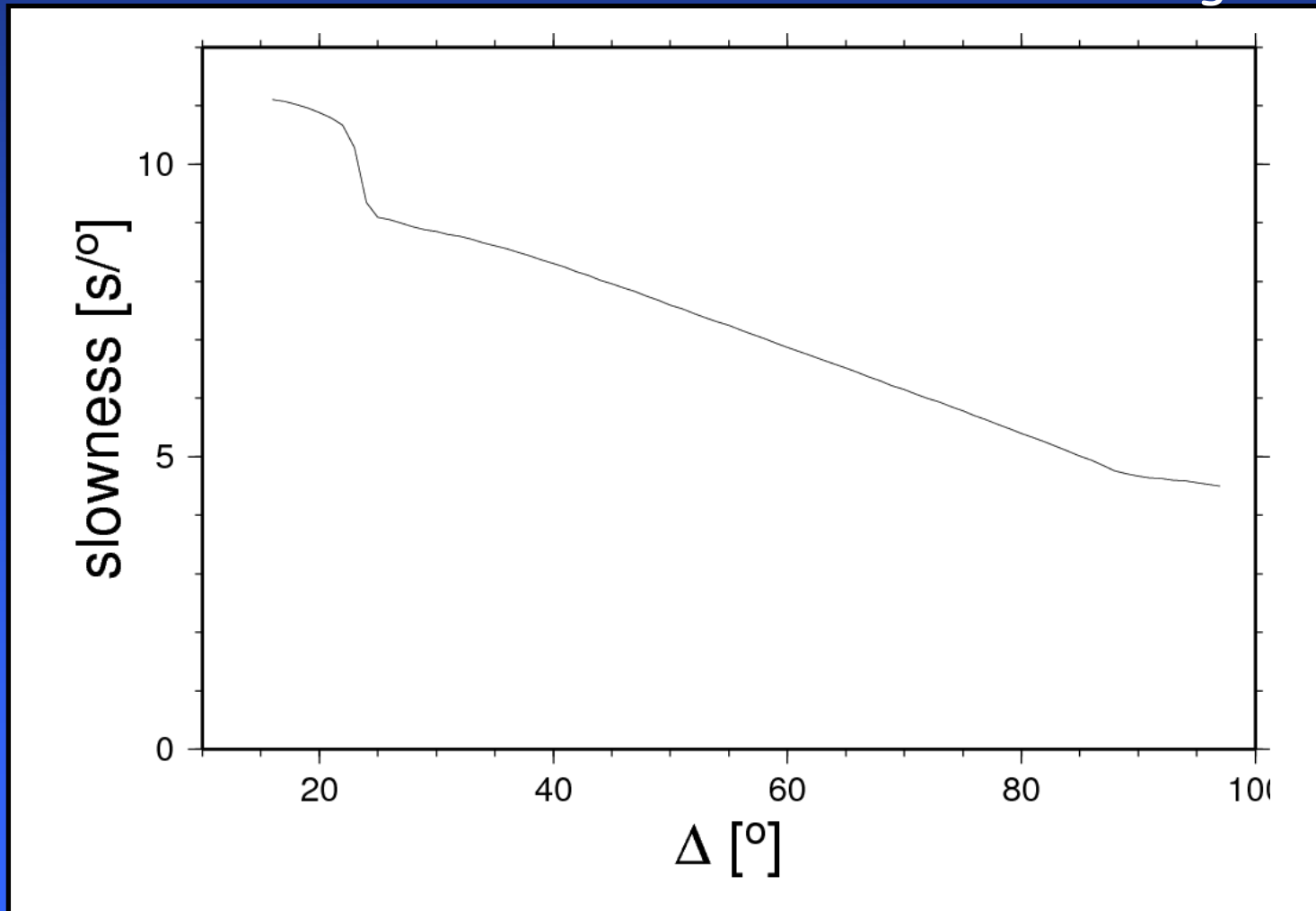
- single station single component
- single station three components
- seismic network (1 or 3 components)
- seismic array (1 or 3 components)

available information for:

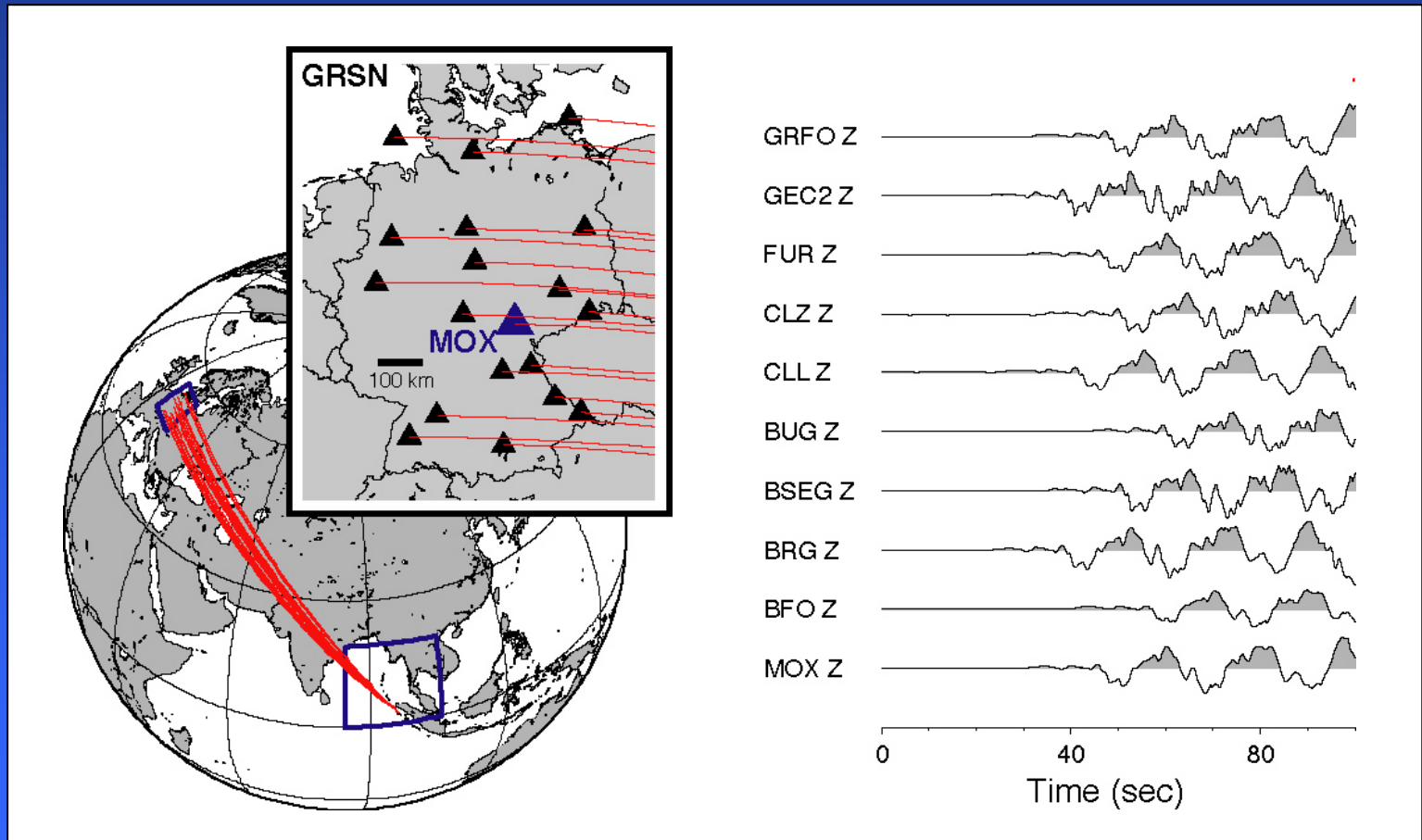
- **single station single component:**
arrival times, amplitudes
- **single station three components**
arrival times, amplitudes, polarization
(= particle motion at site)
- **seismic network (1 or 3 component)**
arrival times, amplitudes, (polarization),
direction of wave (from location),
- **seismic array (1 or 3 component)**
arrival times, ampl., (polarization), direction of wave,
apparent propagation velocity of wave, SNR improvement

Using Ambient Vibration Array Techniques for Site Characterisation

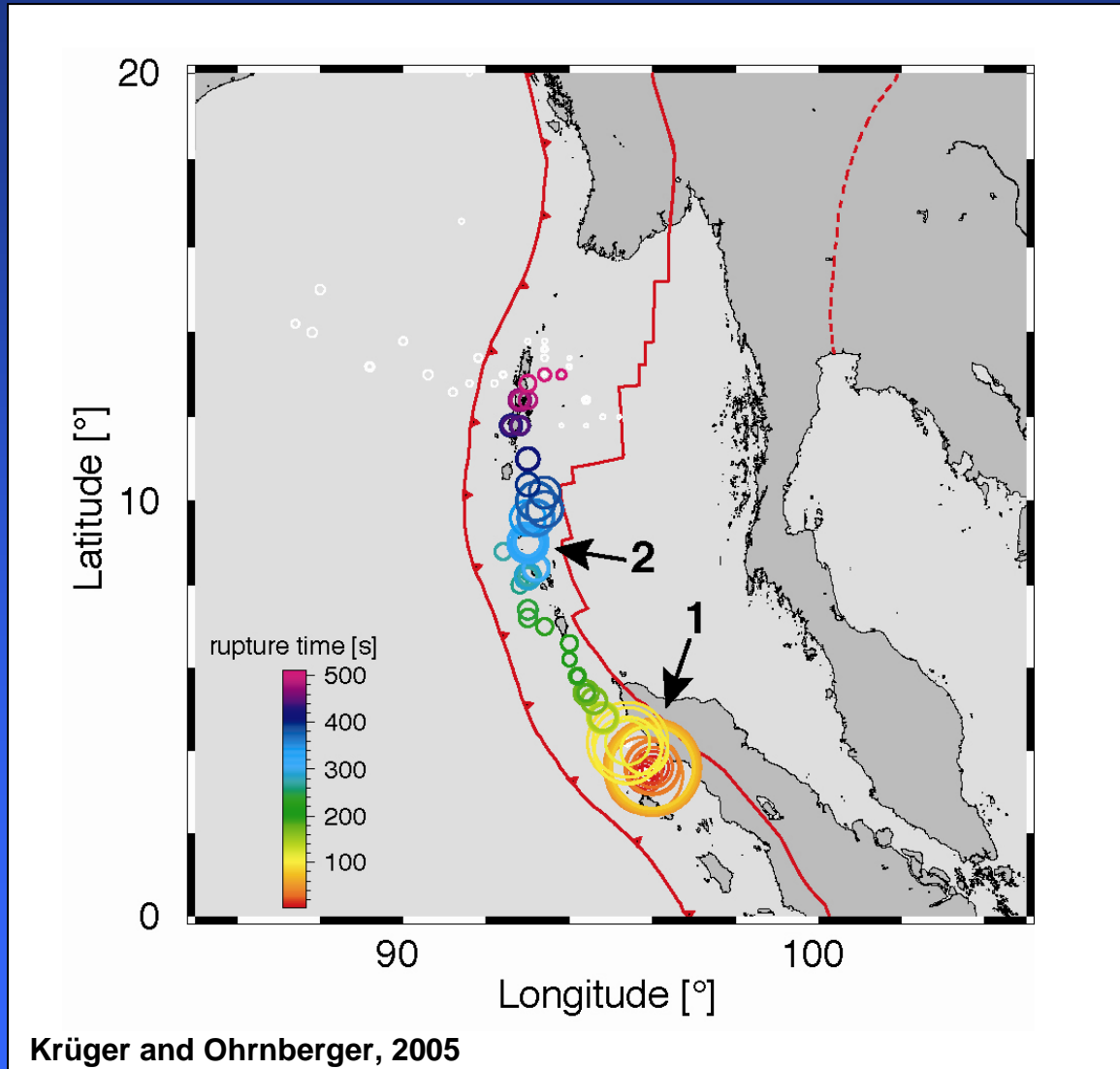
Apparent velocity \leftrightarrow horizontal slowness \leftrightarrow ray parameter
 Slowness - distance relation in teleseismic distance range



German Regional Seismic Network: array operation



Using Ambient Vibration Array Techniques for Site Characterisation



Seismic arrays: historical context and developments

(summary from Mykkeltveit et al., 1983, BSSA, Rost and Thomas, 2002, RG)

First ideas as early as 1920's in exploration geophysics!
combining clusters of geophones for SNR improvement

In seismological context the development and use
of array techniques is closely related to the start of
nuclear test ban negotiations in Geneva 1958

Concept: a **high number of small arrays** to monitor
nuclear underground test activities around the world
(planned 170 small aperture arrays with 10 sensors)

Seismic arrays: historical context and developments

First experimental arrays from 1960 to 1963
in U.S. and U.K. (VELA program)

But: small array concept could not be realized due to
political reasons (array installations blocked)

Therefore: second best solution for detection
and verification purposes of nuclear explosions:

Very large arrays at few spots
→ LASA (1965), NORSAR (1971)

Seismic arrays: historical context and developments

LASA (1965) & NORSAR (1971) facts:

LASA: 200 km aperture, initially 525 stations

NORSAR: 100 km aperture, 198 stations

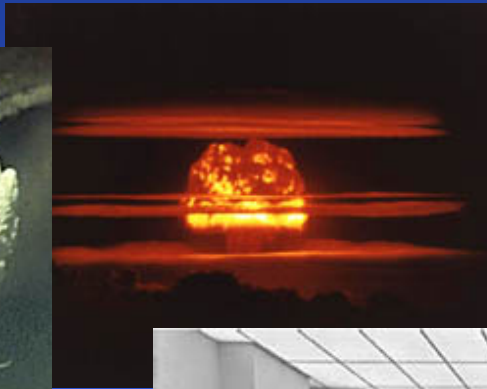
Huge number of stations →

SNR-improvement for detection/discrimination **formidable!**

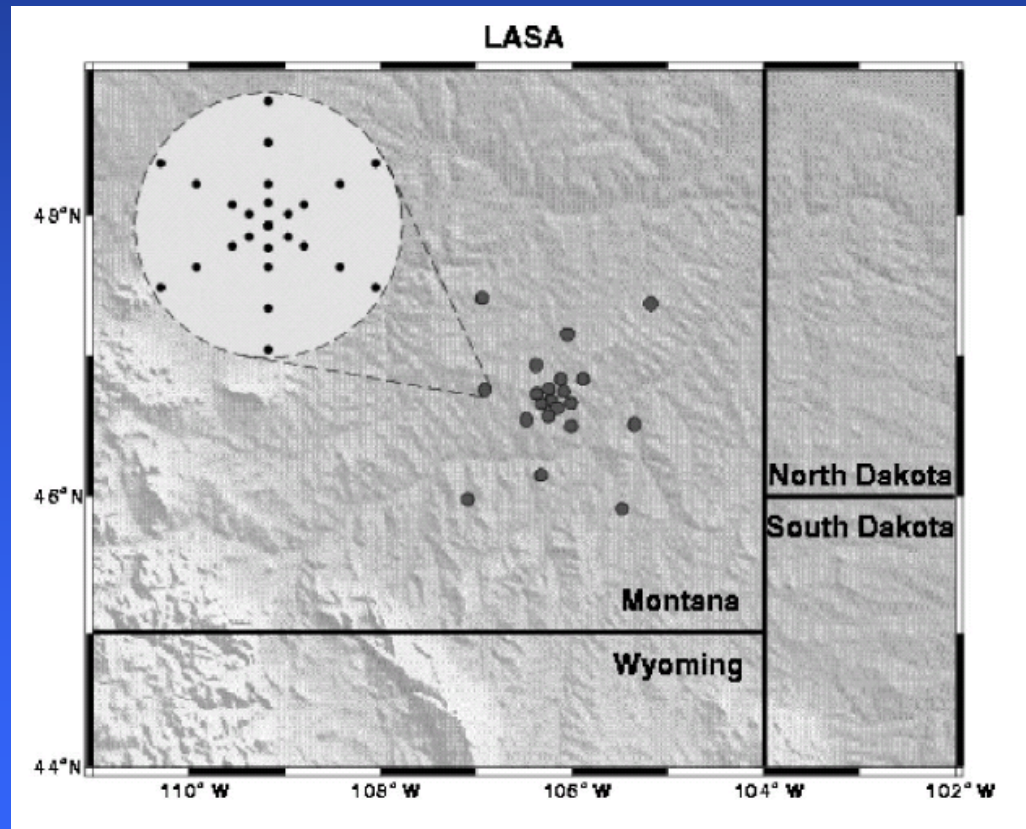
Event location on global scale even for small magnitudes

COST OF OPERATION AND MAINTENANCE!!!!!!

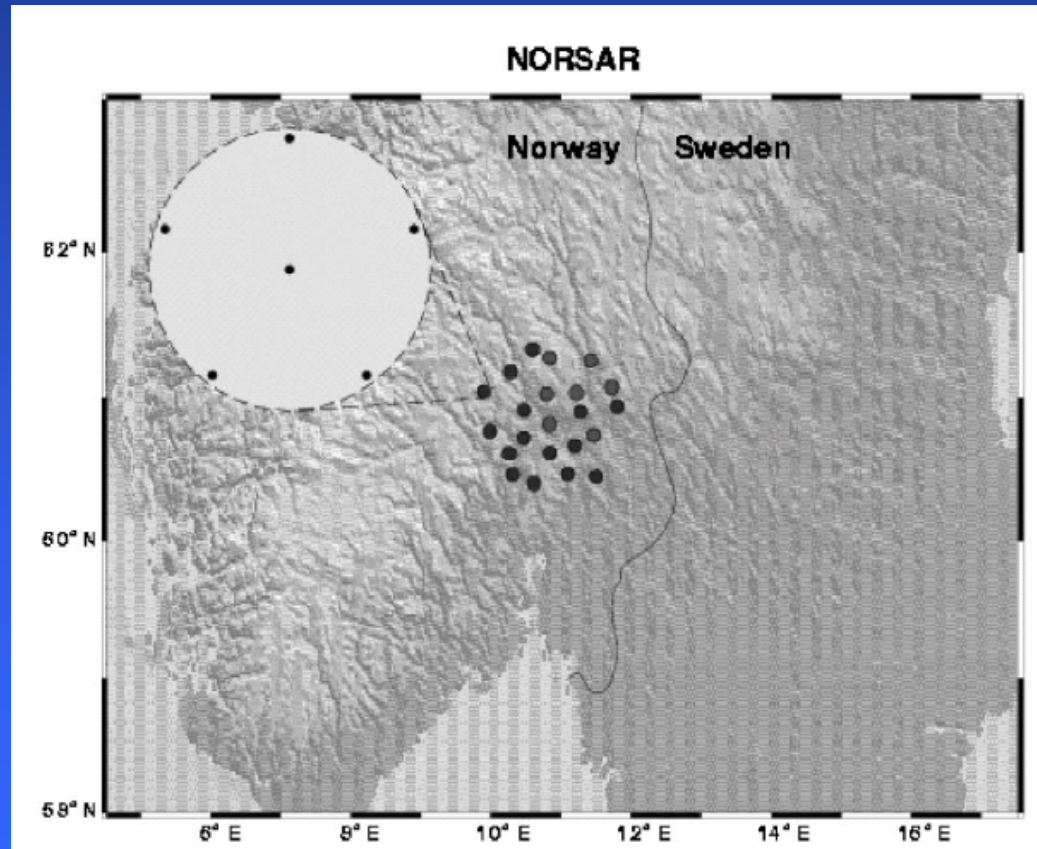
Seismic arrays: historical context and developments



Seismic arrays: historical context and developments



Seismic arrays: historical context and developments



Seismic arrays: historical context and developments

Further application domains:

- structural investigations (global/regional/local)
- seismic exploration
- since relative early times a matter of interest
→ ‚seismic noise‘!

