

Engineering Seismology and Seismic Hazard – 2019

Lecture 14

Measuring Earthquake Size

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Size Measure Types

There are basically two methods to quantify the earthquake size:

1) Maximum Intensity

- Outdated method based on damage description and human ground shaking perception
- Very subjective, not based on actual seismic recordings
- Still very used to quantify the size of historical (pre-instrumental) earthquakes

2) Magnitude

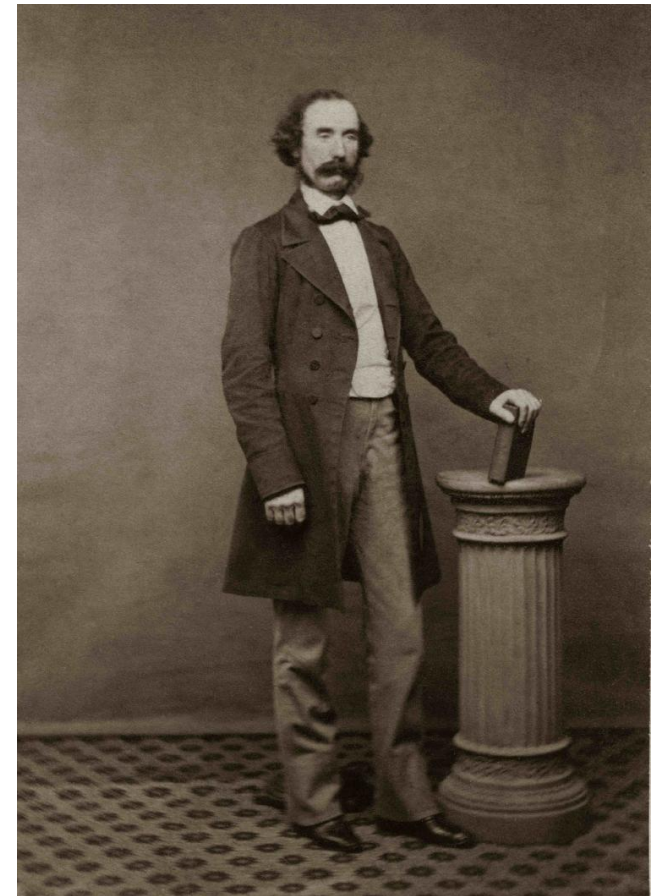
- Modern method based on measurable earthquake parameters
- Objective and reproducible
- Drawback: many variants, subject to various limitations and of not easy comparison

Macroseismic Intensity

Macroseismic intensity concept was introduced by **Robert Mallet** by studying the great earthquake occurred in Southern Italy in 1857.

He related the intensity of the earthquake to the human perceptions of the felt ground motion and the observed distribution of damage on buildings and territory.

In this way, the maximum (observed) intensity I_0 , often called **epicentral intensity**, gives an rough estimate of the size of the earthquake.



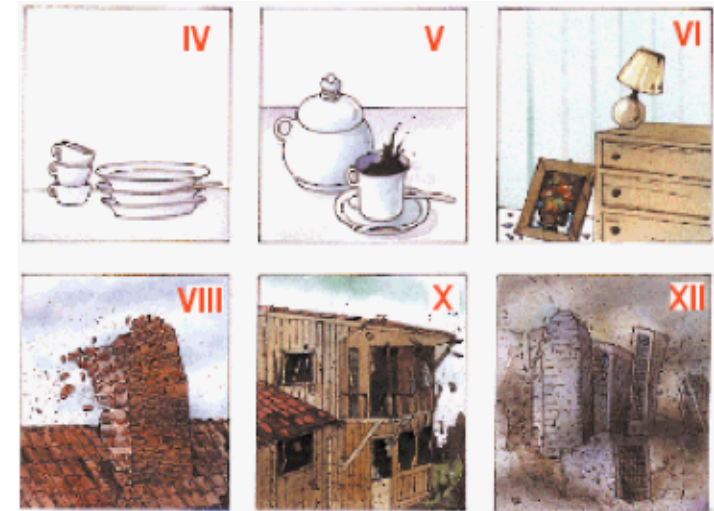
Macroseismic Scales

1. **Mercalli – Cancani – Seiberg (MCS)**: 12 – level scale used in southern Europe;
2. **Modified Mercalli (MM)**: 12 – level scale proposed in 1931 by Wood and Neumann, who adapted the MCS scale to the California data set. It is used in North America and several other countries;
3. **Medvedev – Sponheuer – Karnik (MSK)**: 12 – level scale developed in Central and Eastern Europe and used in several other countries;
4. **European Macroseismic Scale (EMS)**: 12 – level scale adopted since 1998 in Europe. It is a development of the MM scale;
5. **Japanese Meteorological Agency (JMA)**: 7 – level scale used in Japan. It has been revised over the years and has recently been correlated to maximum horizontal acceleration of the ground.

Mercalli Scale

TABLE 13-1 Modified Mercalli Intensity Scale

| Intensity Level | Description |
|-----------------|---|
| I | Not felt. |
| II | Felt only by a few people at rest. Suspended objects may swing. |
| III | Felt noticeably indoors. Many people do not recognize it as an earthquake. Parked cars may rock slightly. |
| IV | Felt indoors by many, outdoors by few. Dishes, windows, doors rattle. Parked cars rock noticeably. |
| V | Felt by most; many awakened. Some dishes, windows broken. Unstable objects overturned. |
| VI | Felt by all. Some heavy furniture moves. Damage slight. |
| VII | Slight to moderate damage in well-built structures; considerable damage in poorly built structures; some chimneys broken. |
| VIII | Considerable damage in well-built structures. Damage great in poorly built structures. Fall of chimneys, factory stacks, columns, monuments, walls. |
| IX | Damage great in well-built structures, with partial collapse. Buildings shifted off foundations. |
| X | Some well-built wooden structures destroyed; most masonry and frame structures destroyed. Rails bent. |
| XI | Few if any masonry structures remain standing. Bridges destroyed. Rails bent greatly. |
| XII | Damage total. Lines of sight and level are distorted. Objects thrown into the air. |



Giuseppe Mercalli



Subjective damage evaluation because of its qualitative nature, related to population density, familiarity with earthquake and type of constructions.