(i.e. in the context of array design for monitoring arrays it has been recognized that noise is almost never incoherent and white, but rather colored and shows spatial coherence)

What is noise...?

" ... In order to record seismic signals it is desirable to know the spectrum of seismic noise since a priori knowledge of the expected signal-to-noise ratio as a function of frequency can best determine the frequency response characteristics of instrumentation. Also, since arrays are constructed for the purpose of enhancing the signal-to-noise ratio it is desirable to know beforehand the nature of the noise. Is it random or propagating ? How coherent is it ? Unfortunately these questions tend to require at least a skeleton array to answer them! . . . "

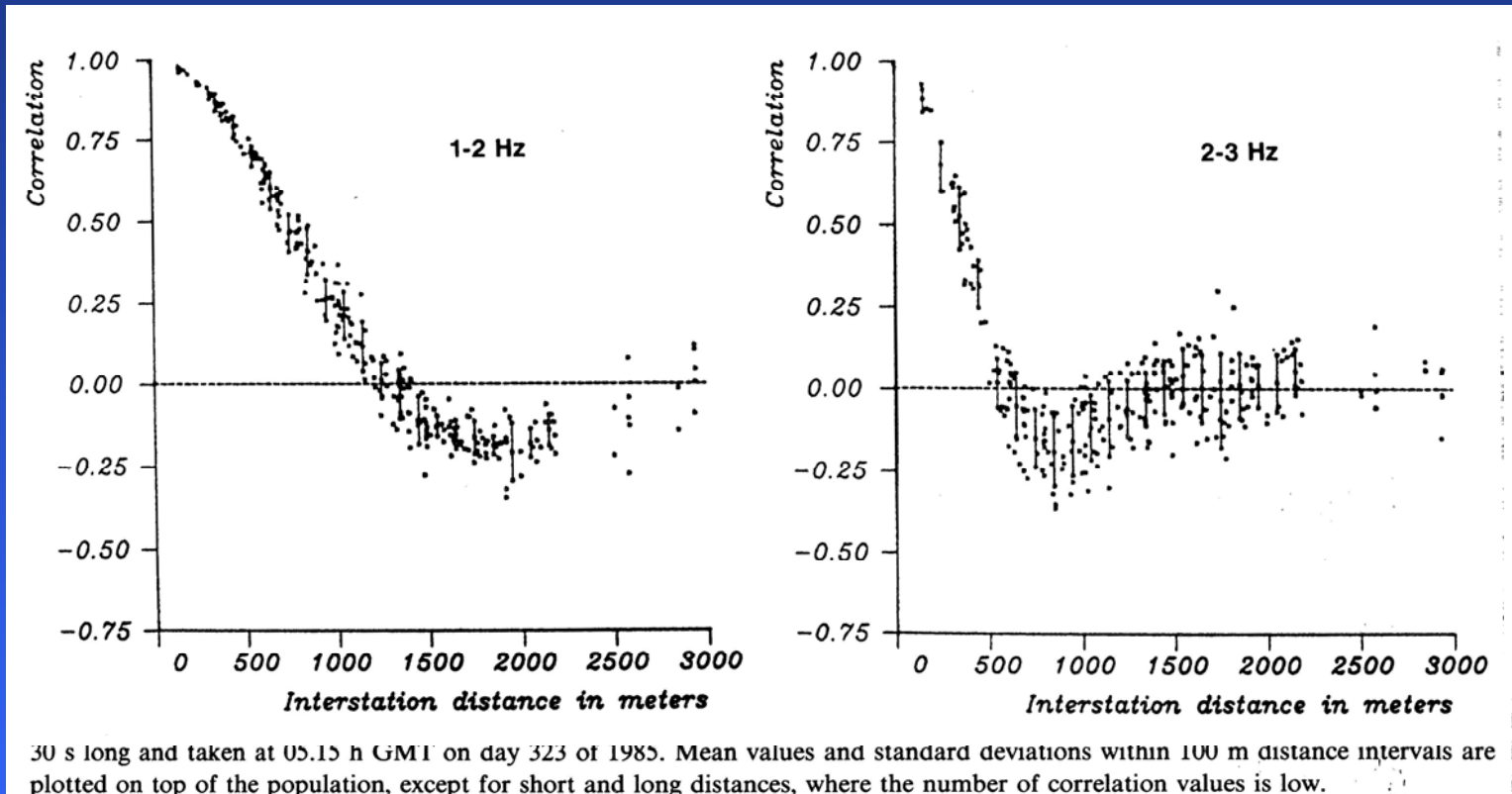
Davies, 1973

What is noise...?

" ... In order to record seismic signals **it is desirable to know the spectrum of seismic noise** since a priori knowledge of the expected signal-to-noise ratio as a function of frequency can best determine the frequency response characteristics of instrumentation. Also, **since arrays are constructed for the purpose of enhancing the signal-to-noise ratio** it is desirable to know beforehand the **nature of the noise**. Is it random or propagating ? How coherent is it ? **Unfortunately these questions tend to require at least a skeleton array to answer them! . . .**"

Davies, 1973

NORES noise correlation analysis \Rightarrow coherence lengths



**Mykkeltveit, S., K. Åstebøl, D.J. Dornboos & E.S. Husebye (1983):
Seismic array configuration optimization. Bull. Seism. Soc. Am., 73: 173-186.**

Seismic arrays: historical context and developments

Further application domains:

- since relative early times a matter of interest:
'seismic noise' → ambient vibrations

K. Aki, 1957, 1965, Toksöz, 1964, Capon et al., 1967
Capon, 1969, Lacoss et al., 1969,
Haubrich and Camy, 1969, Woods and Lintz, 1973,
Henstridge, 1979, Asten and Henstridge, 1984,
Horike, 1985, Tokimatsu et al., 1992, Tokimatsu, 1997

**Basic assumption for array processing:
the need for a wave propagation model**

Simple model and therefore appealing:

Harmonic plane wave representation!

$$D(x, t) = A \exp(i\omega(t \pm x/c)) \quad D(\vec{x}, t) = A \exp(i(\omega t \pm \vec{k}\vec{x}))$$

Particular solution to the homogeneous wave equation

$$\frac{\partial^2 D}{\partial x^2} = \frac{1}{c^2} \frac{\partial^2 D}{\partial t^2}$$

Harmonic plane wave representation

$$D(\vec{x}, t) = A \exp(i(\omega t \pm \vec{k}\vec{x}))$$

$$D(\vec{x}, t) = A \exp(i\omega(t \pm \vec{u}\vec{x}))$$

phase

positions of constant phase at some time t are wavefronts \rightarrow
 $\vec{k}\vec{x} = \text{const.} \rightarrow$ wavefronts are planes in space
 orientation of plane is given by wavenumber vector (normal vector)

Parameters describing plane waves:

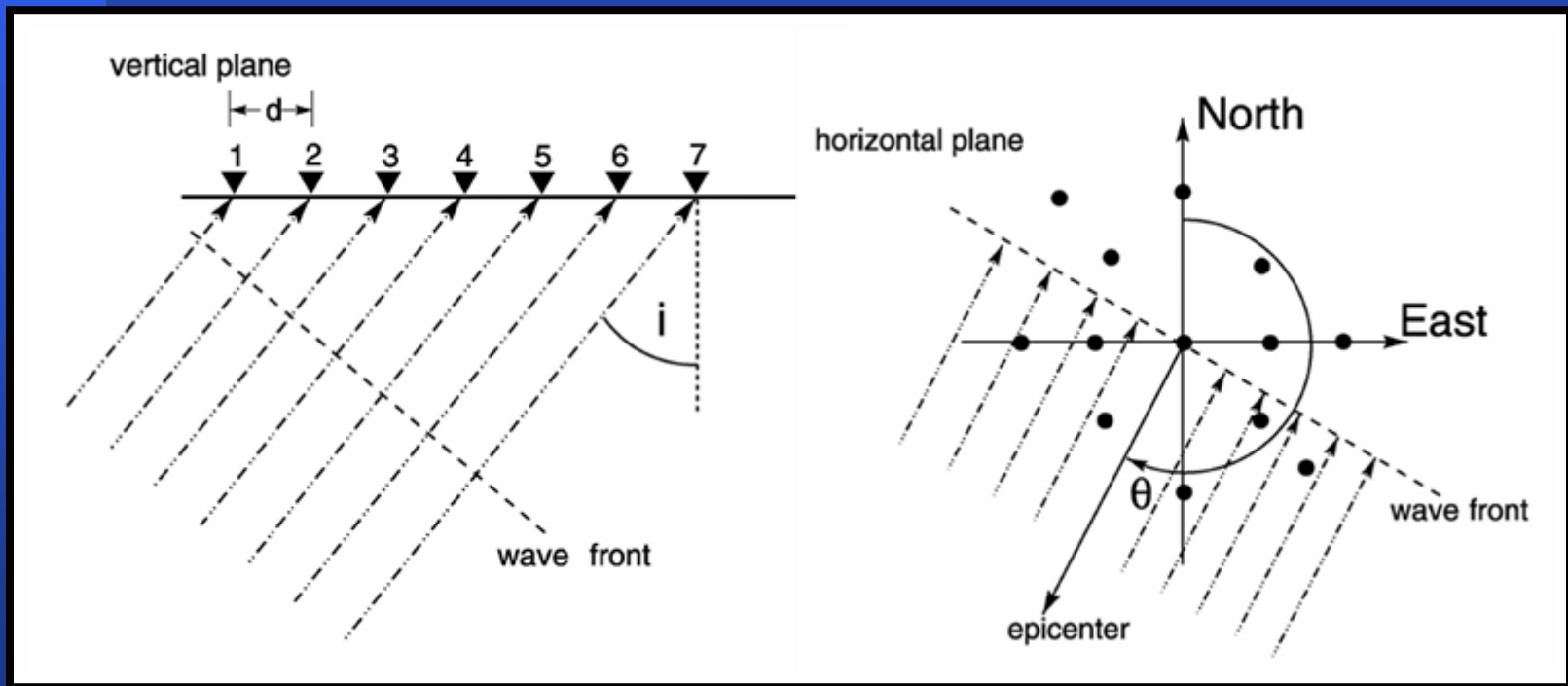
wavenumber $\vec{k} = \omega\vec{u}$ slowness

$$k = \frac{2\pi}{\lambda} = \frac{2\pi f}{v} = \frac{\omega}{v} = \omega|\vec{u}|$$

Period + frequency $T = \frac{1}{f} = \frac{2\pi}{\omega}$

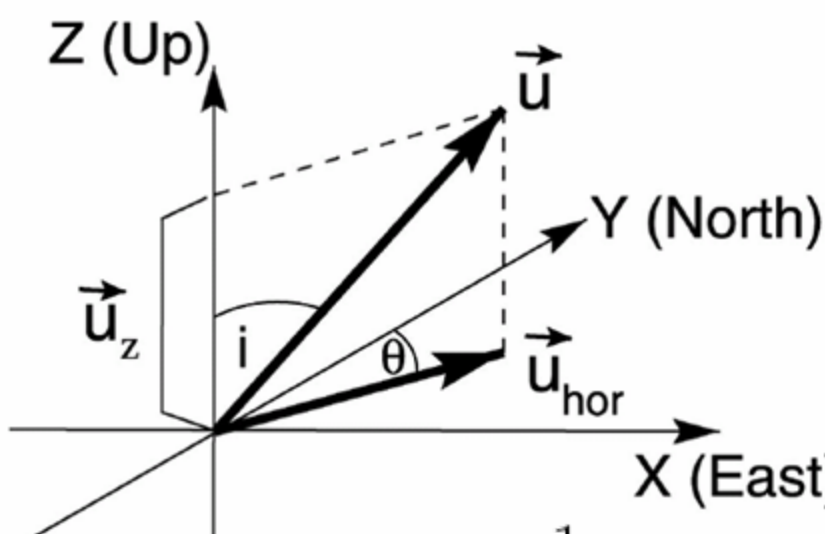
$$v = \lambda f = \lambda\omega/2\pi$$

Basic assumption for array processing: the need for a wave propagation model



Geometry of plane waves – parameters of wave propagation

Basic assumption for array processing: the need for a wave propagation model



slowness vector:

- in direction of wave propagation
- perpendicular to wavefront
- length $\sim v_0^{-1}$

$$\vec{u} = (u_x, u_y, u_z)$$

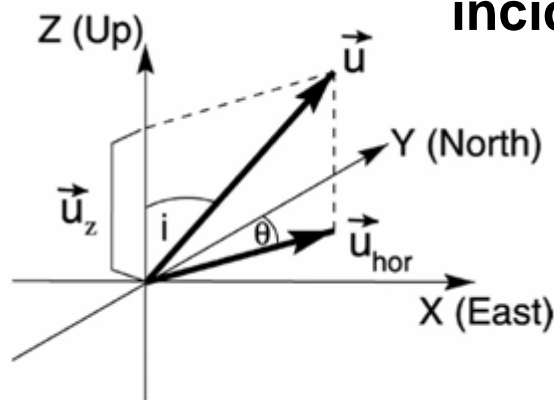
$$\vec{u} = \frac{1}{v_0} (\sin(i) \sin(\theta), \sin(i) \cos(\theta), \cos(i))$$

Geometry of plane waves – parameters of wave propagation

Basic assumption for array processing: the need for a wave propagation model

$$\vec{u} = \frac{1}{v_0} (\sin(i) \sin(\theta), \sin(i) \cos(\theta), \cos(i))$$

**slowness vector described by
incidence angle i , propagation azimuth θ**

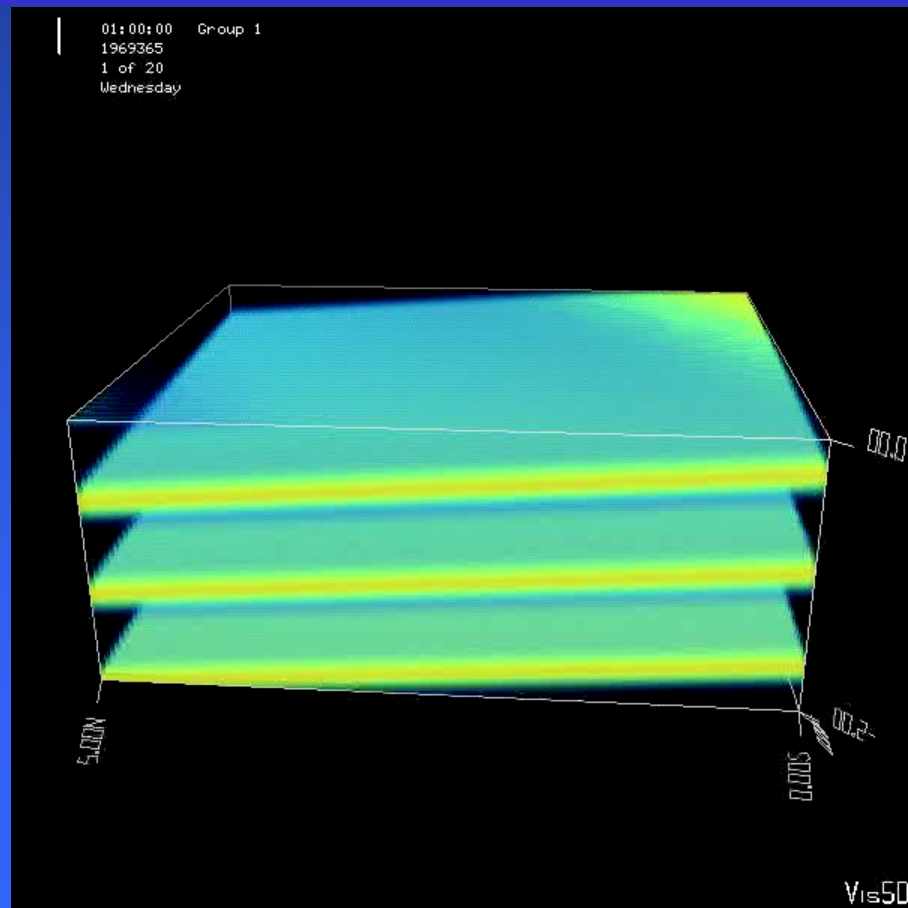


$$\vec{u} = u_{hor} (\sin(\theta), \cos(\theta), \frac{1}{\tan(i)})$$

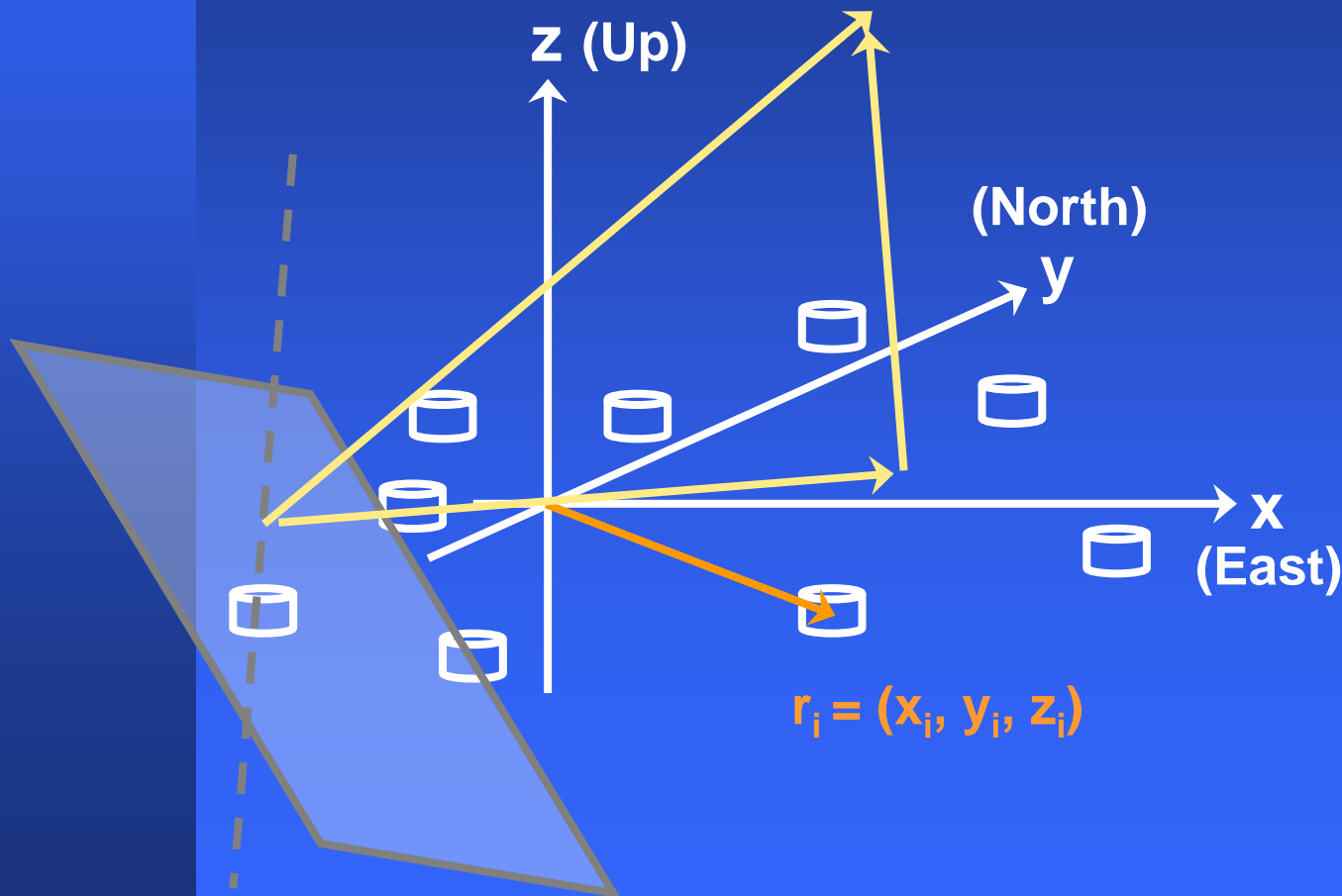
$$|\vec{u}_{hor}| = \frac{1}{v_{app}} = \frac{\sin(i)}{v_0} = p$$