Improvements of the EMS98





Scaling to building category and vulnerability type



| | | VULNERABILITY CLASS | | | | | |
|--------------------------|---|---------------------|---|---|---|---|---|
| | | A | B | C | D | E | F |
| MASONRY | RUBBLE STONE, FIELDSTONE | ○ | | | | | |
| | ADOBE (EARTH BRICK) | ○ | ├ | | | | |
| | SIMPLE STONE | ├ | ○ | | | | |
| | MASSIVE STONE | | | ├ | ○ | ├ | |
| | UNREINFORCED, WITH MANUFACTURED STONE UNITS | ├ | ○ | ├ | | | |
| | UNREINFORCED, WITH RC FLOORS | | | ├ | ○ | ├ | |
| | REINFORCED OR CONFINED | | | | ├ | ○ | ├ |
| REINFORCED CONCRETE (RC) | FRAME WITHOUT EARTHQUAKE-RESISTANT DESIGN (ERD) | ├ | ├ | ○ | ├ | | |
| | FRAME WITH MODERATE LEVEL OF ERD | | ├ | ├ | ○ | ├ | |
| | FRAME WITH HIGH LEVEL OF ERD | | | ├ | ├ | ○ | ├ |
| | WALLS WITHOUT ERD | ├ | ○ | | | | |
| | WALLS WITH MODERATE LEVEL OF ERD | | | ├ | ○ | ├ | |
| | WALLS WITH HIGH LEVEL OF ERD | | | ├ | ○ | ├ | |
| STEEL STRUCTURES | | | | ├ | ├ | ○ | ├ |
| | TIMBER STRUCTURES | | | ├ | ├ | ○ | ├ |
| | | | | | | | |

| DS1 | DS2 | DS3 | DS4 | DS5 |
|---|--|---|---|--|
| | | | | |
| Grade 1: Negligible to slight damage <i>(no structural damage, slight non-structural damage)</i> | Grade 2: Moderate damage <i>(slight structural damage, moderate non-structural damage)</i> | Grade 3: Substantial to heavy damage <i>(moderate structural damage, heavy non-structural damage)</i> | Grade 4: Very heavy damage <i>(heavy structural damage, very heavy non-structural damage)</i> | Grade 5: Destruction <i>(very heavy structural damage)</i> |
| Fine cracks in plaster over <u>frame members</u> or in walls at the base. <u>Fine cracks in partitions and infills</u> | Cracks in columns and <u>beams of frames</u> and in structural walls. <u>Cracks in partition and infill walls</u> ; fall of brittle cladding and plaster. Falling mortar from the joints of wall panels | Cracks in columns and beam column joints of frames at the base and at joints of coupled walls. <u>Spalling of concrete cover, buckling of reinforced rods.</u> <u>Large cracks in partition and infill walls, failure of individual infill panels</u> | <u>Large cracks in structural elements</u> with compression failure of concrete and fracture of rebars; bond failure of beam reinforced bars; tilting of columns. Collapse of a few columns or of a single upper floor | Collapse of ground floor or parts (e. g. wings) of buildings |
| $\min(\Delta_{cr}^{inf}; \Delta_{cr}^{RC})$ | $\min(\Delta_{max}^{inf}; \Delta_y^{RC})$ | $\min\left(\begin{matrix} \Delta_{ult}^{inf}; \Delta_{spalling}^{RC} \\ \Delta_{buckling}^{RC} \end{matrix}\right)$ | Δ_{ult}^{RC} | Δ_{coll}^{RC} |

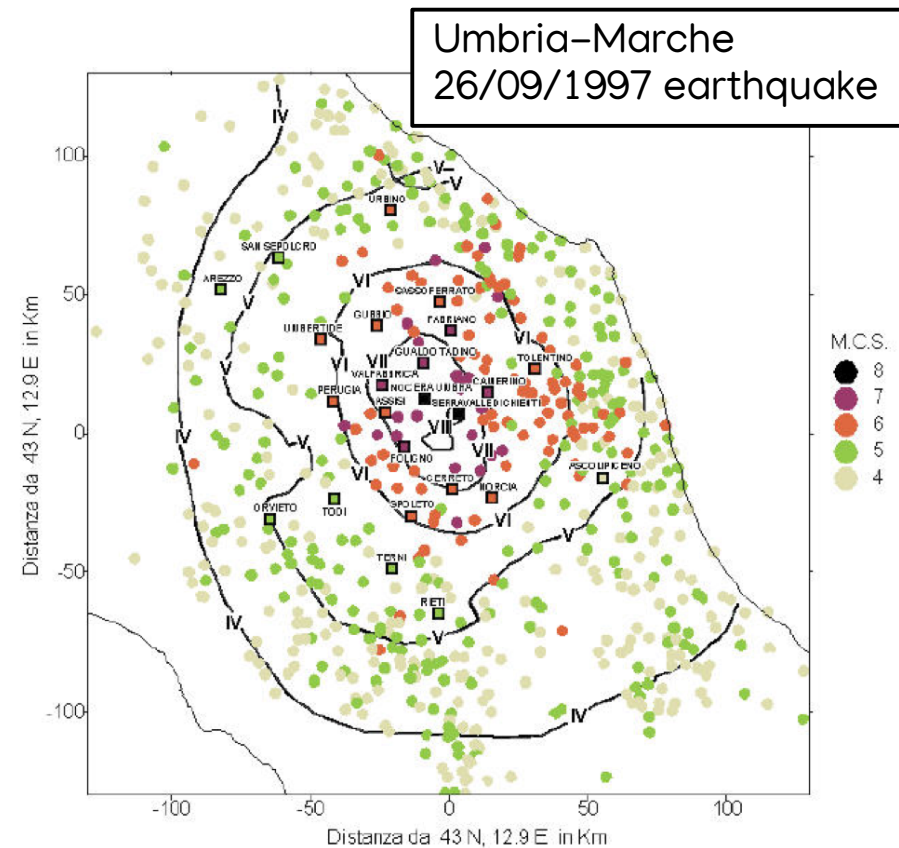
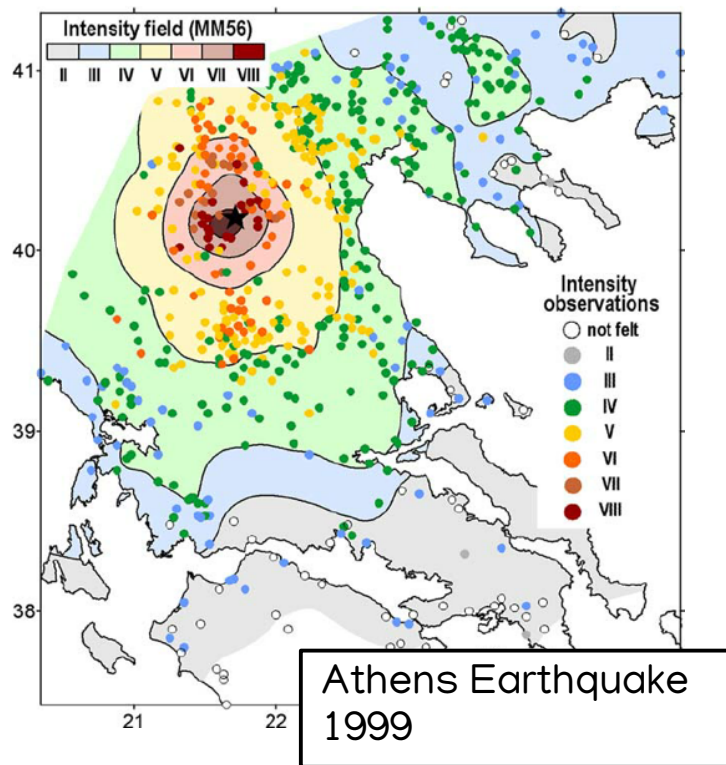
Head to Head Scales

| Modified Mercalli Scale | | Richter Magnitude Scale | JMA | MERCALLI CANCELI SIEBERG | MEDVEDEV SPONHEUER KARNIK | EMS-98 Intensity | Felt | Impact | Magnitude (Approximate Value) | Building Damage (Masonry) |
|-------------------------|--|-------------------------|-----|--------------------------|---------------------------|------------------|-------------|--|-------------------------------|---|
| I | Detected only by sensitive instruments | 1.5 | | II | I | I | Not felt | Not felt | 2 | |
| II | Felt by few persons at rest, especially on upper floors; delicately suspended objects may swing | 2 | I | III | II | II-III | Weak | Felt indoors by a few people. People at rest feel a swaying or light trembling. | 3 | |
| III | Felt noticeably indoors, but not always recognized as earthquake; standing autos rock slightly, vibration like passing truck | 2.5 | | IV | III | IV | Light | Felt indoors by many people, outdoors by very few. A few people are awakened. Windows, doors and dishes rattle. | | |
| IV | Felt indoors by many, outdoors by few, at night some may awaken; dishes, windows, doors disturbed; autos rock noticeably | 3 | II | V | IV | V | Moderate | Felt indoors by most, outdoors by few. Many sleeping people wake up. A few are frightened. Buildings tremble throughout. Hanging objects swing considerably. Small objects are shifted. Doors and windows swing open or shut. | 4 |  |
| V | Felt by most people; some breakage of dishes, windows, and plaster; disturbance of tall objects | 3.5 | III | VI | V | VI | Strong | Many people are frightened and run outdoors. Some objects fall. Many houses suffer slight non-structural damage like hair-line cracks and falling of small pieces of plaster. | | |
| VI | Felt by all, many frightened and run outdoors; falling plaster and chimneys, damage small | 4 | IV | VII | VI | VII | Very strong | Most people are frightened and run outdoors. Furniture is shifted and objects fall from shelves in large numbers. Many well-built ordinary buildings suffer moderate damage: small cracks in walls, fall of plaster, parts of chimneys fall down; older buildings may show large cracks in walls and failure of in-fill walls. | 5 |  |
| VII | Everybody runs outdoors; damage to buildings varies depending on quality of construction; noticed by drivers of autos | 4.5 | V | VIII | VII | VIII | Severe | Many people find it difficult to stand. Many houses have large cracks in walls. A few well built ordinary buildings show serious failure of walls, while weak older structures may collapse. | 6 |  |
| VIII | Panel walls thrown out of frames; fall of walls, monuments, chimneys; sand and mud ejected; drivers of autos disturbed | 5 | | IX | VIII | IX | Violent | General panic. Many weak constructions collapse. Even well built ordinary buildings show very heavy damage: serious failure of walls and partial structural failure. | | |
| IX | Buildings shifted off foundations, cracked, thrown out of plumb; ground cracked; underground pipes broken | 5.5 | | X | IX | X | Extreme | Most ordinary well built buildings collapse, even some with good earthquake resistant design are destroyed. | 7 |  |
| X | Most masonry and frame structures destroyed; ground cracked, rails bent, landslides | 6 | VI | XI | X | X+ | | | | |
| XI | Few structures remain standing; bridges destroyed, fissures in ground, pipes broken, landslides, rails bent | 6.5 | | XII | XI | | | | | |
| XII | Damage total; waves seen on ground surface, lines of sight and level distorted, objects thrown up in air | 7 | VII | | XII | | | | | |
| | | 7.5 | | | | | | | | |
| | | 8 | | | | | | | | |

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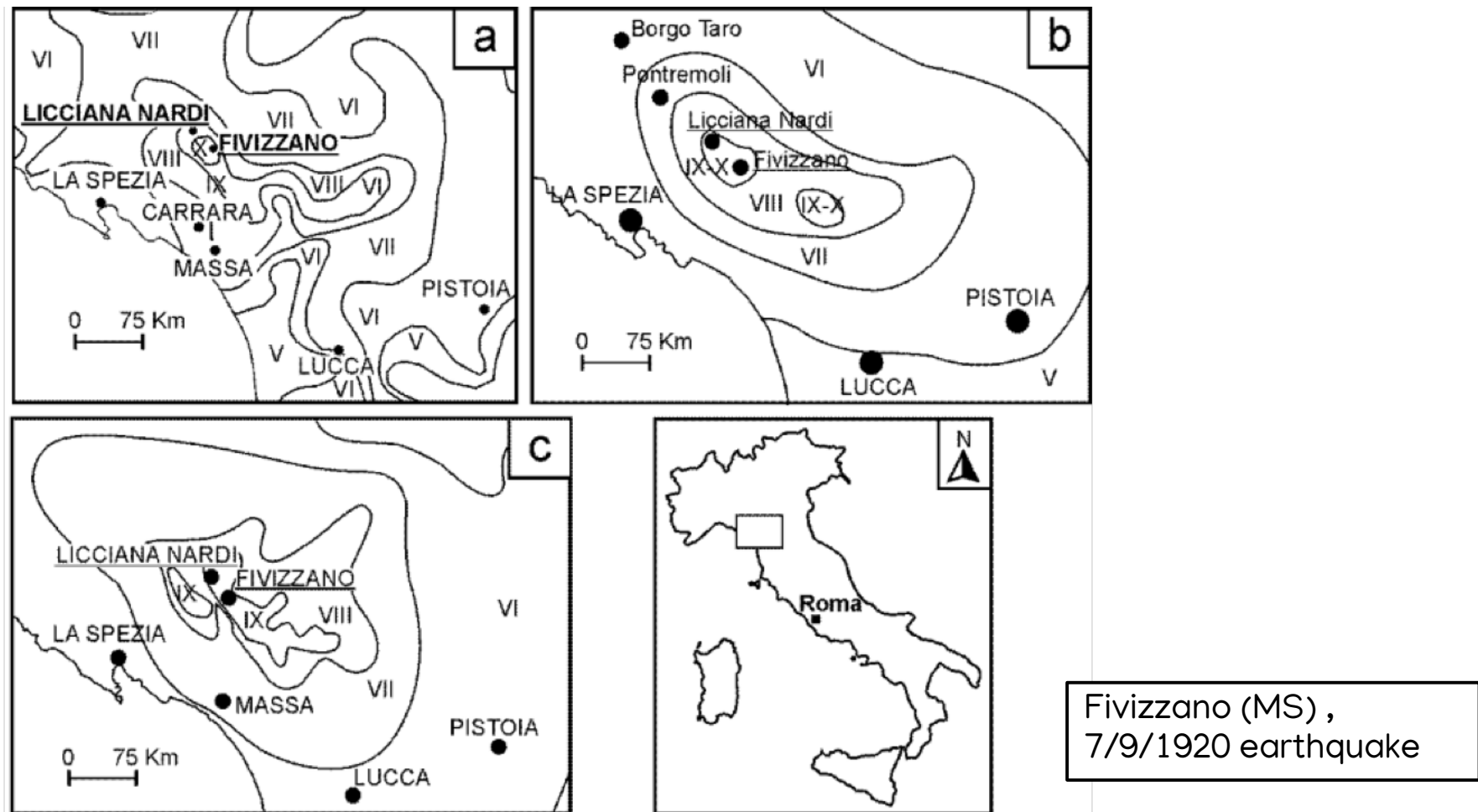
Isoseismals & Contour Maps

By tracing lines on maps joining the points in which the intensity was similar (isolines, isoseismals, isointensity line), it is possible to determine the centre on the shaking (called macroseismic centre), which is characterized by the highest damage and corresponds to a small area.