Geometry of plane waves – parameters of wave propagation

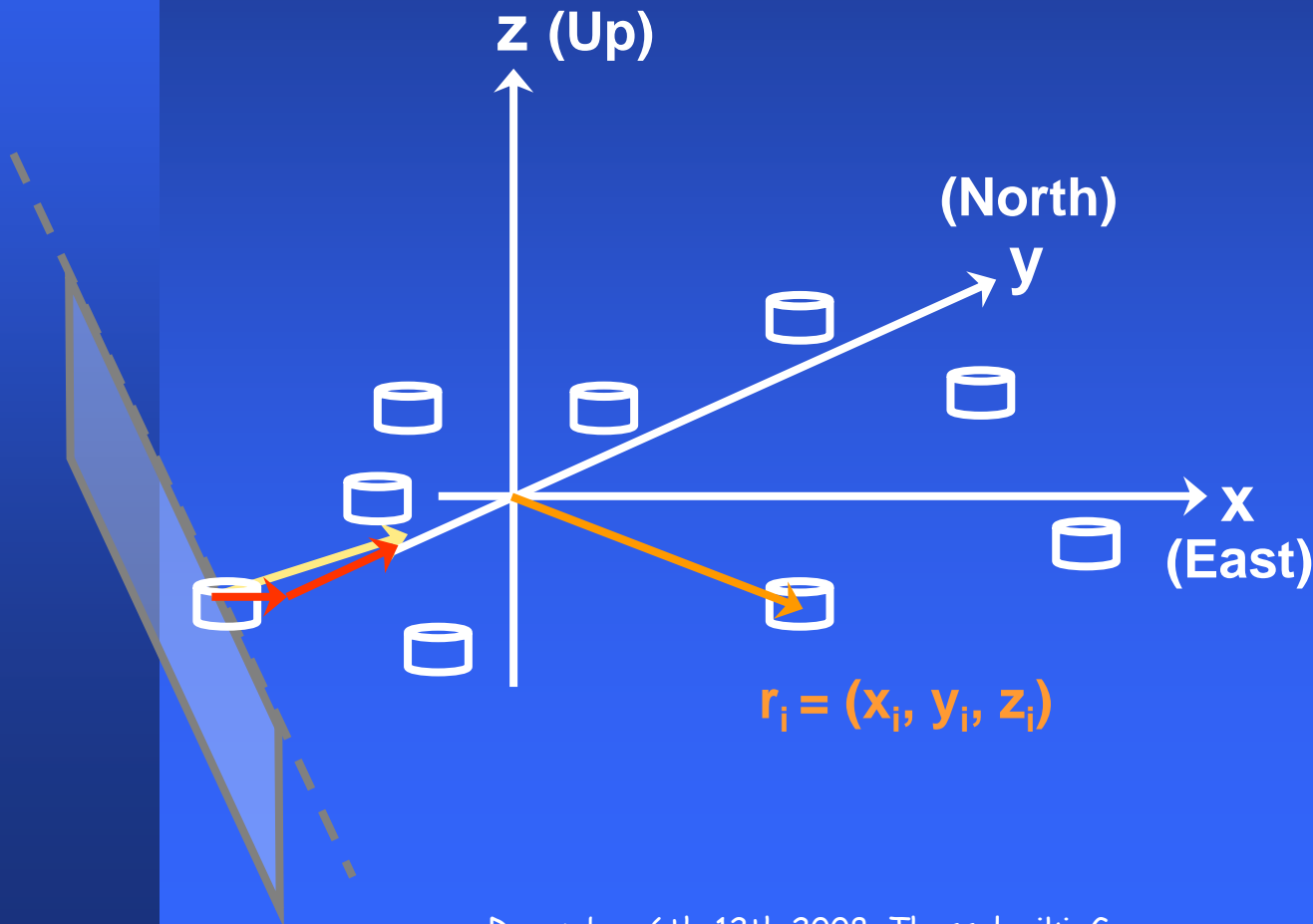
Basic assumption for array processing: the need for a wave propagation model



Plane wave propagation model: body wave type



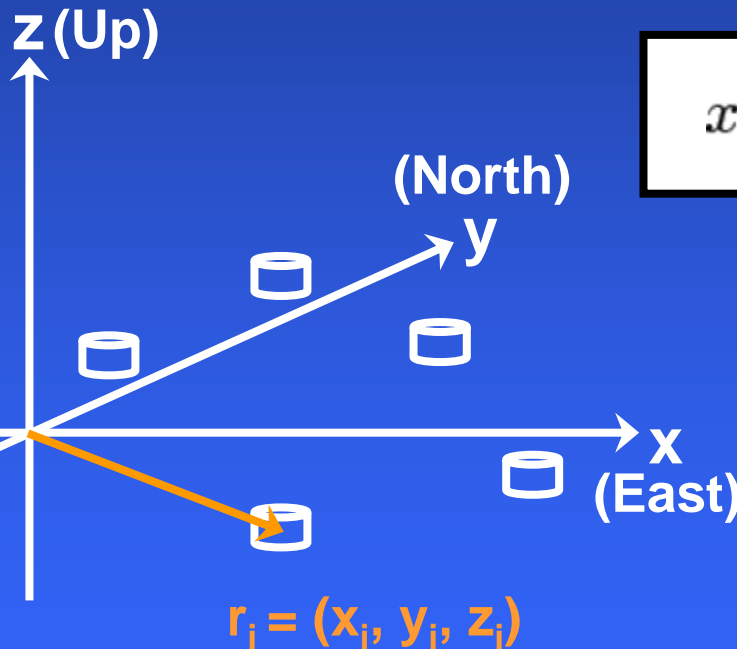
Plane wave propagation model: surface wave type



Plane wave propagation model:

observation of particular waveform $s(t)$ at array sensors

Plane wave description at a single sensor:

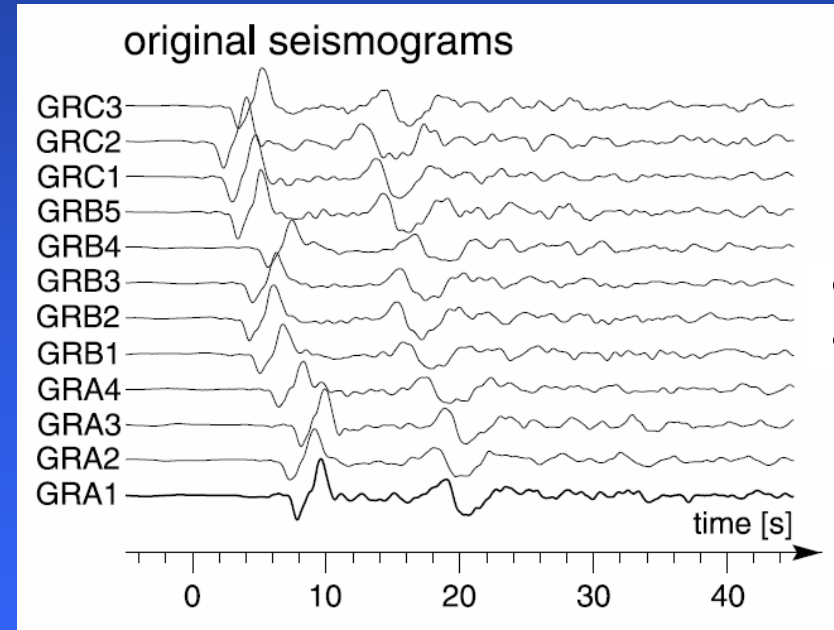
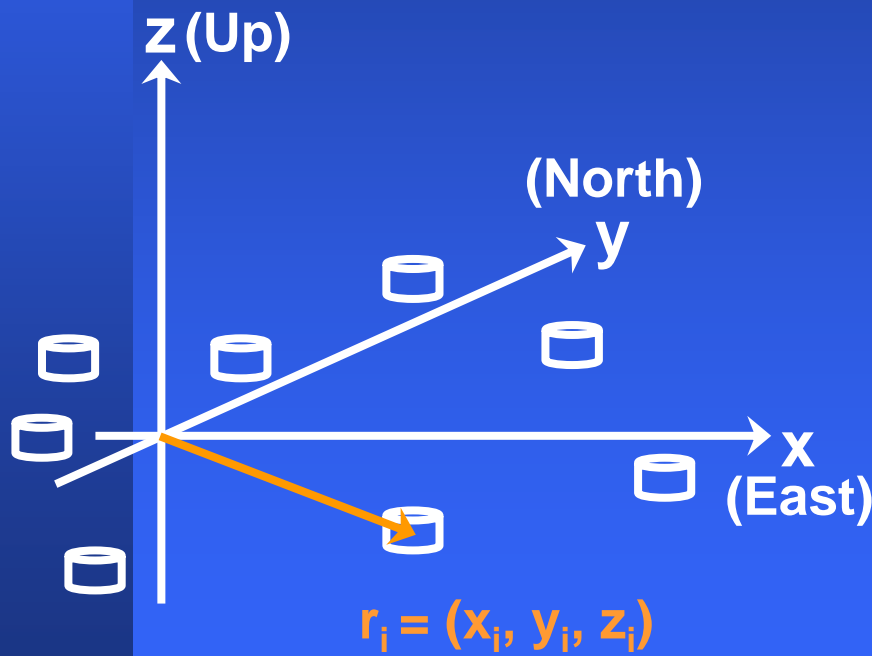


$$x_i(t) = s(t - \vec{r}_i \cdot \vec{u}_{hor}) + n_i(t)$$

relative time shifts
depend on station position
AND horizontal slowness

Plane wave propagation model: array recordings

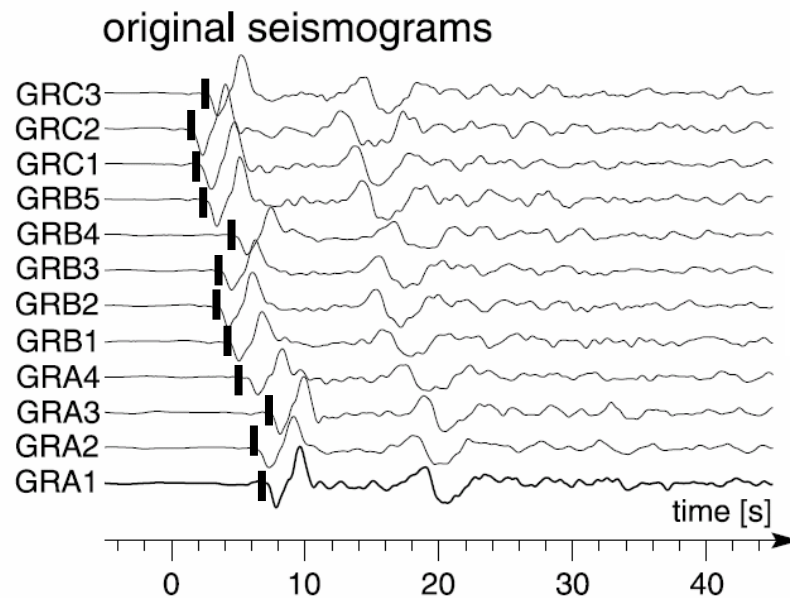
Example plane wave seismogram section:



$$x_i(t) = s(t - \vec{r}_i \vec{u}_{hor}) + n_i(t)$$

Plane wave parameter determination I: transient signals with high SNR

Arrival time picking at N stations



Standard procedure

Plane wave parameter determination I: transient signals with high SNR

Arrival time at station i

$$t_i = t_o + \vec{u}_{hor} \vec{r}$$

+ plane wave model \rightarrow set of linear equations

$$\begin{bmatrix} t_1 - t_o \\ t_2 - t_o \\ \vdots \\ t_N - t_o \end{bmatrix} = \begin{bmatrix} r_{1x} & r_{1y} \\ r_{2x} & r_{2y} \\ \vdots & \vdots \\ r_{Nx} & r_{Ny} \end{bmatrix} \begin{bmatrix} u_x \\ u_y \end{bmatrix}$$

Plane wave parameter determination I: transient signals with high SNR

In short:

$$\vec{t} = \underline{R}\vec{u}_{hor}$$

formal solution:

$$\vec{u}_{hor} = \underline{R}^{-1}\vec{t}$$

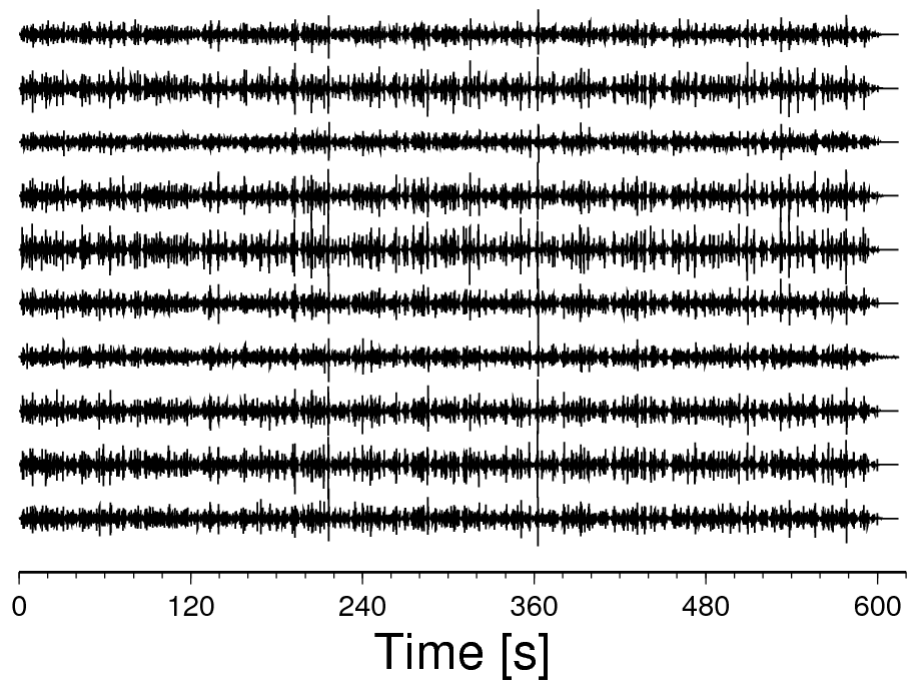
we get (e.g. by LSQ)

$$p = |\vec{u}_{hor}| \quad \theta = \text{atan}(u_x/u_y)$$

Inverse of app. velocity / propagation azimuth

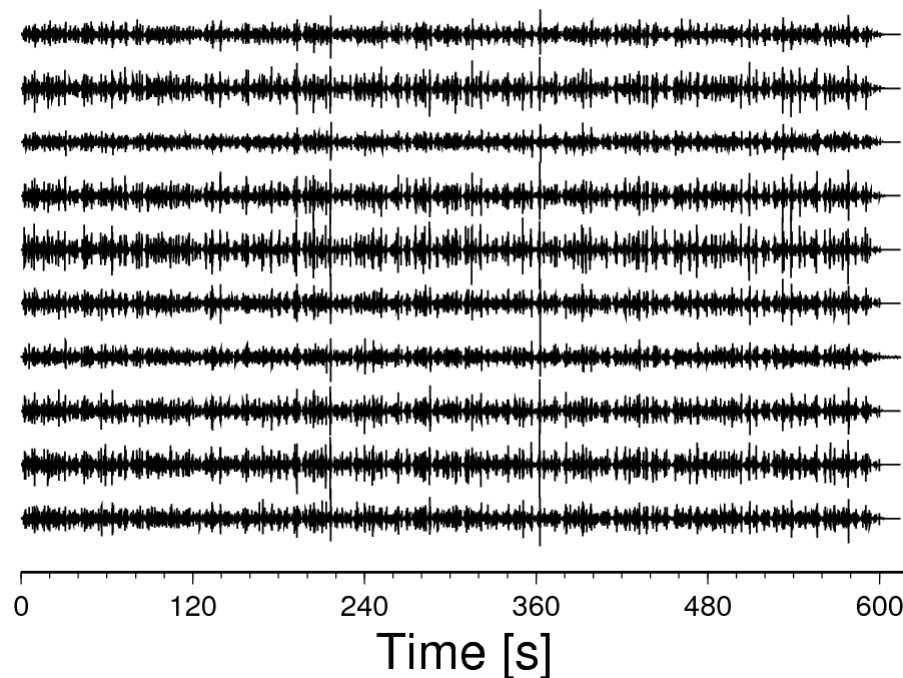
Plane wave parameter determination II: enhancing signals for specific parameters

Question: is there a signal with parameters θ_0, ρ_0



Plane wave parameter determination II: enhancing signals for specific parameters

Answer: let's try!



Plane wave parameter determination II: enhancing signals for specific parameters

Answer: let's try!

$$\vec{u} = u_{hor}(\sin(\theta), \cos(\theta), \frac{1}{\tan(i)})$$

observation

$$x_i(t) = s(t - \vec{r}_i \vec{u}_{hor}) + n_i(t)$$

delay observation

$$\tilde{x}_i(t) = x_i(t + \vec{r}_i \vec{u}_{hor})$$

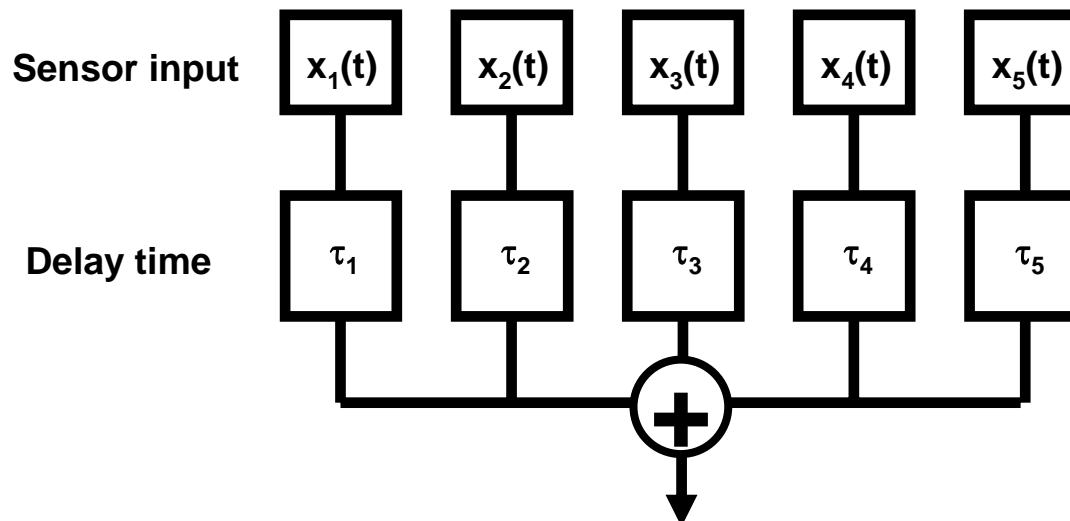
$$\tilde{x}_i(t) = s(t) + n_i(t + \vec{r}_i \vec{u}_{hor})$$

and sum

$$b(t) = \frac{1}{N} \sum_{i=1}^N \tilde{x}_i(t) = s(t) + \frac{1}{N} \sum_{i=1}^N n_i(t + \vec{r}_i \vec{u}_{hor})$$

uncorrelated noise is suppressed by \sqrt{N} (at best)

Plane wave parameter determination II: enhancing signals for specific parameters

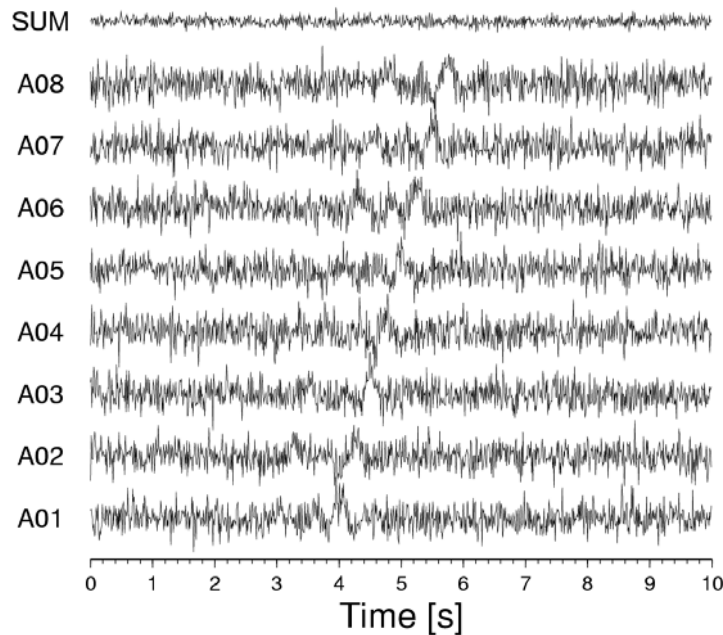


Delay-and-sum Beam = $b(t)$ = Array output

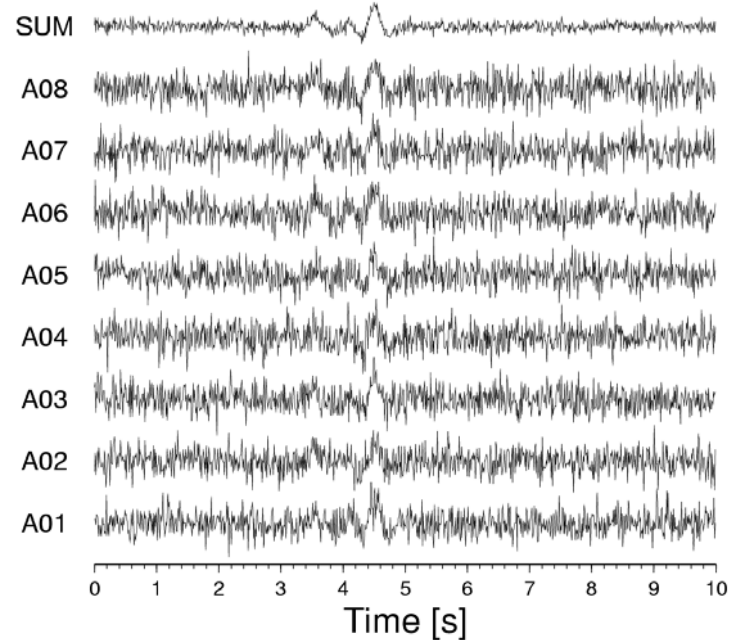
$$b(t) = \frac{1}{N} \sum_{i=1}^N \tilde{x}_i(t) = s(t) + \frac{1}{N} \sum_{i=1}^N n_i(t + \vec{r}_i \cdot \vec{u}_{hor})$$

Plane wave parameter determination II: enhancing signals for specific parameters

with some p, θ



with p_0, θ_0



Plane wave parameter determination II: enhancing signals for specific parameters

Delay and sum beamformer – how well did it work?

Quantify by power measure... → beam energy

$$E(\text{beam}) = \sum_{k=1}^N |b(k\Delta t)|^2$$

Quantify by coherence measure... → semblance

$$\text{Semblance} = \frac{\left| \sum_{i=1}^N \tilde{x}_i(t) \right|^2}{N \sum_{i=1}^N |\tilde{x}_i(t)|^2}$$

semblance = filter output / filter input energy ratio

Plane wave parameter determination II: enhancing signals for specific parameters

Delay and sum beamformer – how well did it work?

Quantify by power measure... → beam energy

$$E(\text{beam}) = \sum_{k=1}^N |b(k\Delta t)|^2$$

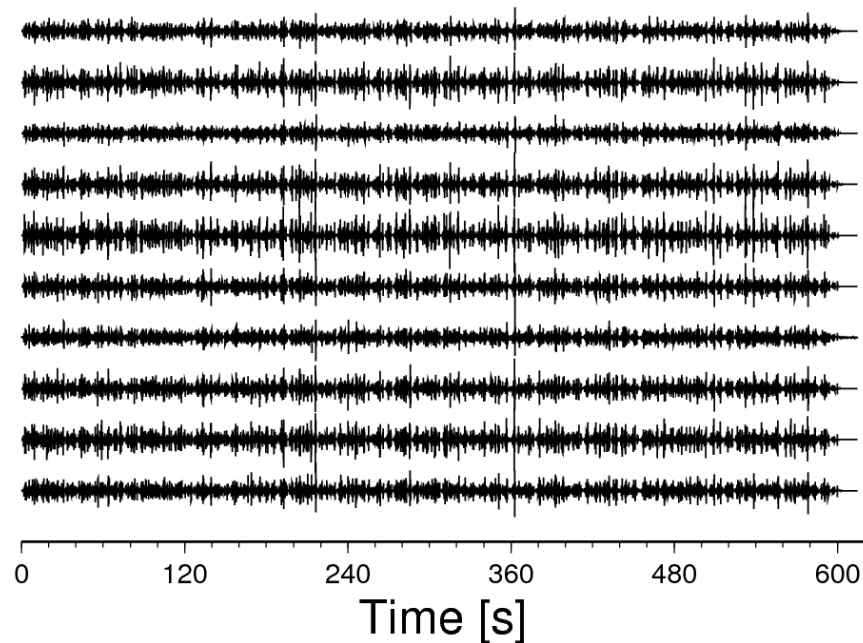
Quantify by coherence measure... → semblance

$$S = \frac{\sum_{j=-M/2}^{j=M/2} \left| \sum_{i=1}^N \tilde{x}_i(t_j) \right|^2}{N \sum_{j=-M/2}^{j=M/2} \sum_{i=1}^N |\tilde{x}_i(t_j)|^2}$$

semblance = filter output / filter input energy ratio

Plane wave parameter determination III: any signal arriving with any possible parameter

Question: is there some signal with arbitrary parameter θ , p which we might be interested in (e.g. Rayleigh waves...)?



Plane wave parameter determination III: any signal arriving with any possible parameter

**Answer: let's do the same procedure as before –
now we just have to search for different values of θ , p**

GRIDSEARCH technique!

**As quantitative measure of goodness of fit, we can use:
Beampower (or Semblance)**

Delay and sum beamforming \rightarrow Slowness power spectrum

Slowness power spectrum: Beampower as function of p and θ

Other standard tool in array analysis:

Vespagram: Beampower as function of p for constant θ

Plane wave parameter determination IV: Beamforming ... a different view

Noisefree signal at station i:

$$x_i(t) = s(t - \vec{r}_i \vec{u}_0)$$

Signal propagates with true (horizontal) slowness vector \vec{u}_0

Beamforming according to test slowness vector \vec{u}

→ time shifted traces:

$$\tilde{x}_i(t) = x_i(t + \vec{r}_i(\vec{u} - \vec{u}_0))$$

Beam:

$$b(t) = \frac{1}{N} \sum_{i=1}^N x_i(t + \vec{r}_i(\vec{u} - \vec{u}_0))$$

Parseval theorem:

$$E(\text{beam}) = \int_{-\infty}^{\infty} b^2(t) dt = \int_{-\infty}^{\infty} |B(\omega)|^2 d\omega$$

Plane wave parameter determination IV: Beamforming ... a different view

Time domain \leftrightarrow frequency domain: Fourier transform

Shifting theorem of FT: $x(t - t_0) \Leftrightarrow X(f) \exp(2\pi j f t_0)$

Then we get for the beam energy in frequency domain:

$$E(\text{beam}) = \int_{-\infty}^{\infty} |B(\omega)|^2 d\omega$$

$$E(\text{beam}) = \int_{-\infty}^{\infty} \left| \frac{1}{N} \sum_{i=1}^N \tilde{X}_i(\omega) \right|^2 d\omega$$

$$E(\text{beam}) = \int_{-\infty}^{\infty} \left| \frac{1}{N} \sum_{i=1}^N X_i(\omega) \exp(j\omega \vec{r}_i \cdot (\vec{u} - \vec{u}_0)) \right|^2 d\omega$$

Plane wave parameter determination IV: Beamforming ... a different view

$$E(\text{beam}) = \int_{-\infty}^{\infty} |X_i(\omega)|^2 \left| \frac{1}{N} \sum_{i=1}^N \exp(j\omega \vec{r}_i(\vec{u} - \vec{u}_0)) \right|^2 d\omega$$

$$E(\vec{u} - \vec{u}_0) = \int_{-\infty}^{\infty} |X_i(\omega)|^2 |A(\vec{u} - \vec{u}_0, \omega)|^2 d\omega$$

Array response function:

$$A(\vec{u} - \vec{u}_0, \omega) = \left| \frac{1}{N} \sum_{i=1}^N \exp(j\omega \vec{r}_i(\vec{u} - \vec{u}_0)) \right|$$

Plane wave parameter determination IV: Beamforming ... a different view → ARRAY RESPONSE

Array response function:

in slowness:

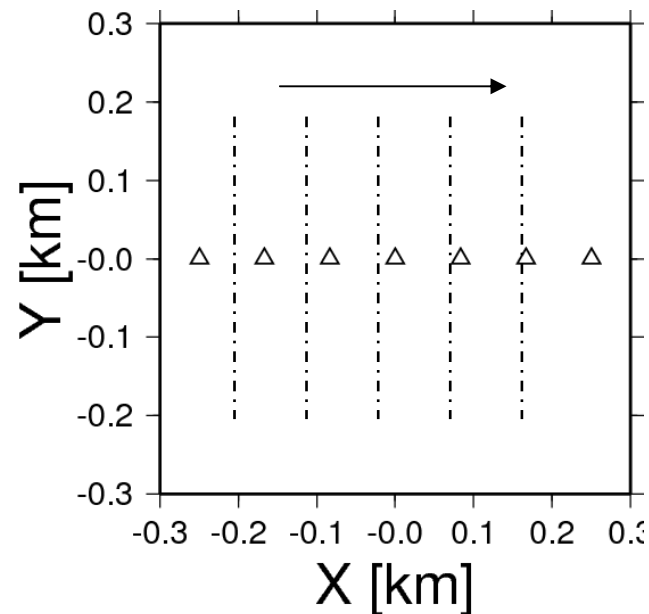
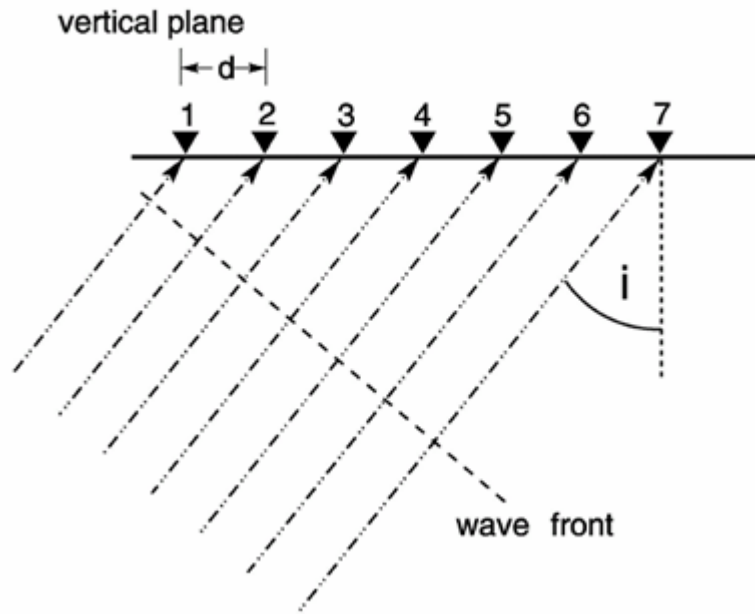
$$A(\vec{u} - \vec{u}_0, \omega) = \left| \frac{1}{N} \sum_{i=1}^N \exp(j\omega \vec{r}_i (\vec{u} - \vec{u}_0)) \right|$$

in wavenumber:

$$A(\vec{k} - \vec{k}_0) = \left| \frac{1}{N} \sum_{i=1}^N \exp(j\vec{r}_i (\vec{k} - \vec{k}_0)) \right|$$

Estimating the quality of an array ARRAY RESPONSE

Array response function, starting with simplest layout



Array response – parametrization of array geometry Starting simple – 1D line of receivers, spaced equidistantly

For the linear array example, we need only 2 parameters to describe the array geometry:

d_{min} = interstation distance

N = number of sensors

$(N-1)d_{min} = D_{max} = \text{Aperture}$

Station positions are then uniquely defined by $\vec{r}_i \rightarrow id_{min}$

In this linear problem the wavenumber vector reduces to its x-component: $\vec{k} - \vec{k}_0 \rightarrow k_x - k_0$

and therefore the wavenumber response:

$$\left| A(\vec{k} - \vec{k}_0) \right| = |A(k_x - k_0)|$$

Array response – parametrization of array geometry Starting simple – 1D line of receivers, spaced equidistantly

The 1D array response is then written as:

$$|A(k_x - k_0)| = \left| \frac{1}{N} \sum_{i=1}^N \exp(jid_{min}(k_x - k_0)) \right|$$

Note: expression is periodic in x-component

Periodicity at:

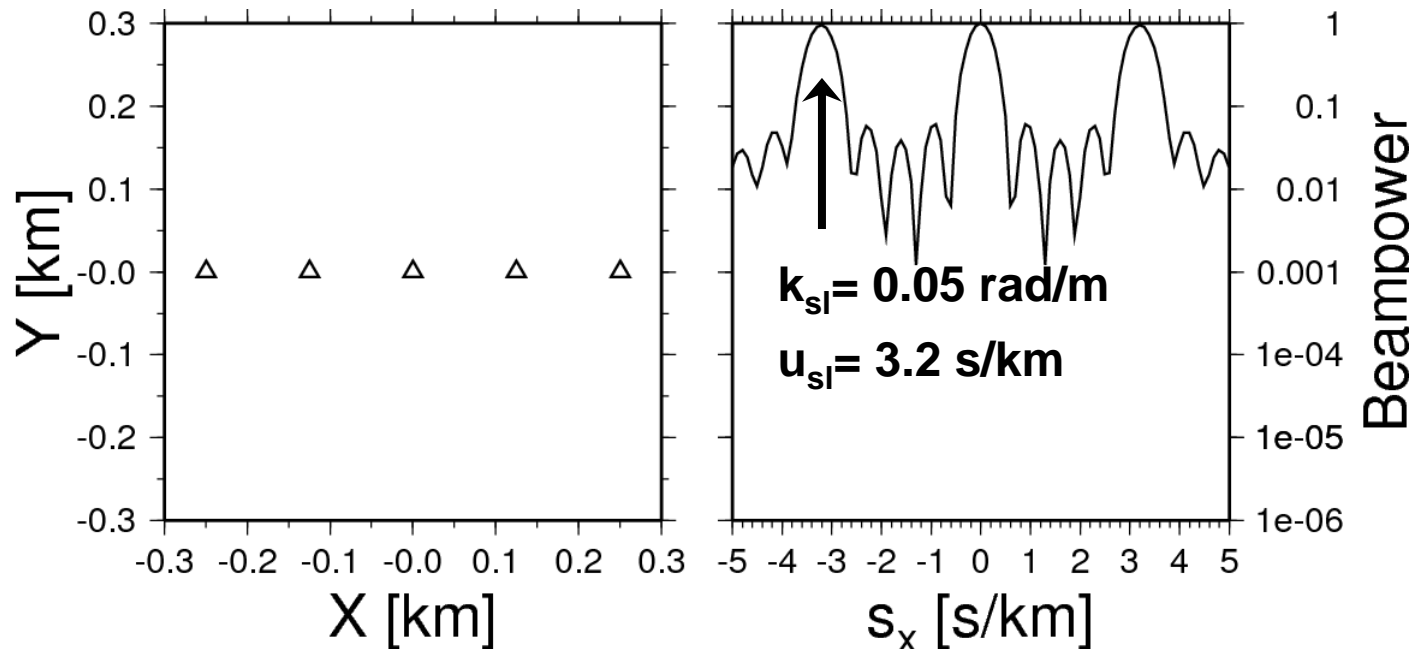
$$k_{sidelobe} = 2\pi/d_{min} \Rightarrow u_{sidelobe} = 1/(fd_{min})$$

width of main lobe: $2\pi/((N - 1)d_{min}) \rightarrow 2\pi/D_{max}$

Array response – parametrization of array geometry

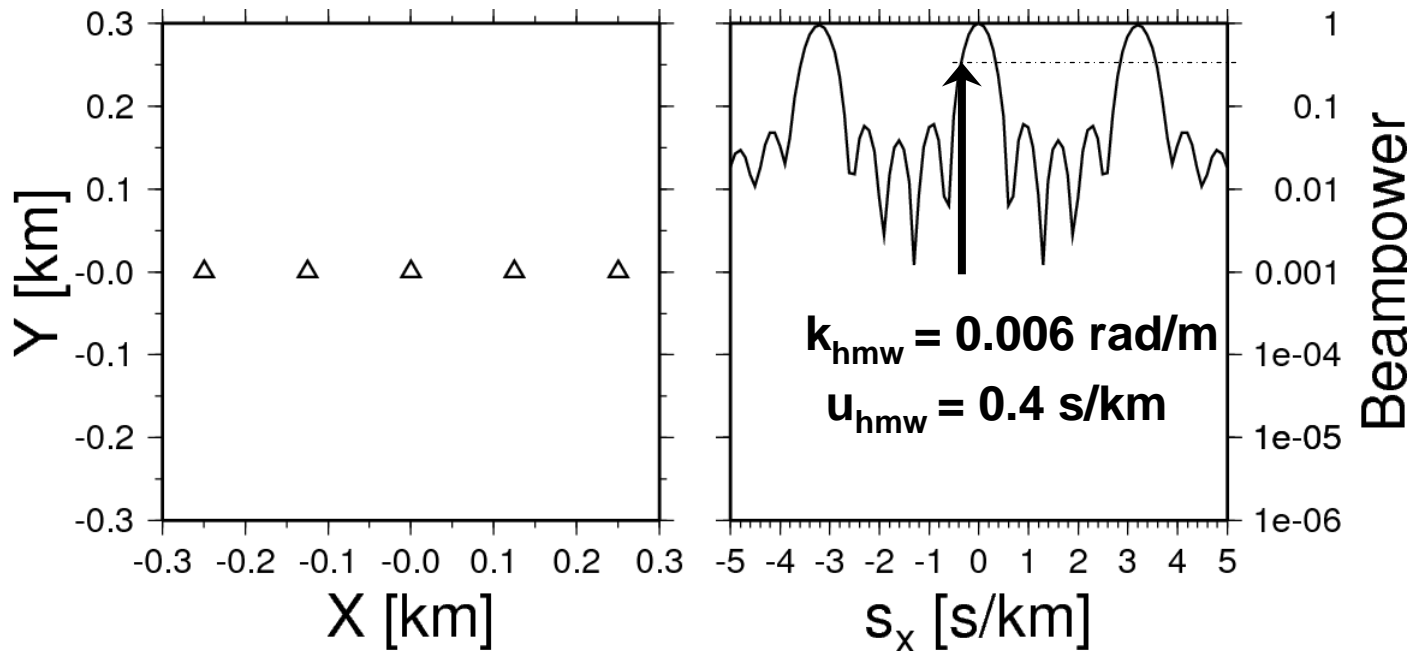
Starting simple – 1D line of receivers, spaced equidistantly