Uncertainty and Subjectivity

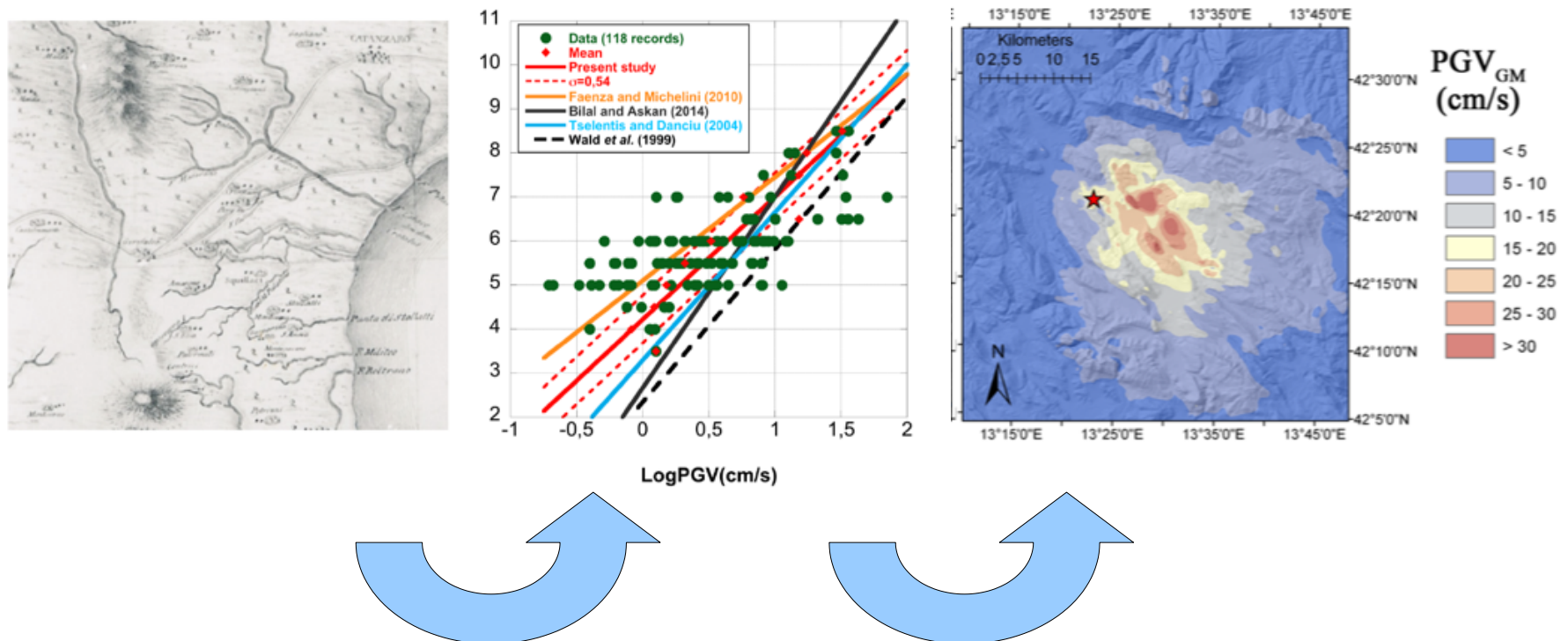
Tracing of isoseismals is highly subjective. Given the same damage description, intensity maps from different analysts can be very different.



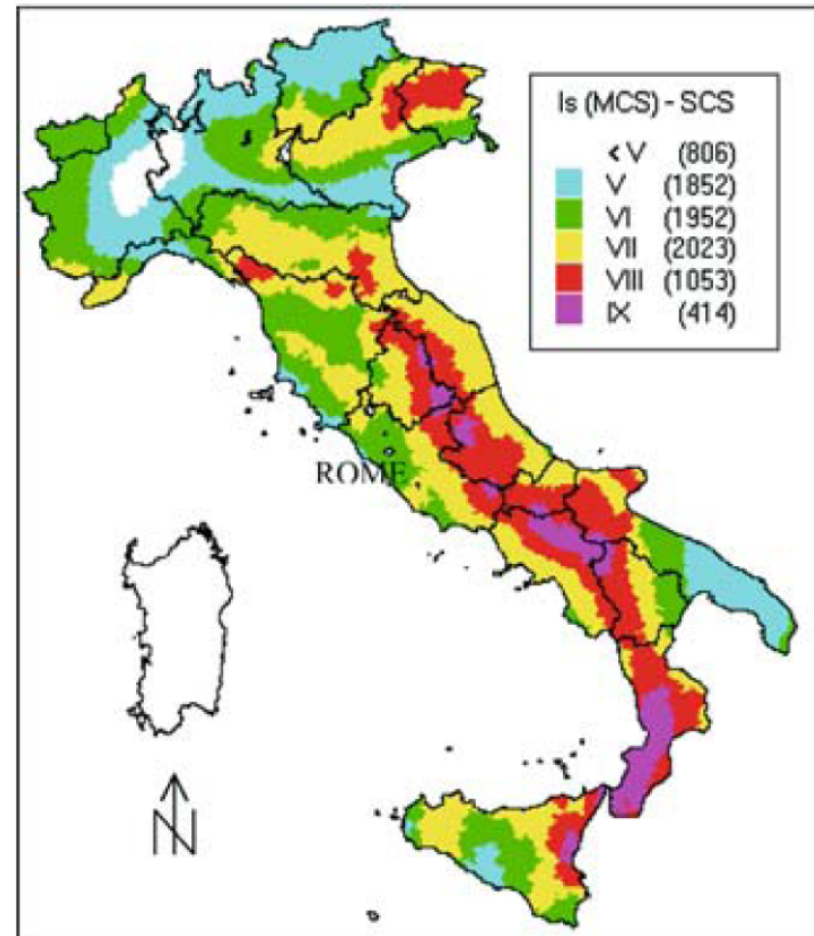
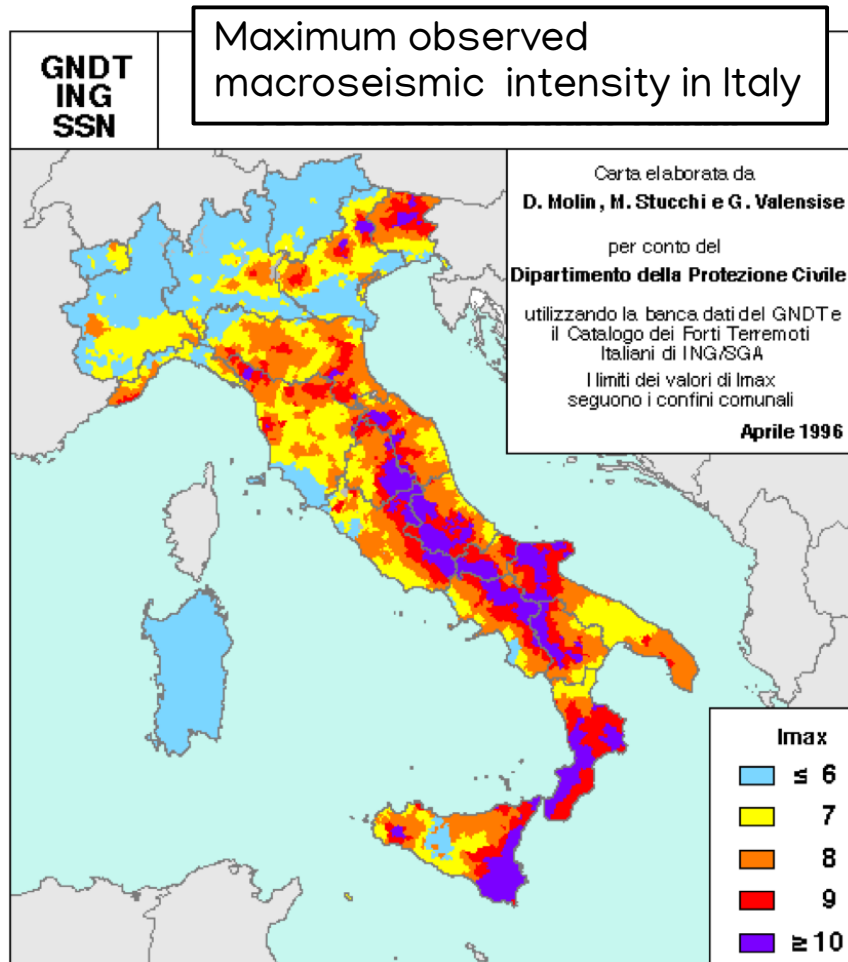
Historical Earthquakes