Example: $N = 5$ sensors, $d_{\min} = 125$ m (in slowness @2.5 Hz)



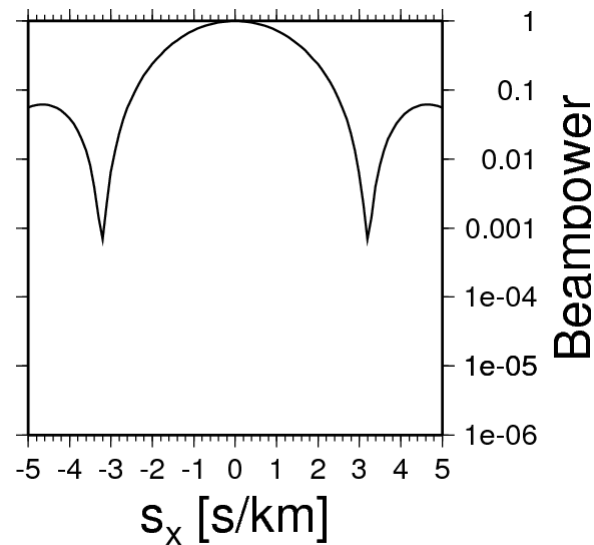
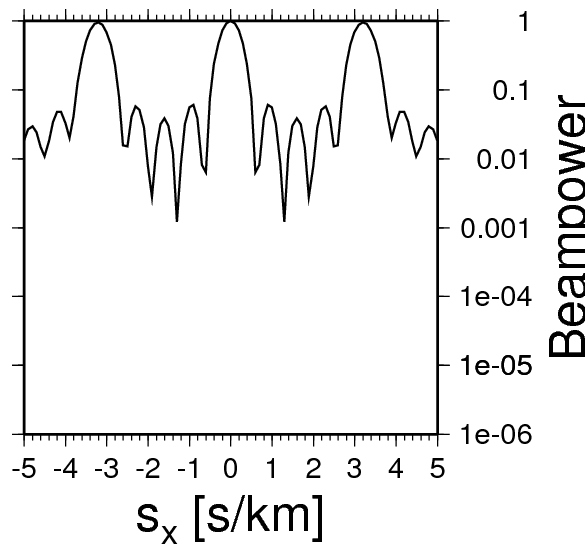
Array response – parametrization of array geometry Starting simple – 1D line of receivers, spaced equidistantly

Example: $N = 5$ sensors, $d_{\min} = 125$ m (in slowness @2.5 Hz)



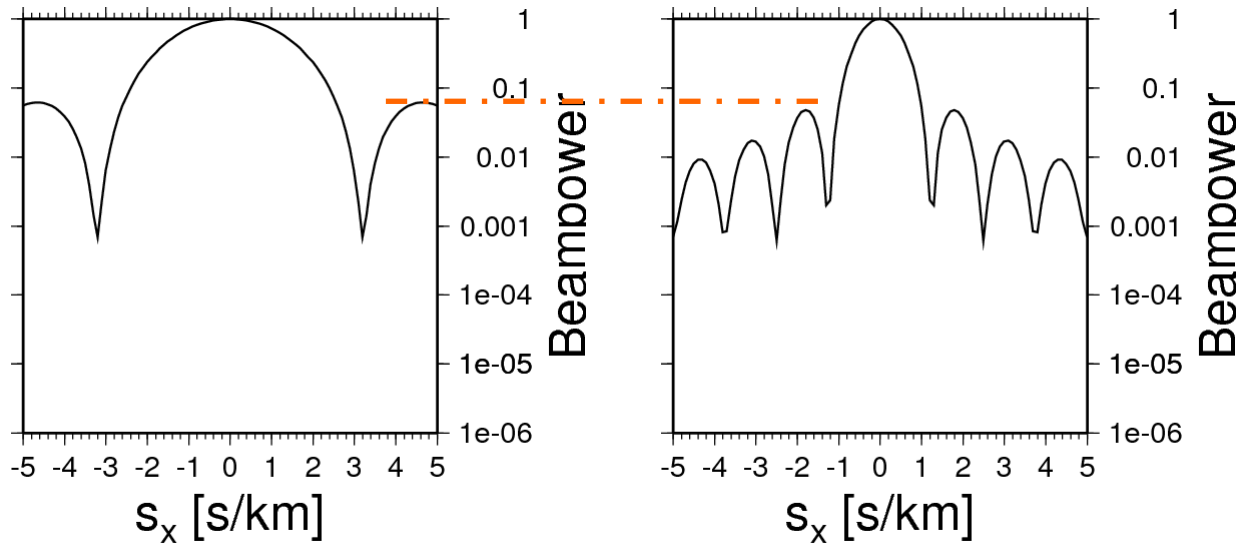
Array response – parametrization of array geometry 1D layout – parameter influence – interstation distance d_{\min}

$N = 5, d_{\min} = 125 \text{ m} \rightarrow d_{\min} = 25 \text{ m}$

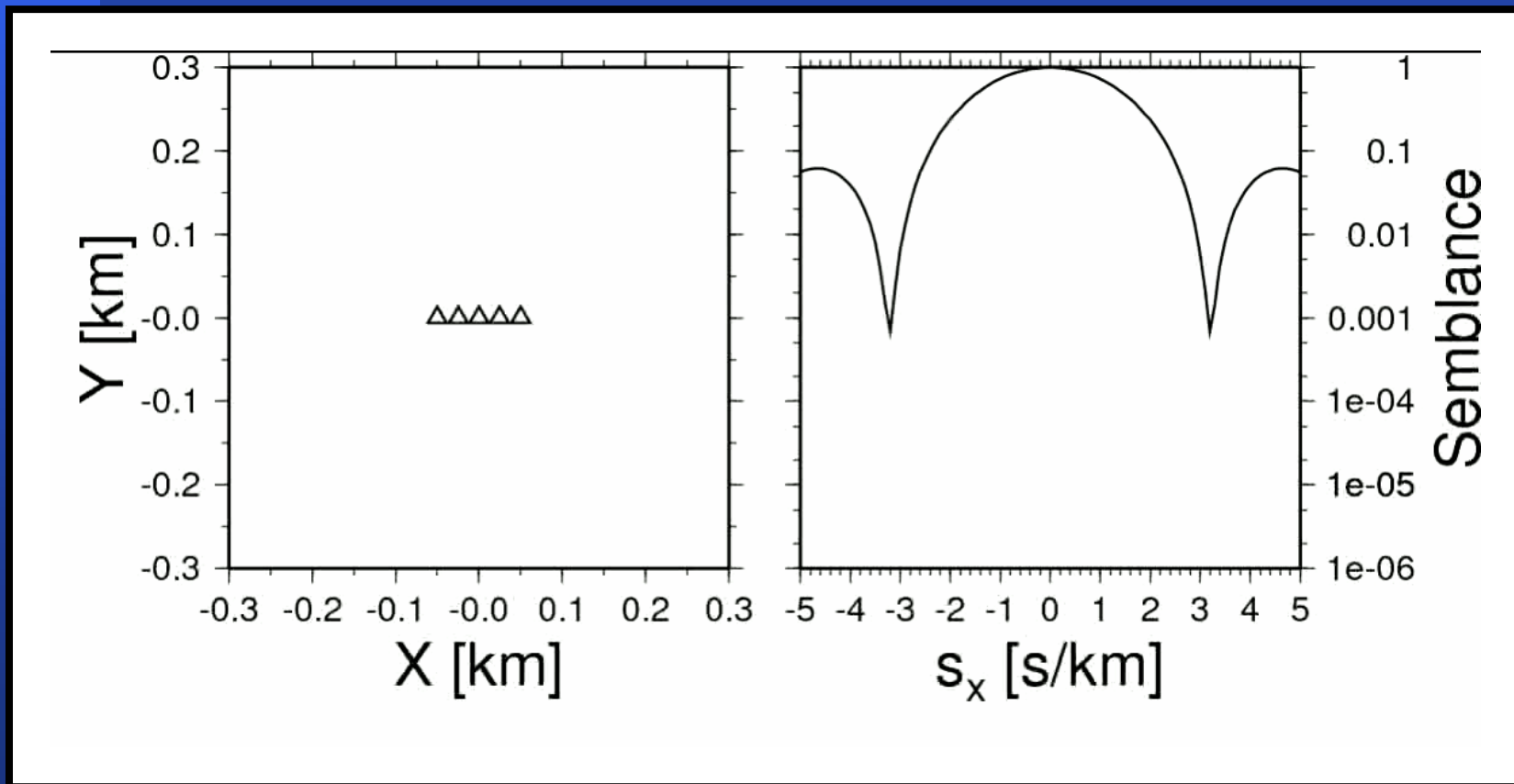


Array response – parametrization of array geometry 1D layout – parameter influence – number of stations N

$d_{\min} = 25 \text{ m}, N = 5 \rightarrow N = 15$

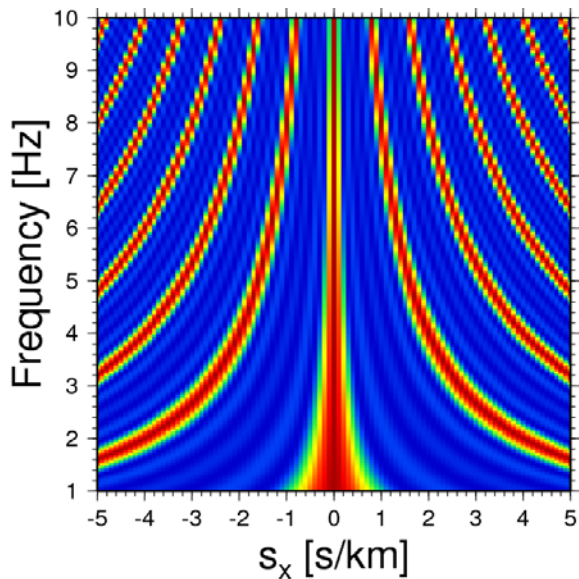


Array response – parametrization of array geometry 1D layout – parameter influence...

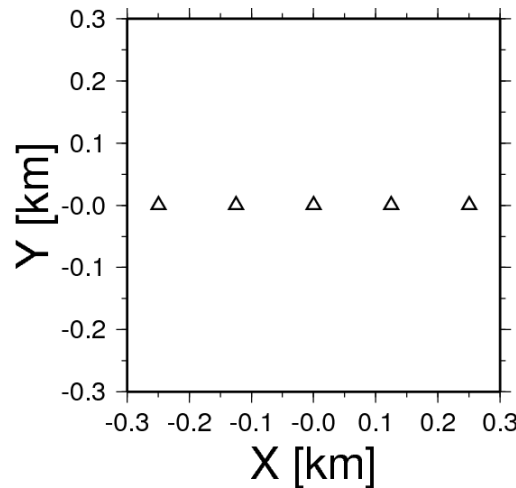


Array response – 1D layout – parameter influence broadband frequency wavenumber approach

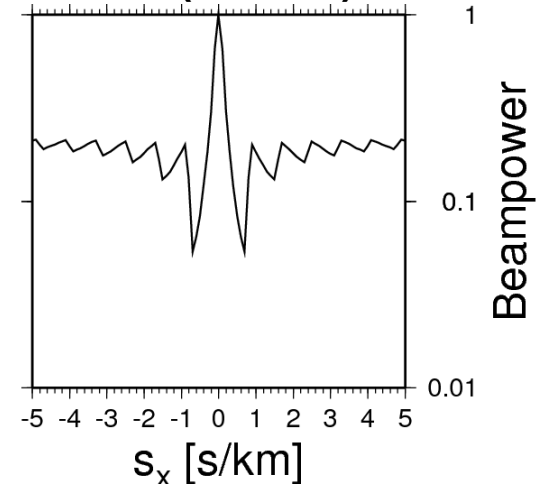
1D array reponse (1-10 Hz)



Linear array layout

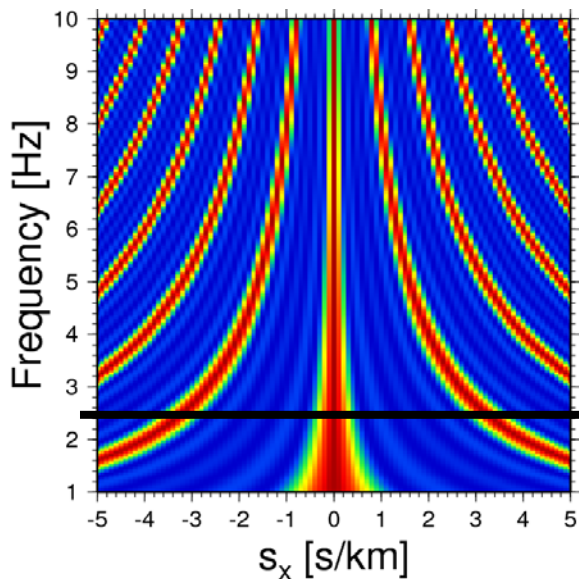


broadband response (1-10 Hz)

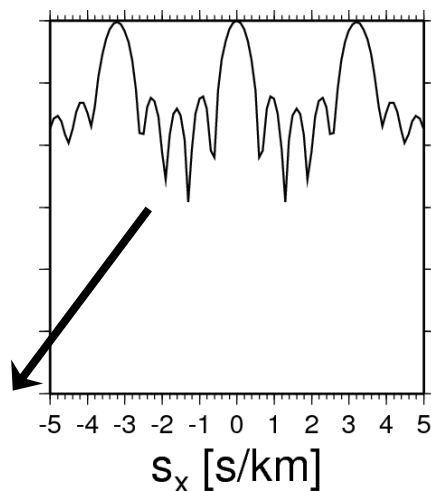


Array response – 1D layout – parameter influence broadband frequency wavenumber approach

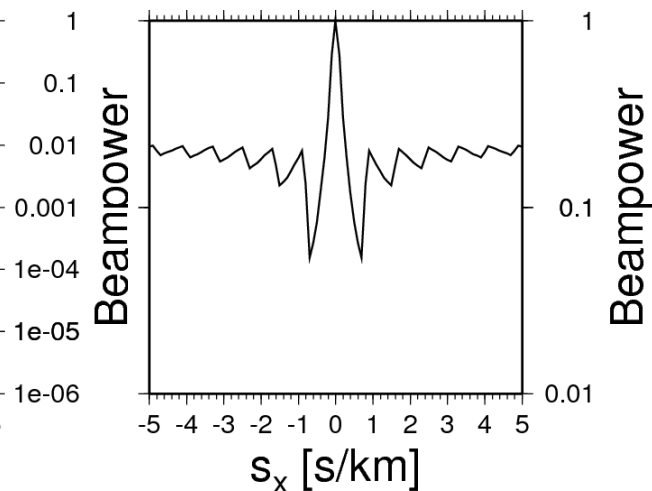
1D array reponse (1-10 Hz)



Array response @ 2.5 Hz



summation of all responses



broadband response (1-10 Hz)

Array geometry and discrete spatial sampling of a continuous wavefield

Array measurements can be seen as:

a **discrete spatial sampling** of a **continuous process**



sensor locations



**seismic wavefield
(1D/2D/3D projection)**

**For 1D linear arrays with equidistant spacing
the equivalence to time series sampling
is easy to recognize**

Array geometry and discrete spatial sampling of a continuous wavefield

discrete spatial sampling of a continuous process

consequences: **aliasing (sampling theorem)**

at least 3 samples per period, wavelength

time domain $\Delta T < T_{min}/2$

spatial domain $\Delta x < \lambda_{min}^*/2$ * apparent

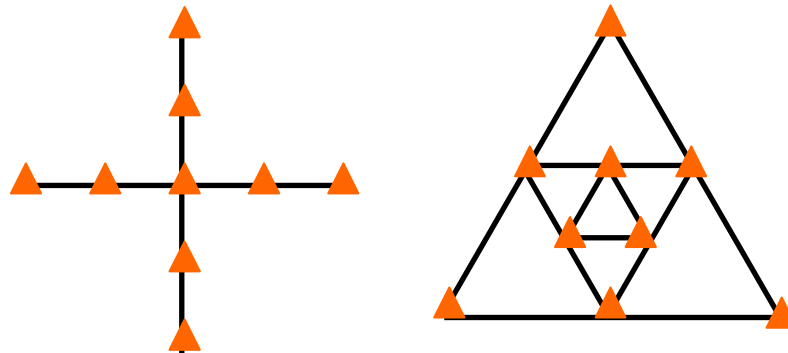
spectral resolution limit

time domain $\Delta \omega = 2\pi / ((N - 1)\Delta T)$

spatial domain $\Delta k = 2\pi / ((N - 1)d_{min}) = 2\pi / D_{max}$

Array response Extension to 2D situation – planar arrays

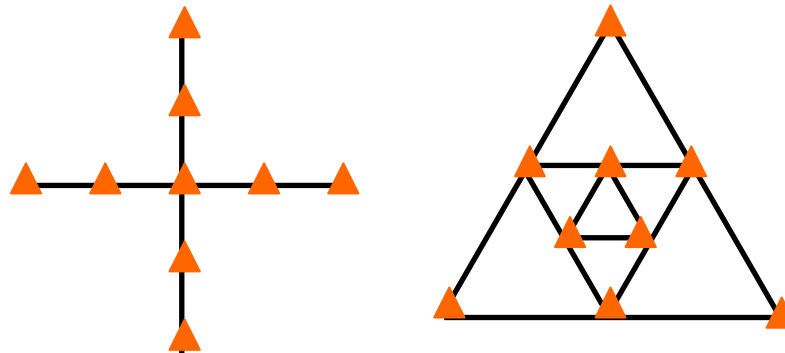
$$A(\vec{u} - \vec{u}_0, \omega) = \left| \frac{1}{N} \sum_{i=1}^N \exp(j\omega \vec{r}_i(\vec{u} - \vec{u}_0)) \right|$$



$$A(\vec{k} - \vec{k}_0) = \left| \frac{1}{N} \sum_{i=1}^N \exp(j\vec{r}_i(\vec{k} - \vec{k}_0)) \right|$$

Array response Extension to 2D situation – planar arrays

similar story as for 1D-layouts,
BUT parametrization more difficult

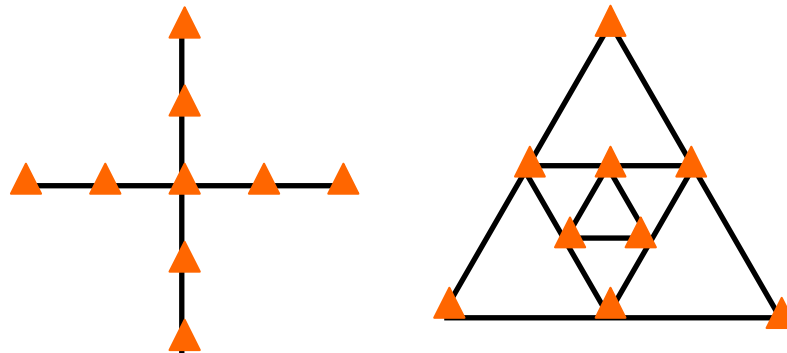


d_{\min} , N , D_{\max} (aperture)

Array response Extension to 2D situation – planar arrays

N clear

BUT: d_{\min} and D_{\max} show directional dependence

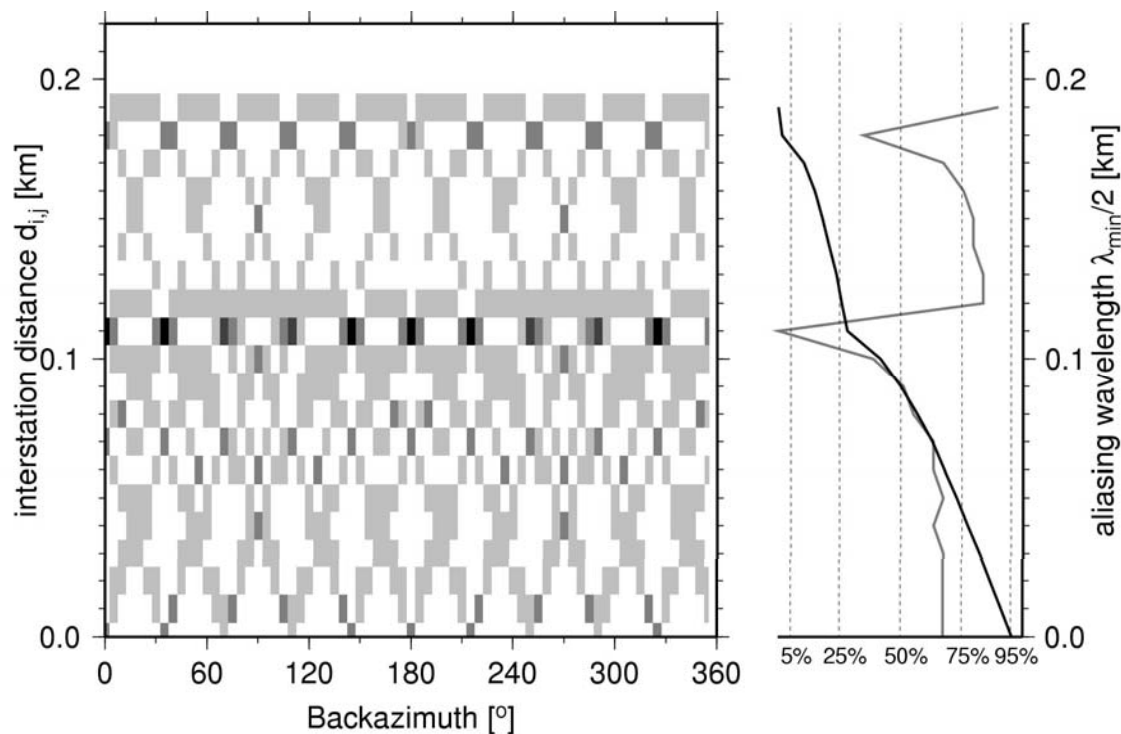


especially there will always be some direction, in which d_{\min} is vanishing!

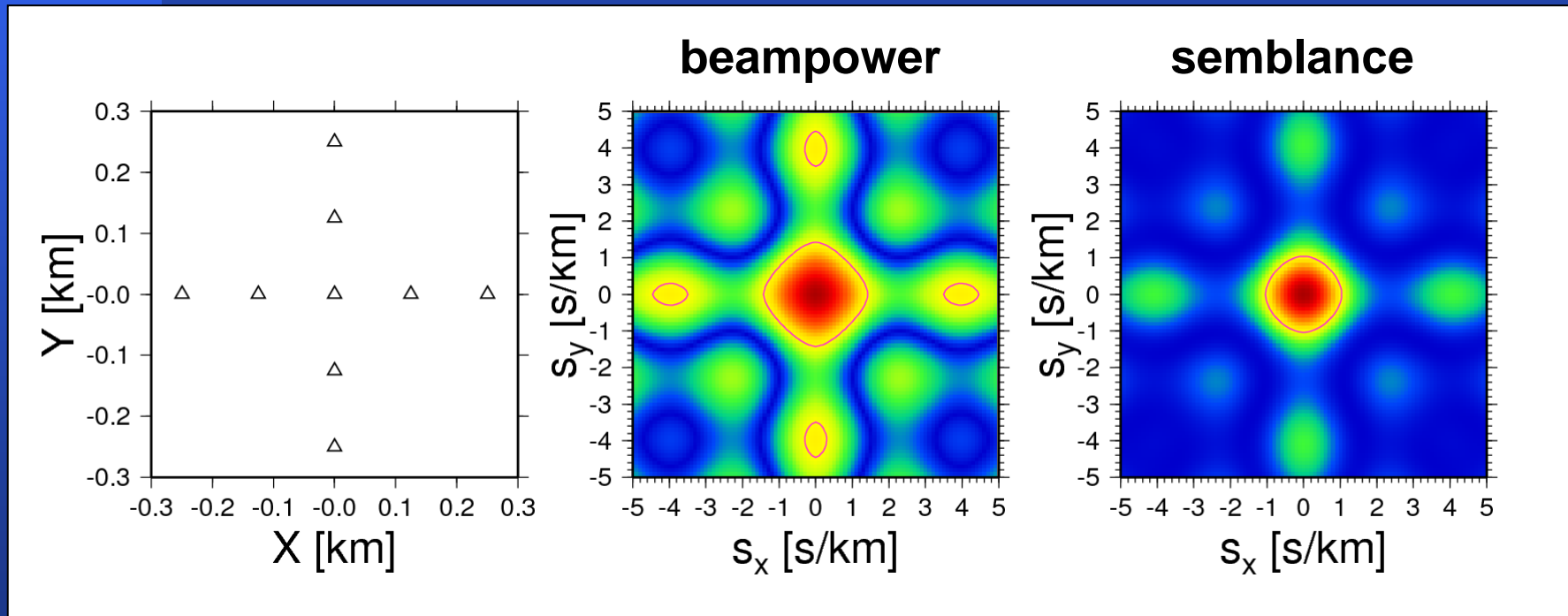
limits of array geometry: $\lambda_{\min} > 2d_{\min}$, $\lambda_{\max} \sim 3D_{\max}$

Array response Extension to 2D situation – planar arrays

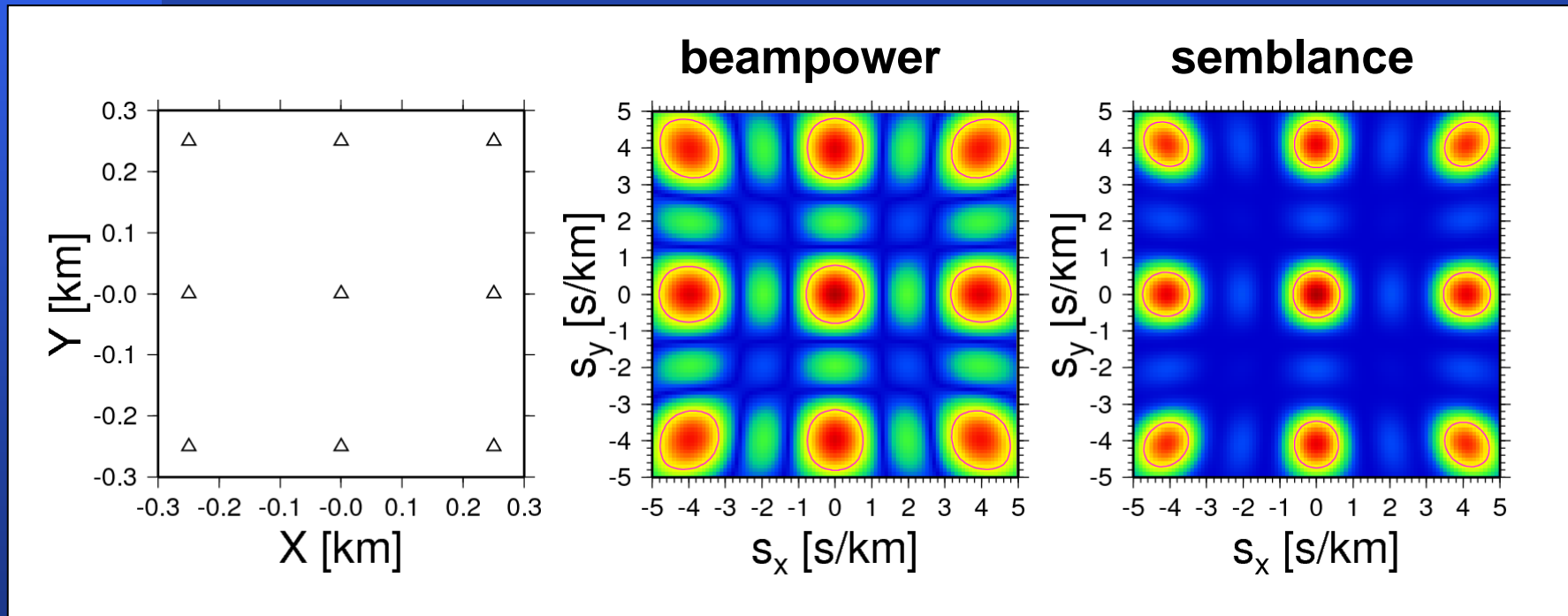
d_{\min} and D_{\max} show directional dependence



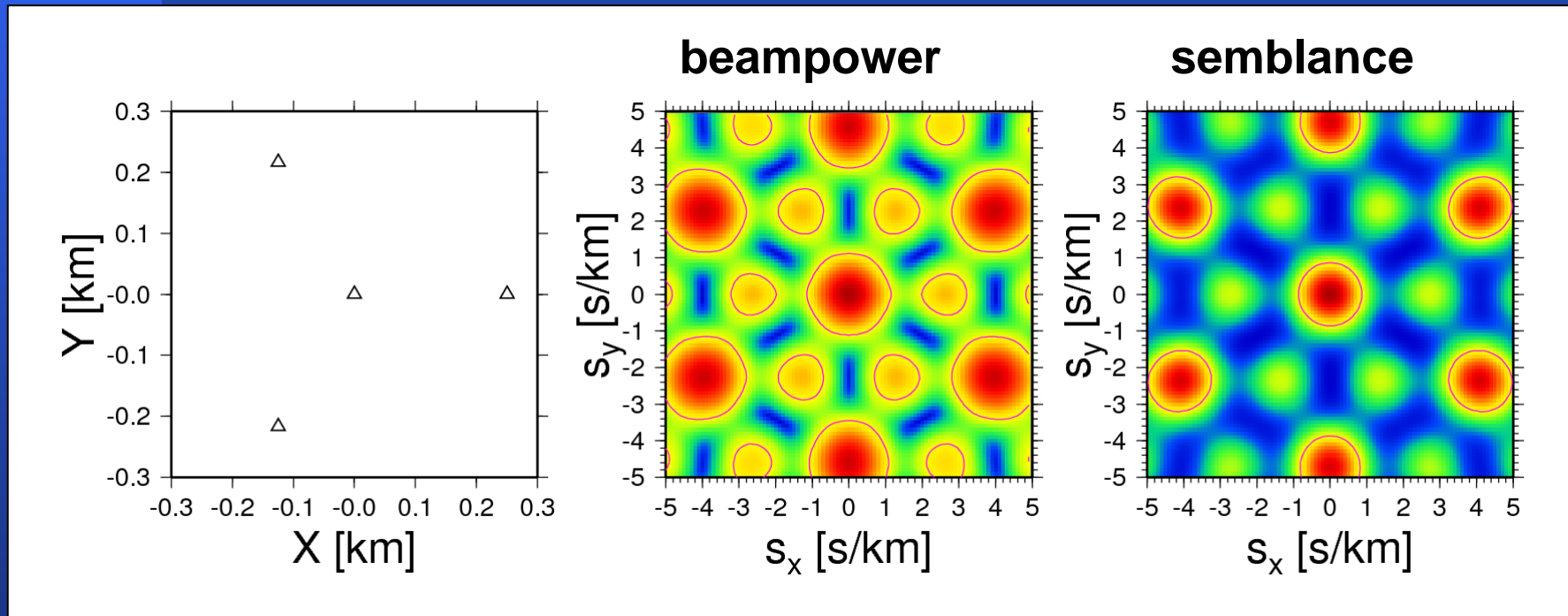
Some examples for typical symmetric array geometries



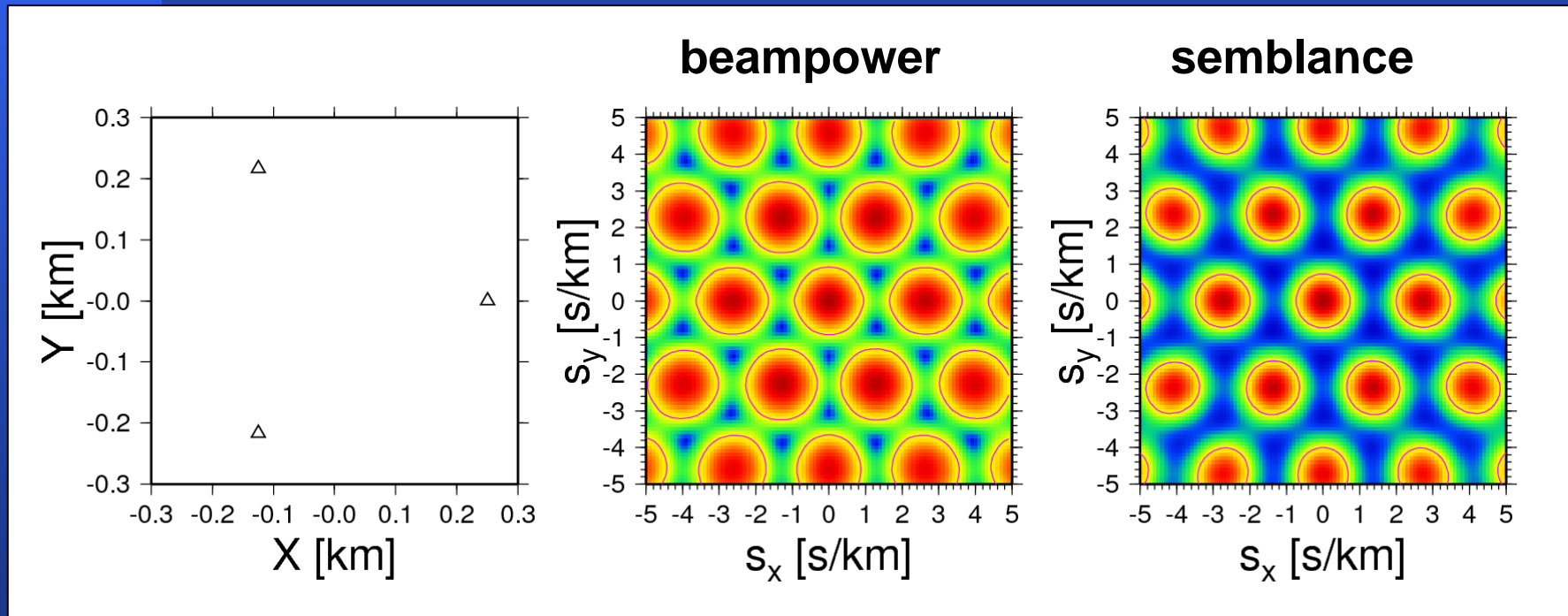
Some examples for typical symmetric array geometries



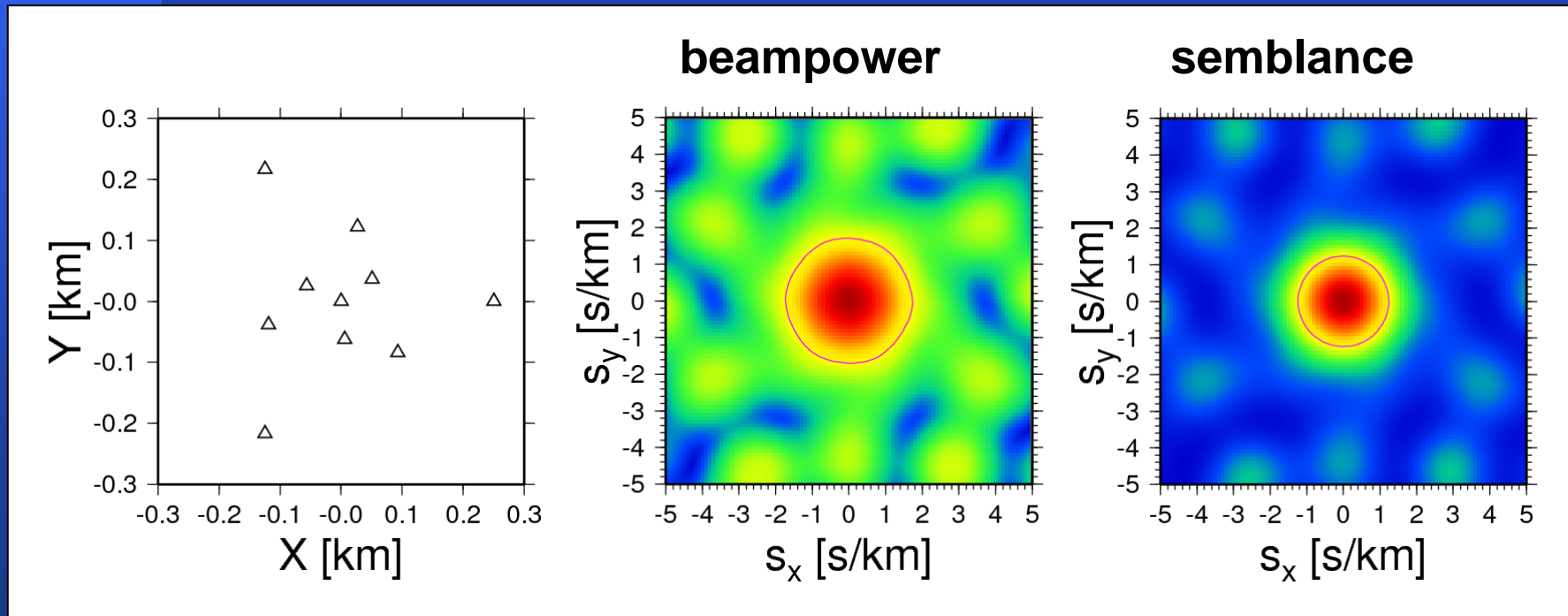
Some examples for typical symmetric array geometries