Links past with the future: Intensity - ground motion relationships are essential for the use of historical earthquakes for which no instrumental records exist.

These relations must be calibrated on present day recordings.



Examples in Italy



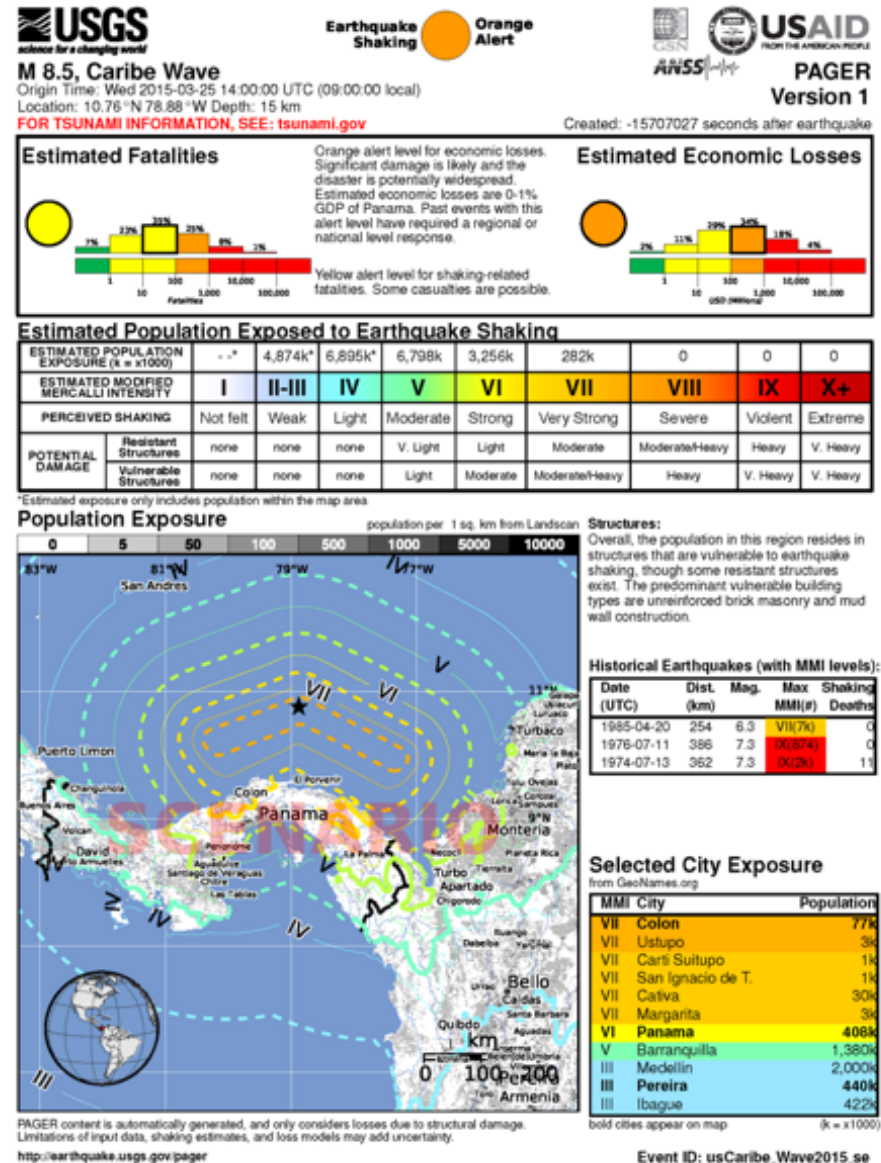
Probabilistic hazard map in
MCS intensity (10% in 50 years)

Intensity in ShakeMaps

ShakeMap®, developed by the U.S. Geological Survey (USGS), portrays the distribution and severity of shaking.

Using macroseismic intensity facilitates communication of earthquake information beyond just magnitude and location for emergency management and response.

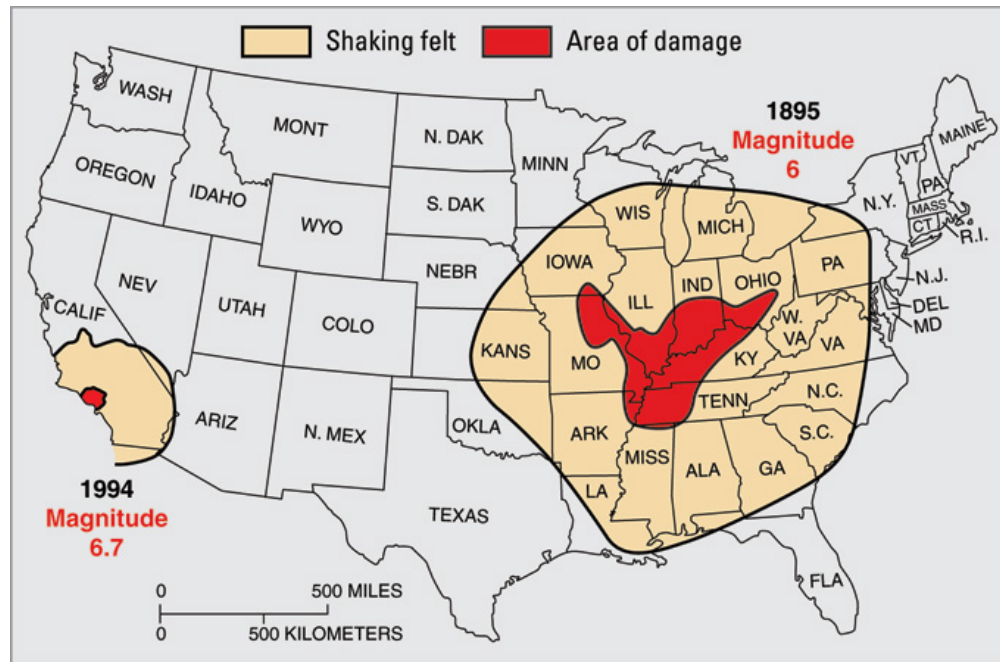
NOTE: Not a representation of actual damage distribution!