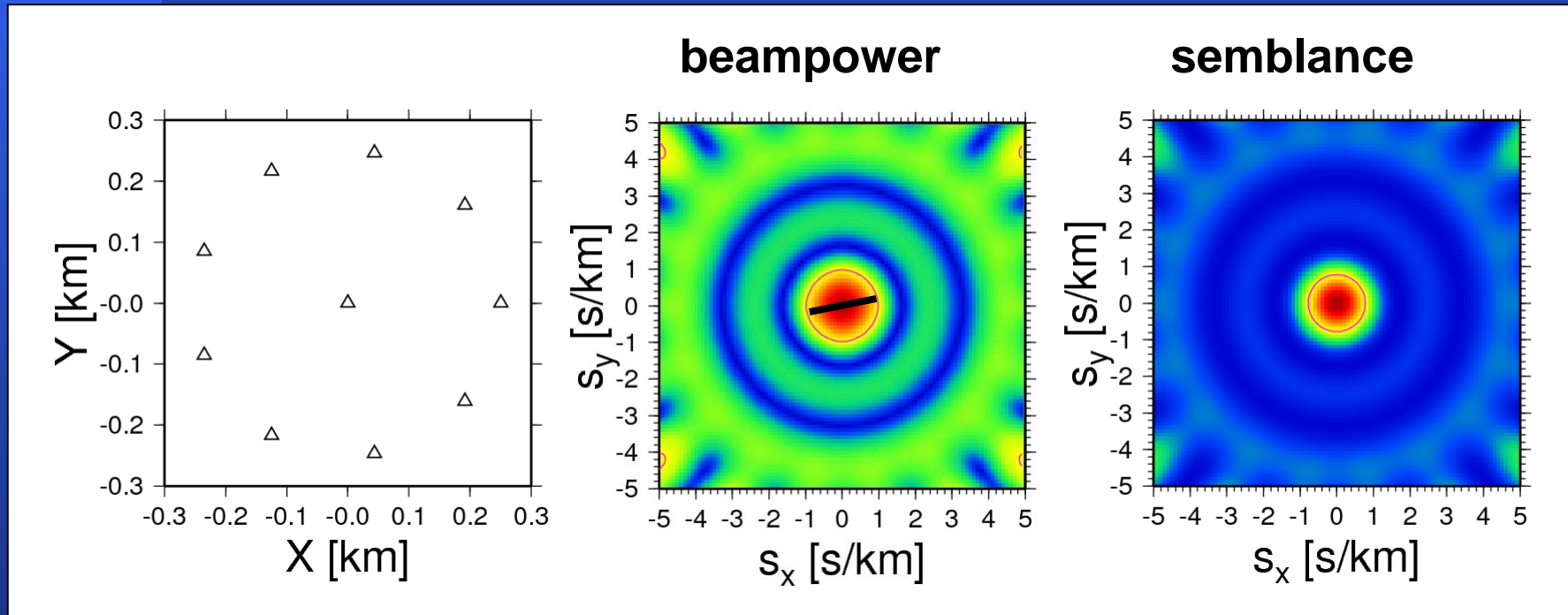
Some examples for typical symmetric array geometries



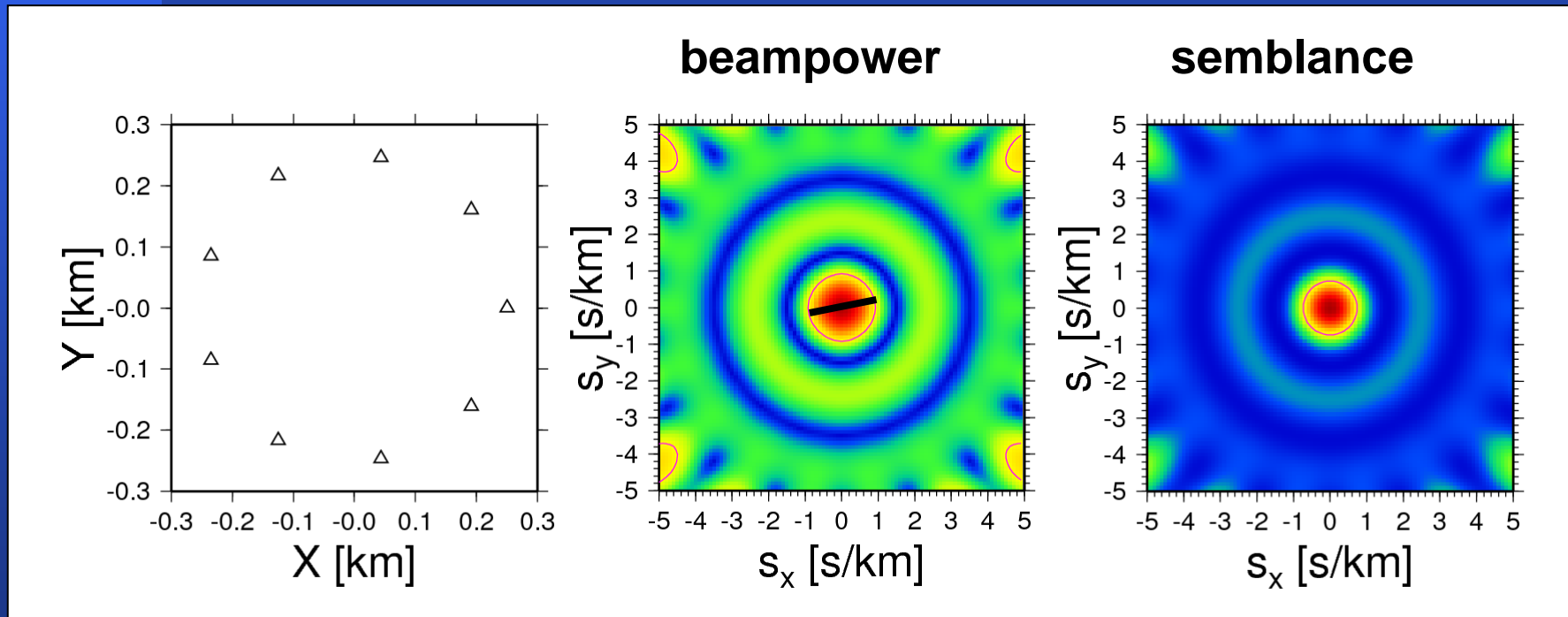
Some examples for typical symmetric array geometries



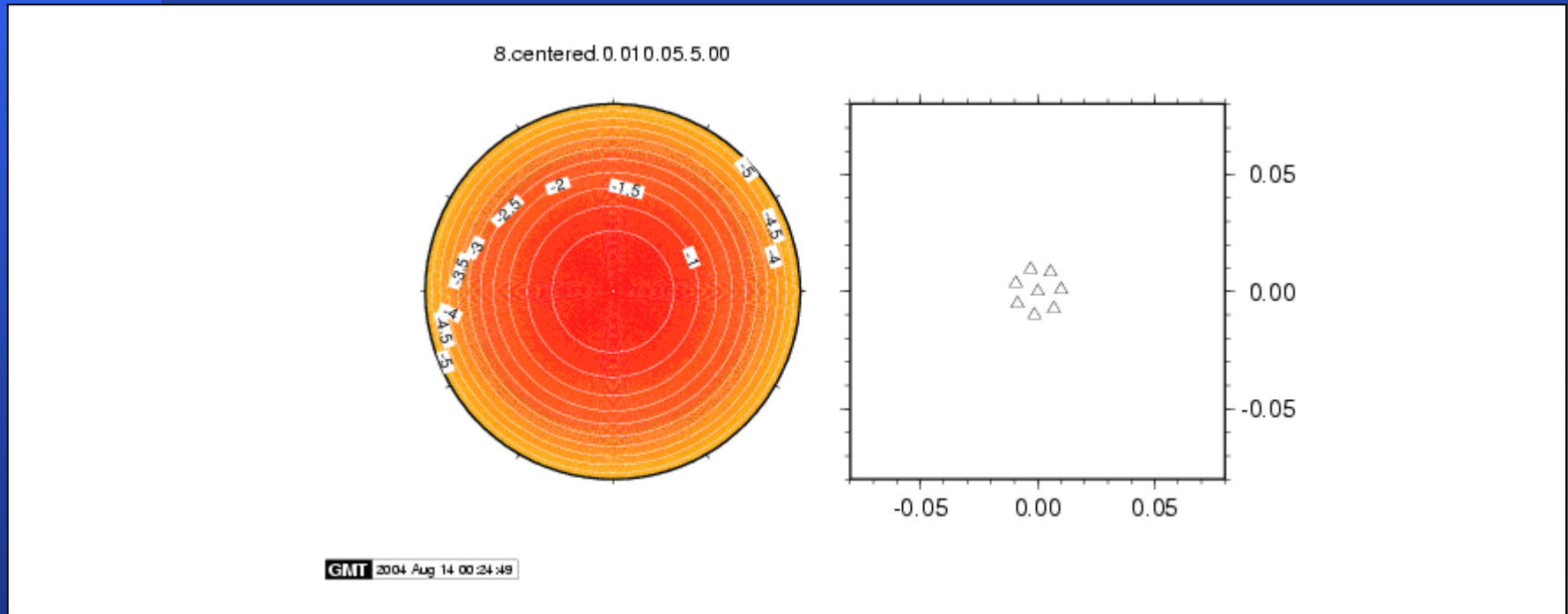
Some examples for typical symmetric array geometries



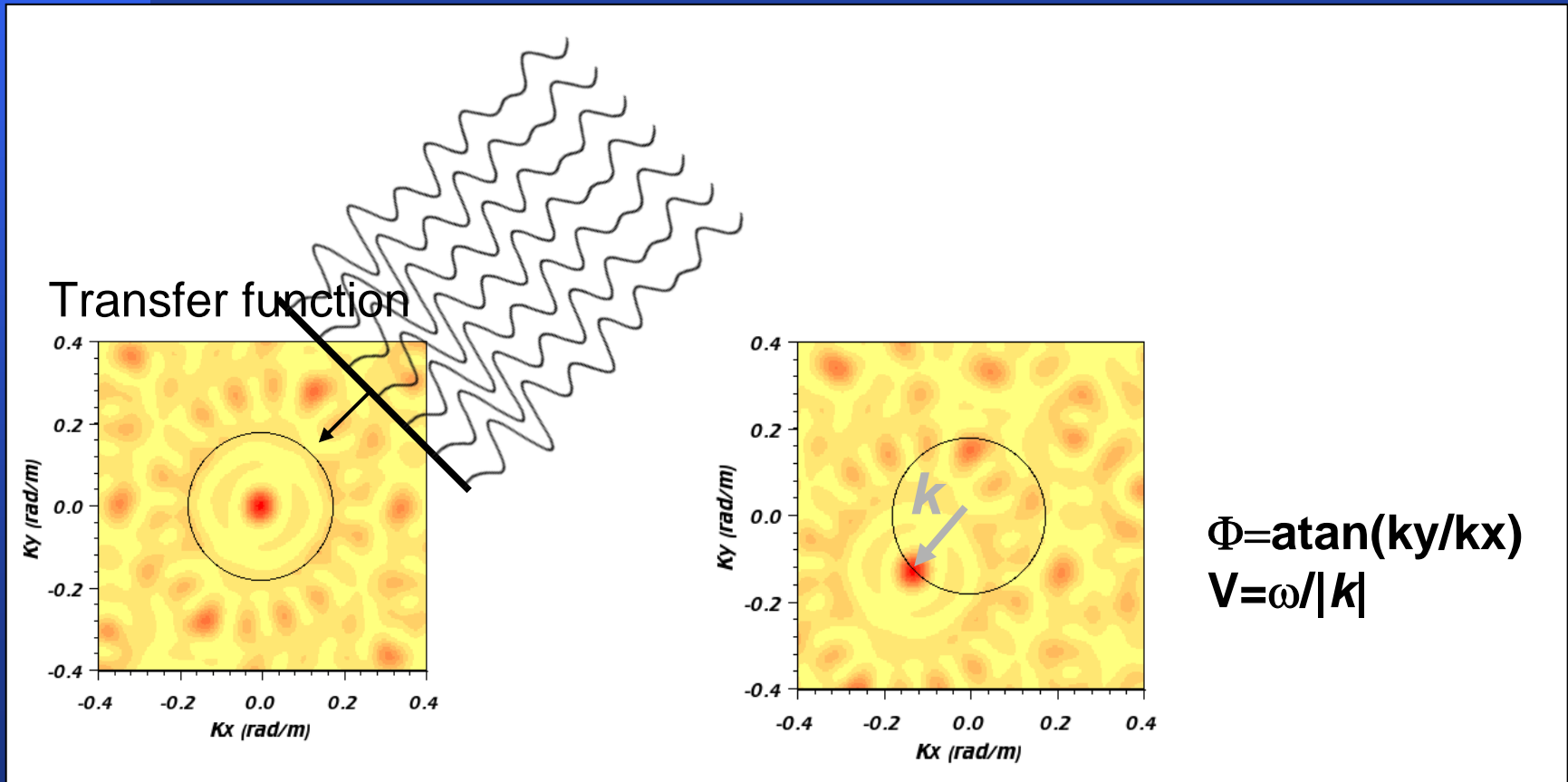
Some examples for typical symmetric array geometries



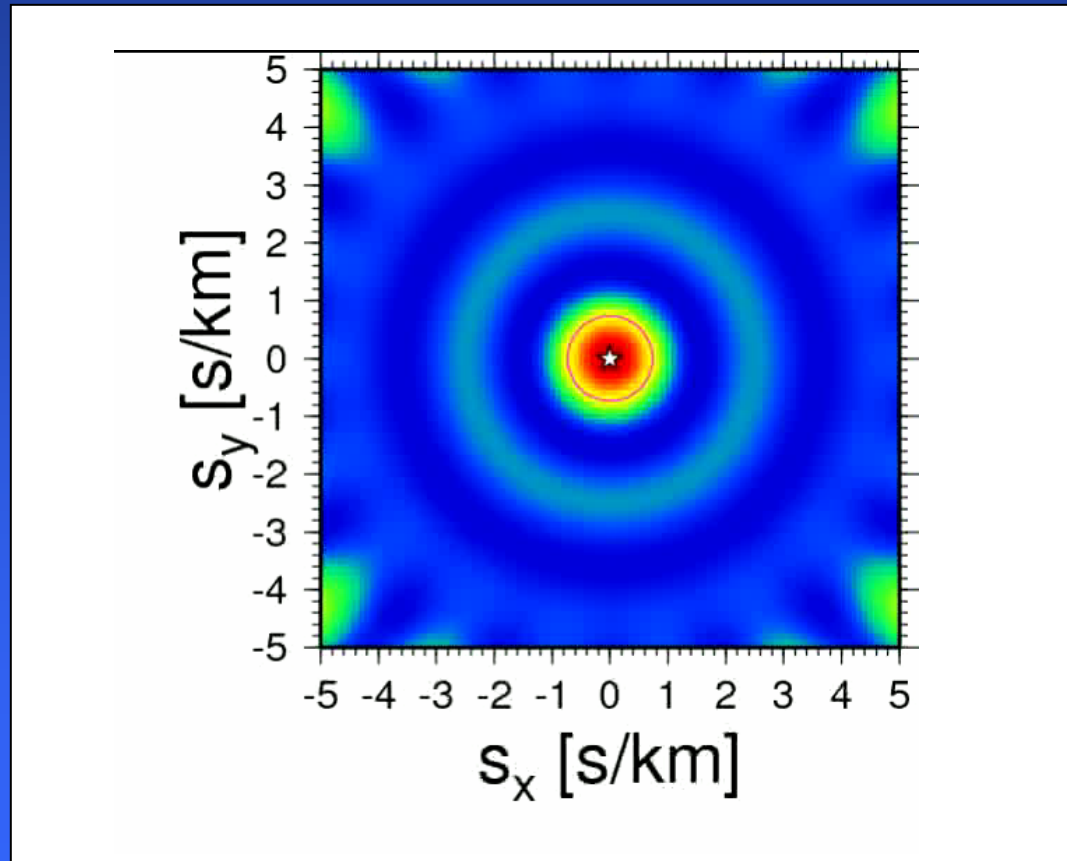
Some examples for typical symmetric array geometries



Array response moves with true slowness

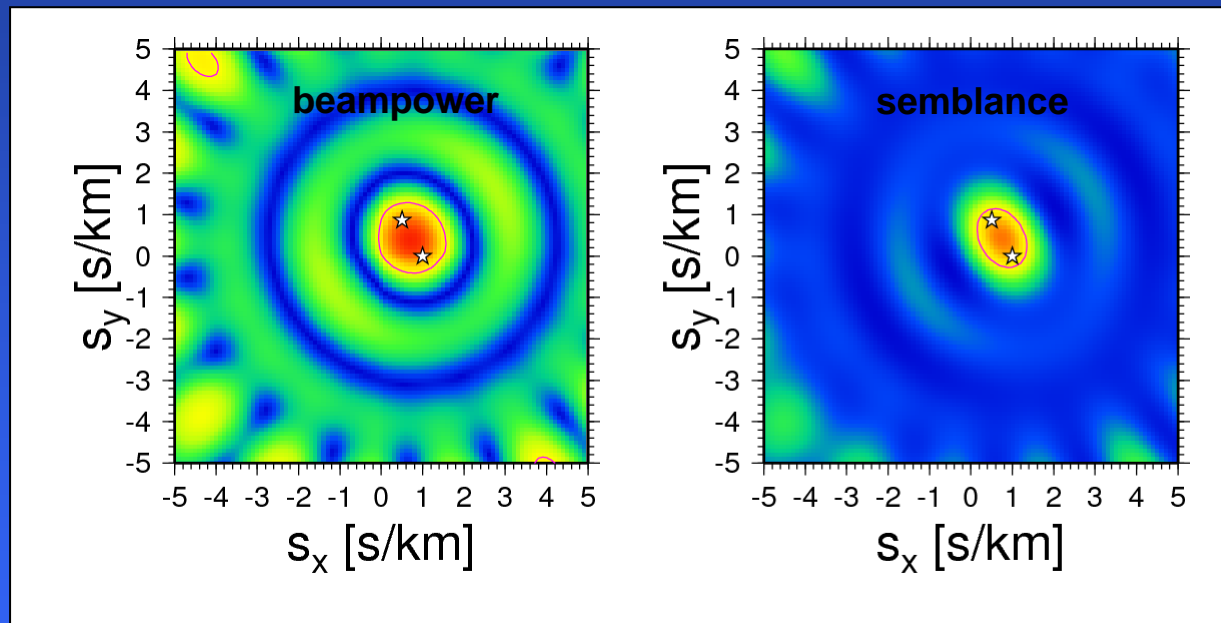


Array response moves with true slowness



2D Array response – resolution limit?

2 sources, pure harmonic waves for [f_{low}, f_{high}] = [0.9, 1.1] Hz

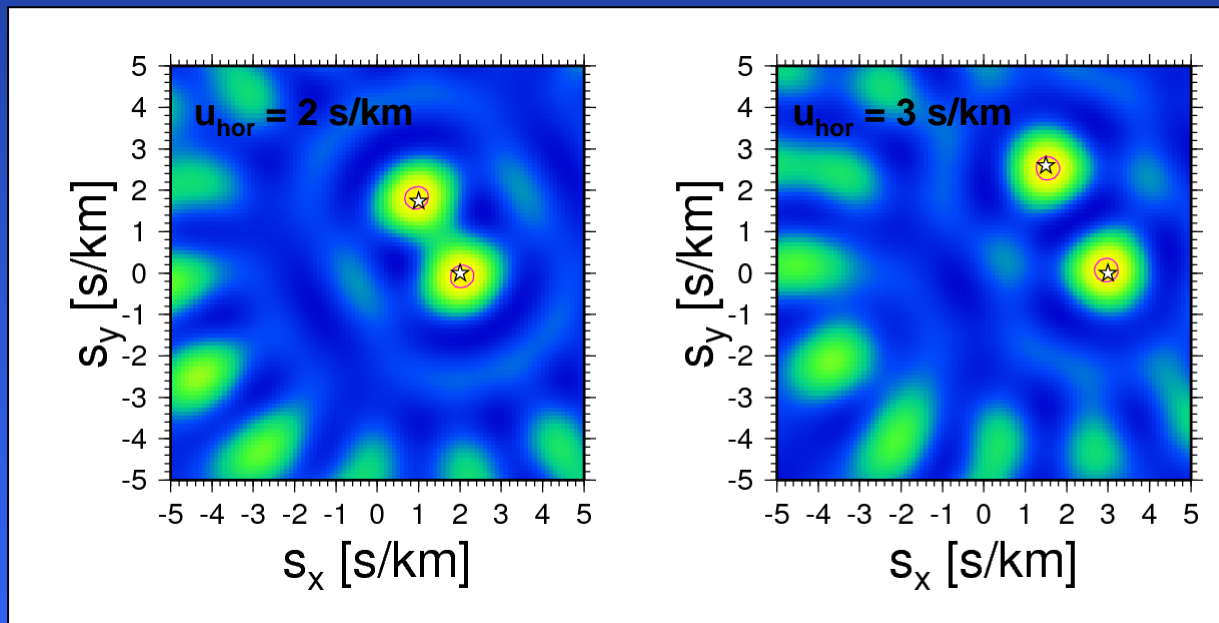


Waveparameter source A: $u_{\text{hor}} = 1 \text{ s/km}$, $\theta = 90^\circ$

Waveparameter source B: $u_{\text{hor}} = 1 \text{ s/km}$, $\theta = 30^\circ$

2D Array response – resolution limit?

2 sources, pure harmonic waves for $[f_{low}, f_{high}] = [0.9, 1.1]$ Hz



Waveparameter source A: $\theta = 90^\circ$

Waveparameter source B: $\theta = 30^\circ$

So far – so good – and now?

Now let's go finally to real life!

PURPOSE:

Using array techniques to analyze ambient vibration wavefields with the aim to derive shallow structural velocity models!

Background: Dispersion curve analysis

OVERVIEW: Array Analysis of Microtremor Wavefields Applying basic principles (general) to a special problem domain

- What is special with microtremor wavefields?
 - What is to be changed from the viewpoint of analysis?
 - What is to be changed from the viewpoint of geometries?
- Complications and attempts to deal with them

What is special with microtremor wavefields?

- low energetic wavefield
 - multiple sources
- unknown spatiotemporal structure of sources
 - unknown composition of wavefield,
strong assumptions necessary

What is to be changed from the viewpoint of analysis?

- **adapt processing scheme for narrowband analysis of continuous data streams:
processing of analysis windows with constant time-bandwidth product**
 - **uncertainty estimate required:
critical review of assumptions**
 - **critical interpretation of results**

What is to be changed from the viewpoint of geometries?

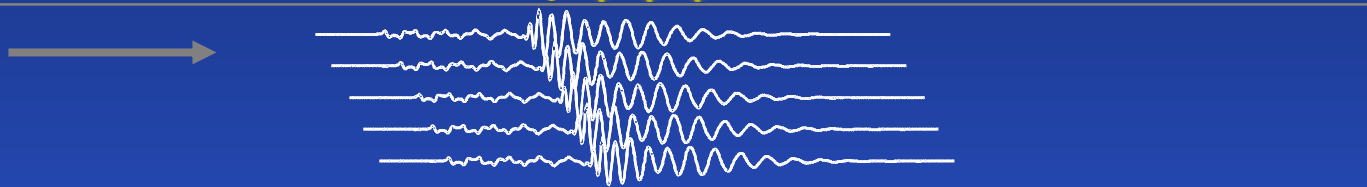
- temporal experiments → N relatively low
- usually urban environment → logistical constraints
 - no optimal single array configuration possible due to trade-off between number of stations, aperture and interstation distance
 - existence of (very) local sources which violates the plane wave assumption → avoid wherever possible!

Using Ambient Vibration Array Techniques for Site Characterisation

Source

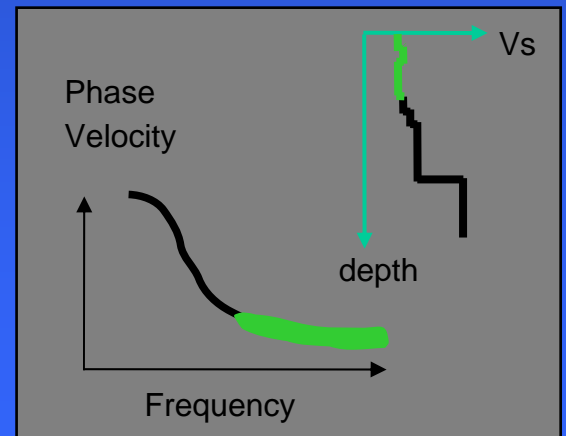
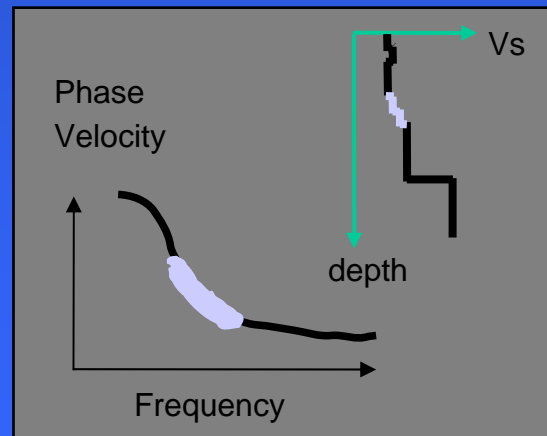
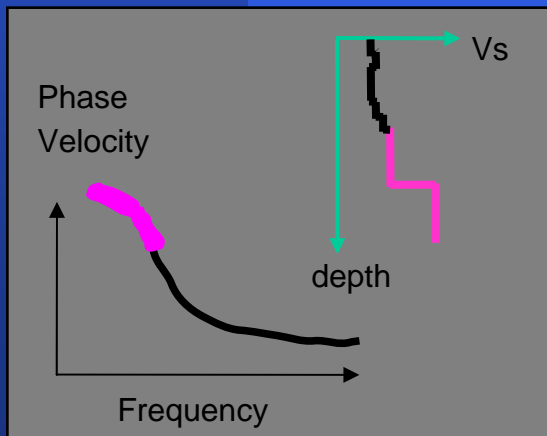
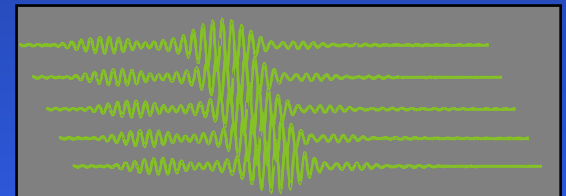
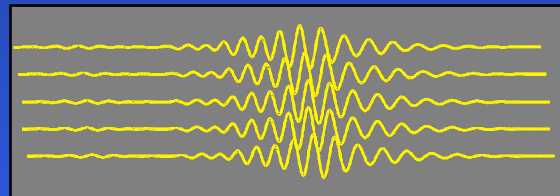
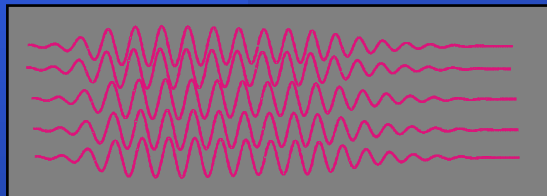


Sensors

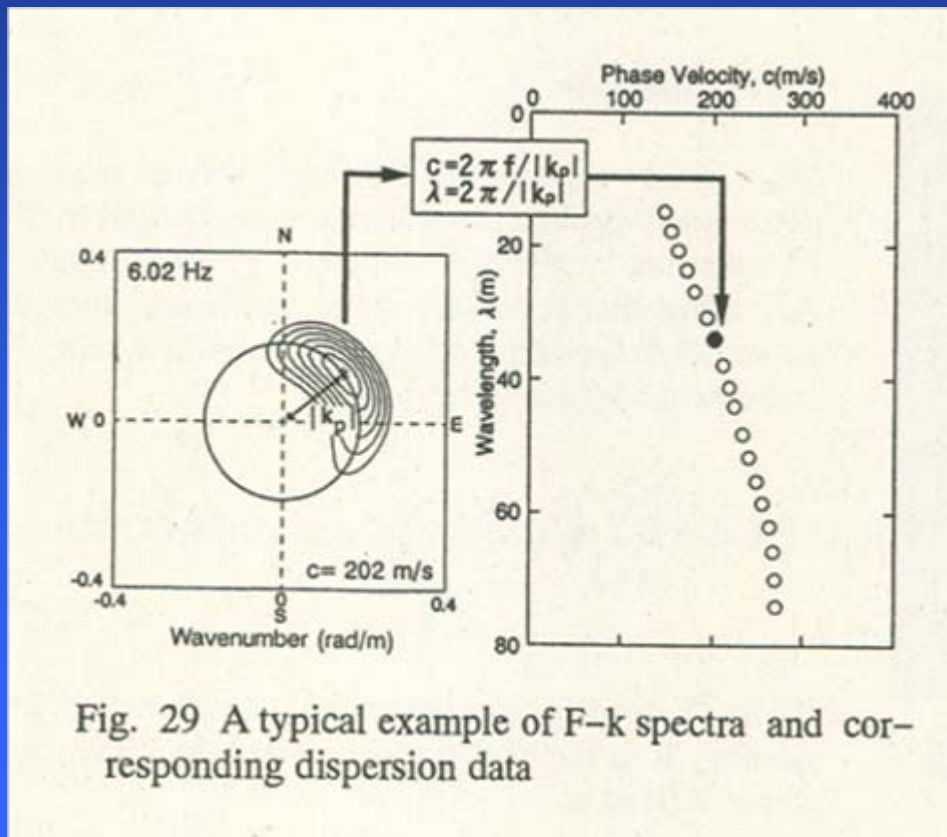


Low frequency

High frequency

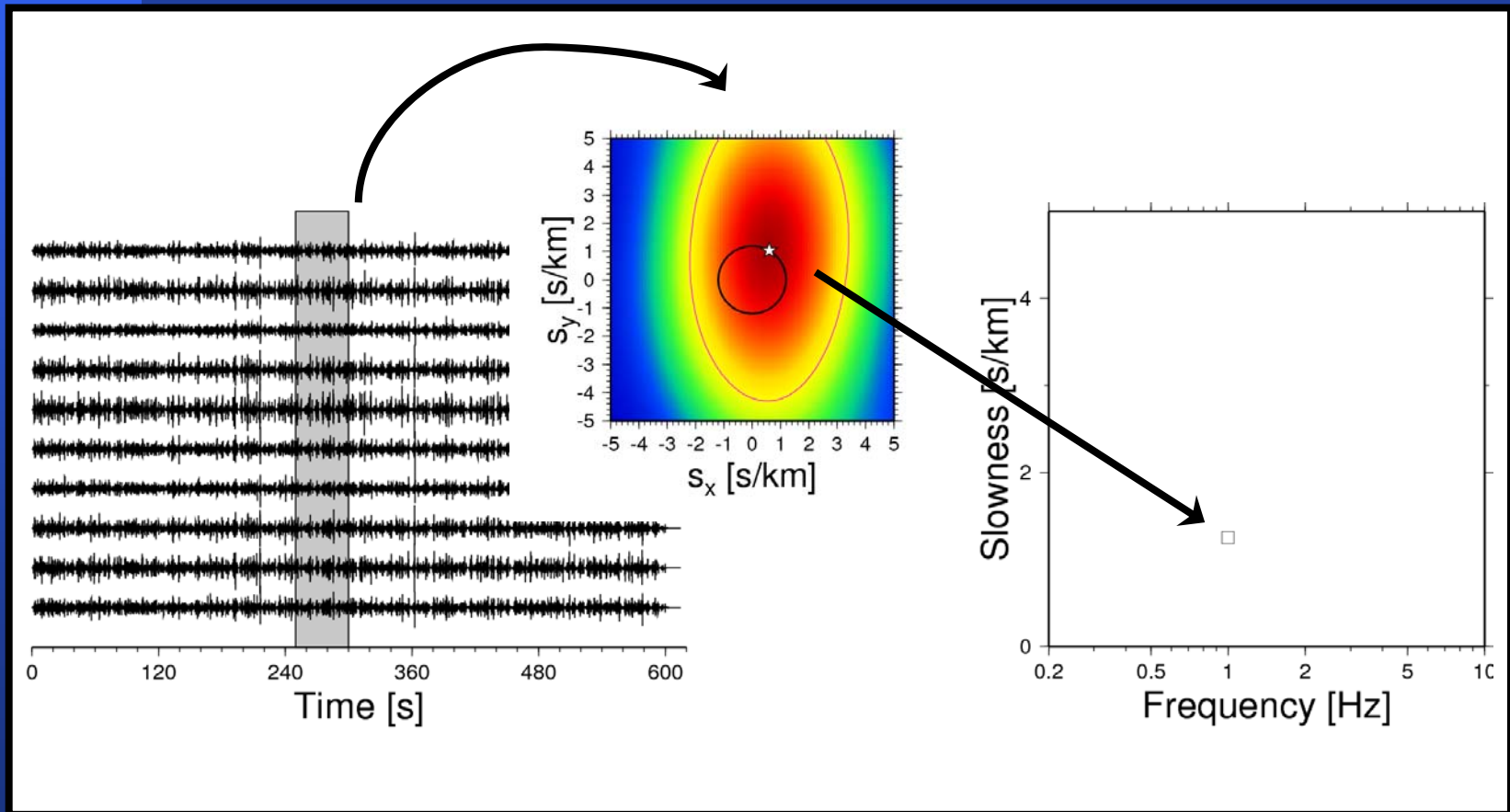


Derivation of dispersion curve - howto

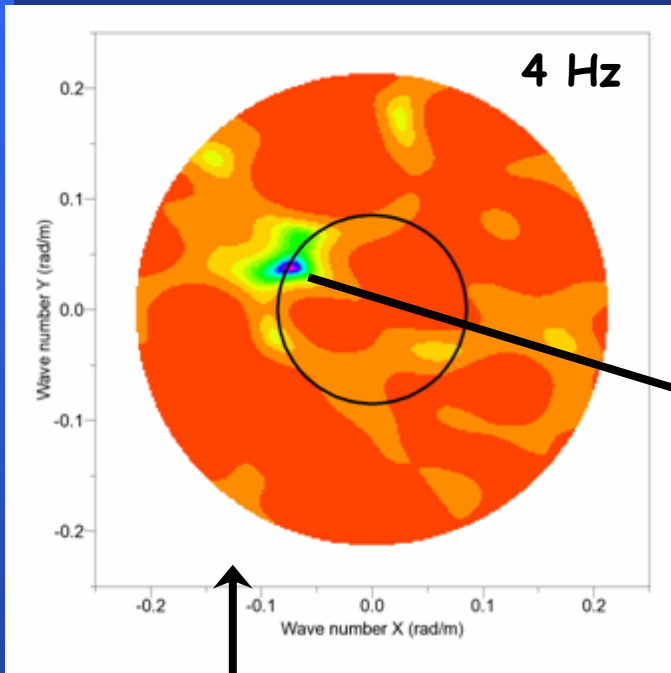


from Tokimatsu, 1997

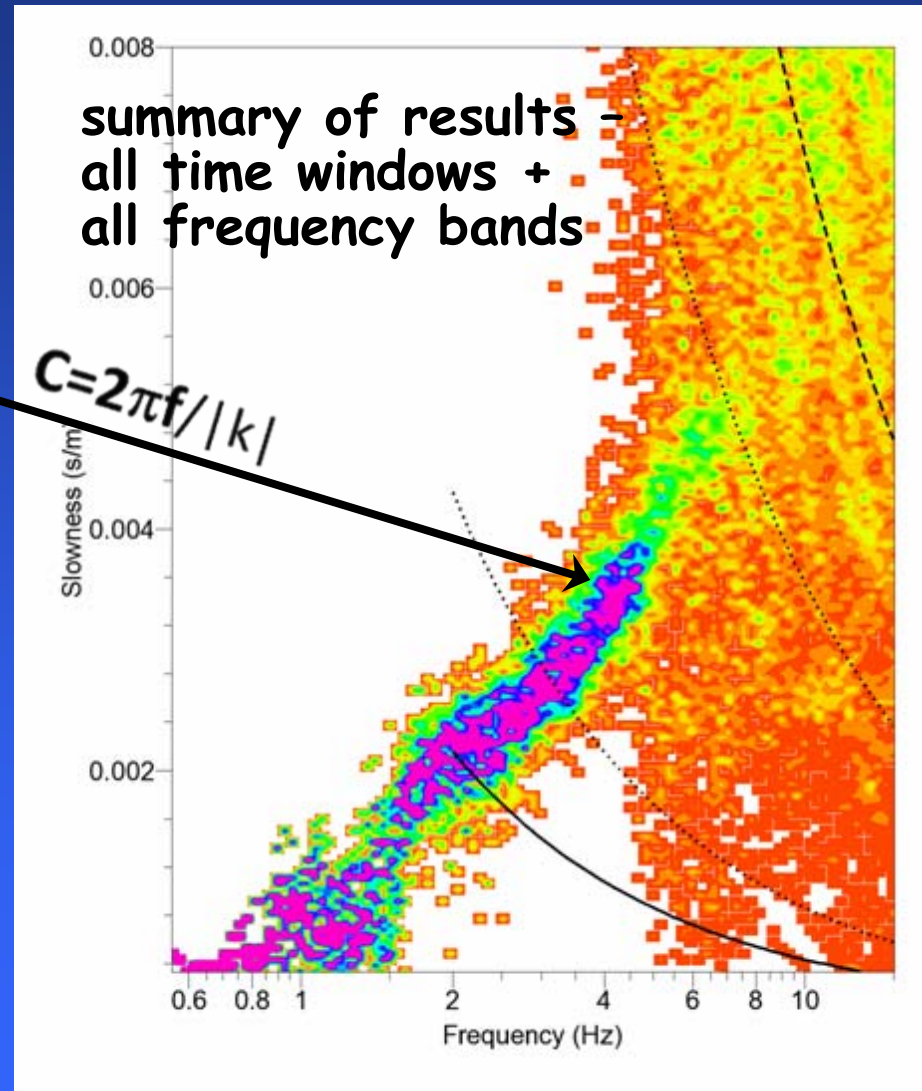
Derivation of dispersion curve - howto



Using Ambient Vibration Array Techniques for Site Characterisation



Single time window
f-k analysis result;
center frequency 4Hz
bandwidth as fraction
of center frequency





Using Ambient Vibration Array Techniques for Site Characterisation