Limitations

The maximum intensity measure is biased by many factors not always directly dependent to the earthquake:

- Depth of the event
- Distribution of the population and personal perception
- Construction practice
- Effect of local geology (seismic site effects)
- Regional geology (path attenuation)



This makes earthquakes from different regions hardly comparable.

Local Magnitude

The concept of magnitude was introduced by Richter (1935) to provide an objective instrumental measure of the size of the earthquake.

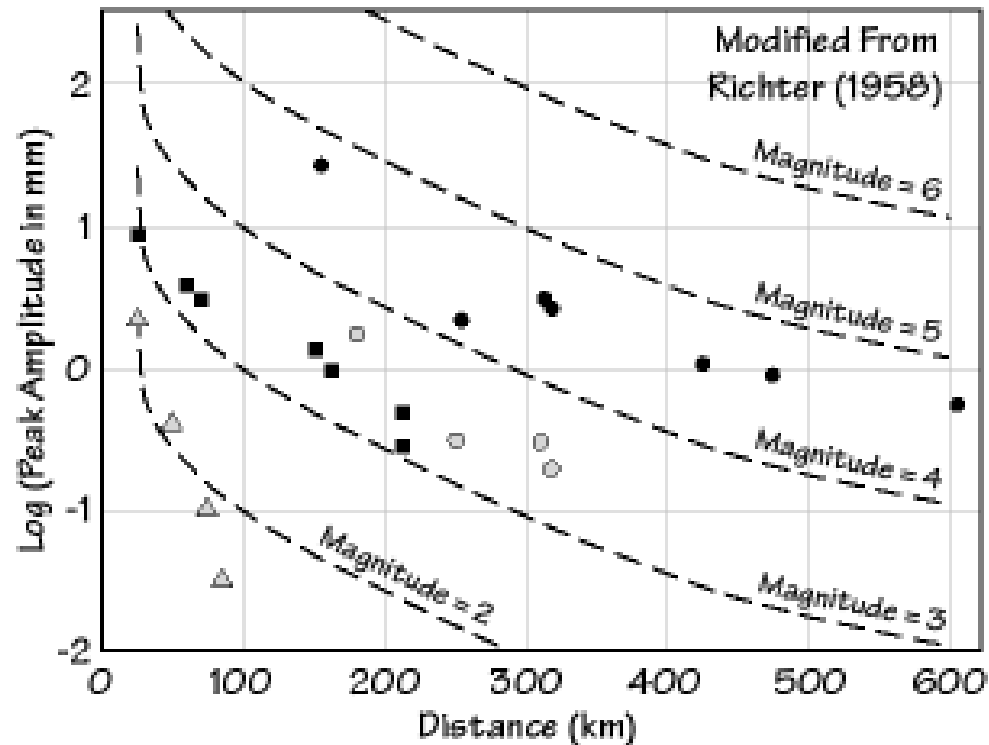
Contrary to seismic intensity, the magnitude (M) uses instrumental measurements of the earth ground motion adjusted to **epicentral distance** and **source depth**.

Such magnitude estimate is called **local** (M_L) or simply Richter, from its inventor.



Local Magnitude

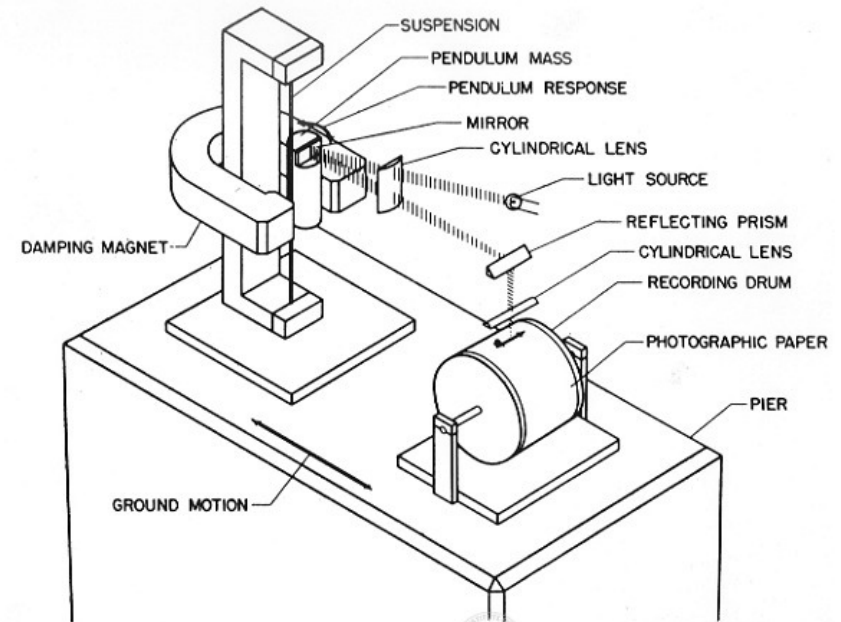
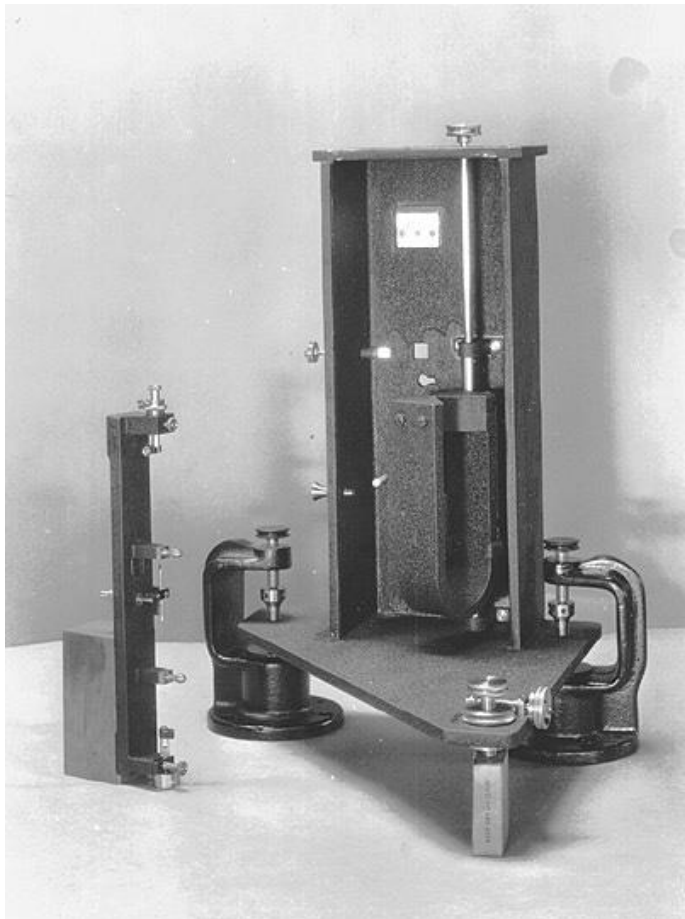
The original Richter scale was based on the observation that the (log) amplitude of seismic waves decreases with epicentral distance.



A magnitude 0 earthquake is defined as the size event that generates a maximum ground motion of 1 micrometer at epicentral distance of 100 km with a **Wood-Anderson instrument**.

Wood-Anderson Seismograph

The ML magnitude scale is based on the use of the Wood-Anderson seismograph, which is a torsion horizontal seismometer with period of about 0.8 seconds.



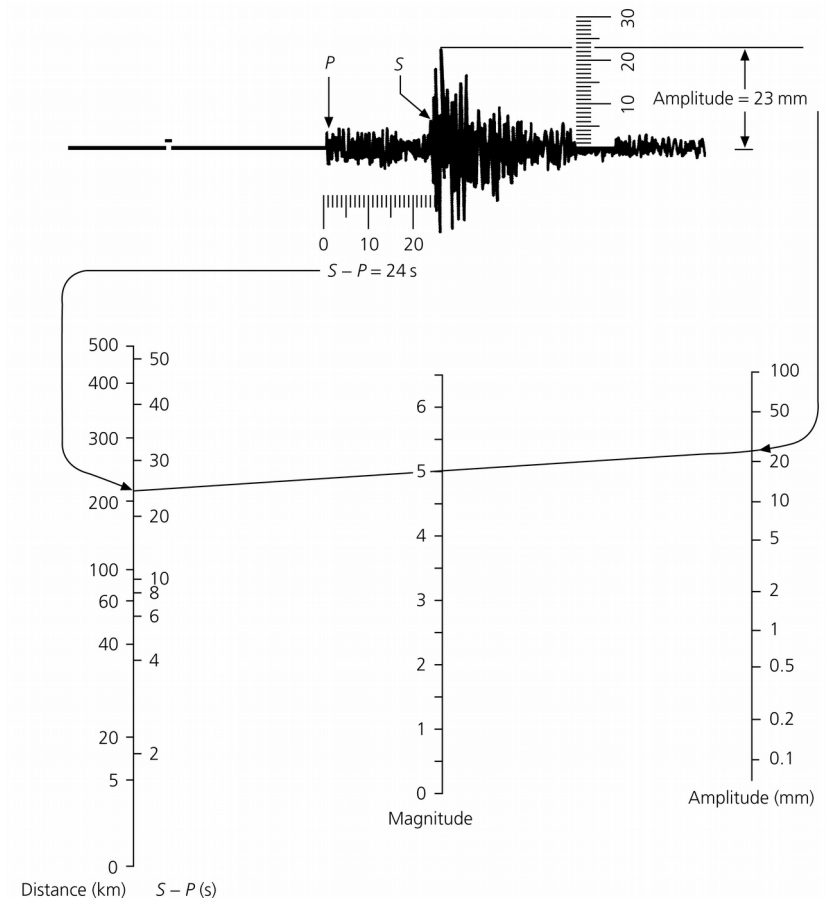
Magnitude Calculation

A for the original formulation, M_L can be computed with respect to a reference amplitude, which depends on distance to the event:

$$M_L = \log_{10}(A) - \log_{10}(A_{ref})$$

Several empirical formulations exist as function of epicentral or hypocentral distance, e.g. the Lillie formulation:

$$M_L = \log_{10}(A) - 2.48 + 2.76 \log_{10}(\Delta)$$

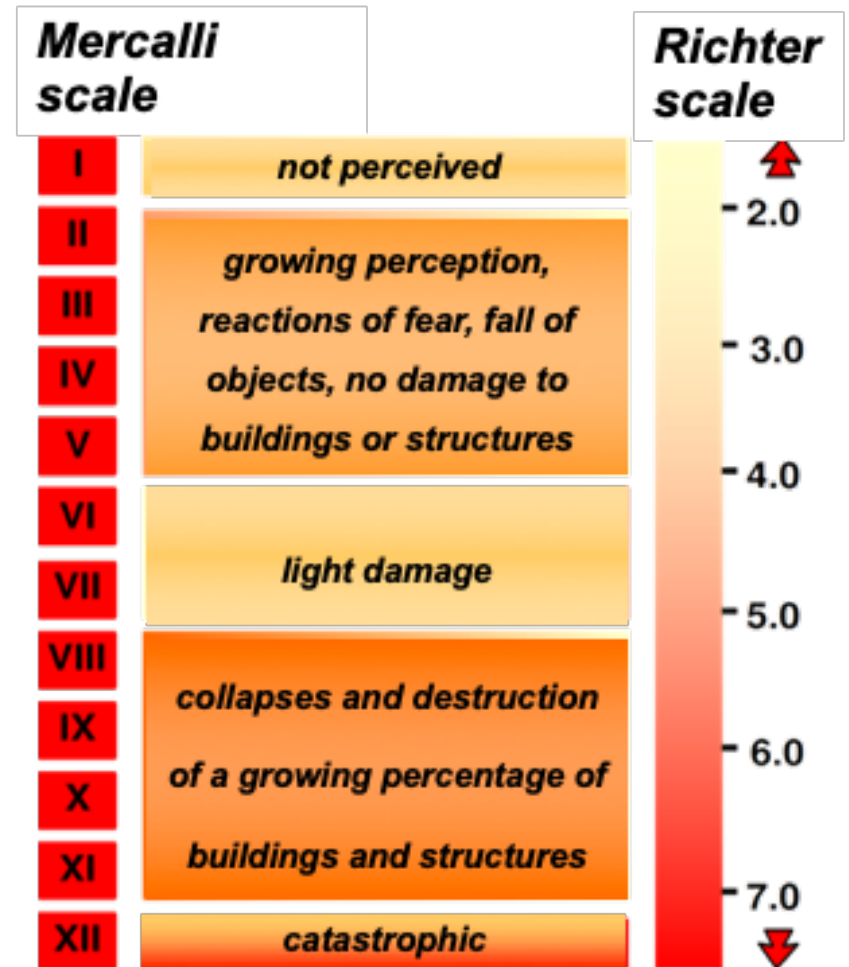


M_L vs Mercalli Intensity

Approximate relations between epicentral Mercalli intensity and Richter magnitude scale exist (e.g. Gutenberg and Richter, 1956):

$$M_L = \frac{2}{3} I + 1$$

This is useful to homogeneously quantify the size of historical earthquakes, but with **large uncertainty**.

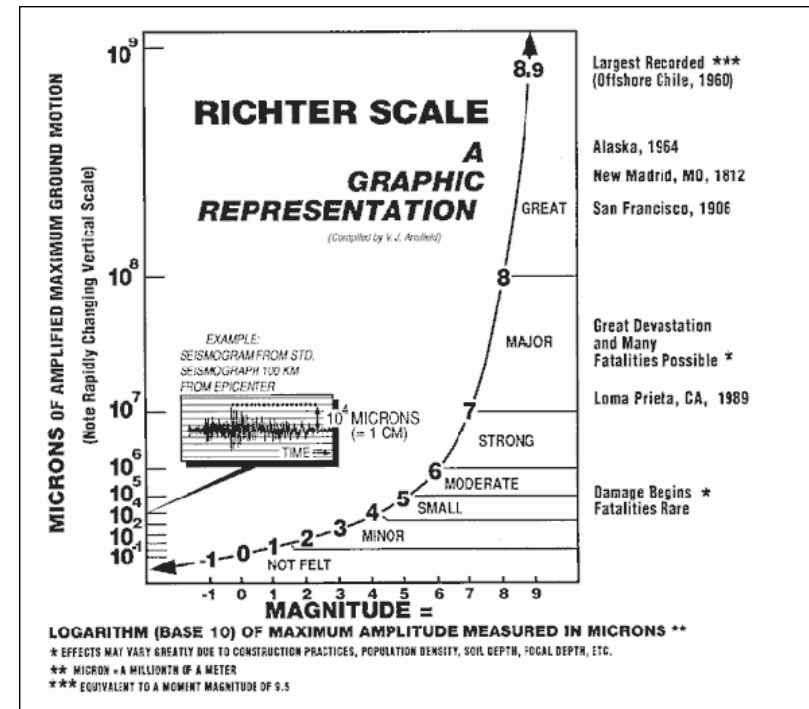


Problems with M_L

Richter Magnitude suffers from many limitations, such as:

- It is strictly valid only for Southern California (in original form) and adjustments are needed for other regions
- Depends on a specific type of seismometer, whose dominant periods limits the capability of the scale to resolve large magnitudes (the saturation problem)

| Magnitude | Description | How it feels | Frequency |
|---------------|-------------|--|-------------------------------|
| Less than 2.0 | Micro | Not felt by people. | Millions per year. |
| 2.0 to 2.9 | Minor | No building damages. | More than 1 million per year. |
| 3.0 to 3.9 | Minor | Often felt, may shake objects inside buildings. | More than 100,000 per year. |
| 4.0 to 4.9 | Light | Indoor objects shake or fell to the floor. Not significant damage. | 10,000 to 15,000 per year. |
| 5.0 to 5.9 | Moderate | Extensive damage to buildings not designed correctly. | 1,000 to 1,500 per year. |
| 6.0 to 6.9 | Strong | Can cause damage up to | 100 to 1500 per |



Other Magnitude Scales

After local magnitude, the concept has been developed and extended so as to be applicable to a variety of wave types and distances.

In general form, all magnitude scales based on amplitude measurements are like:

$$M = \log(A/T) + f(\Delta, h) + C_s + C_r$$

M = Magnitude

A = Amplitude

T = Period

f = Correction for distance and depth

C_s = Correction for site

C_r = Correction for source region

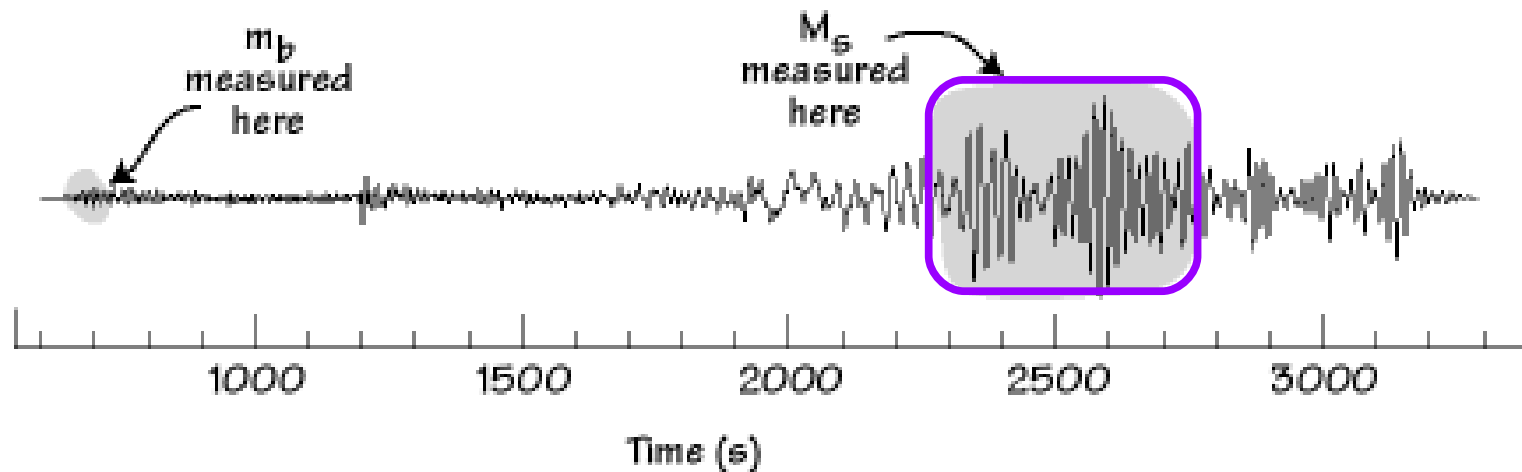
Surface Wave Magnitude

For distances $20^\circ < \Delta < 160^\circ$ with hypocentres in the uppermost 50 km

Measured by the amplitude of the Rayleigh waves

Dominant period of around **20 seconds**.

$$M_S = \log_{10} (A/T)_{max} + 1.66 \log_{10} \Delta + 3.3$$



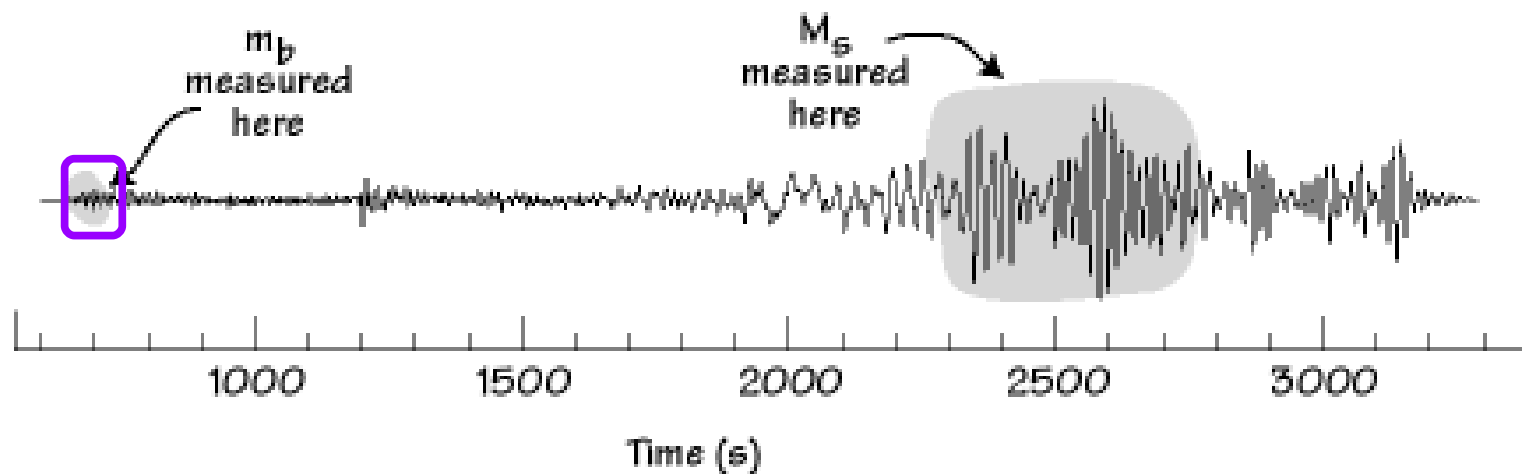
Body Wave Magnitude

Used for deep earthquakes and earthquakes measured at distances > 600 km (**teleaseismic events**)

Measured by the amplitudes of the first arrivals of P-waves

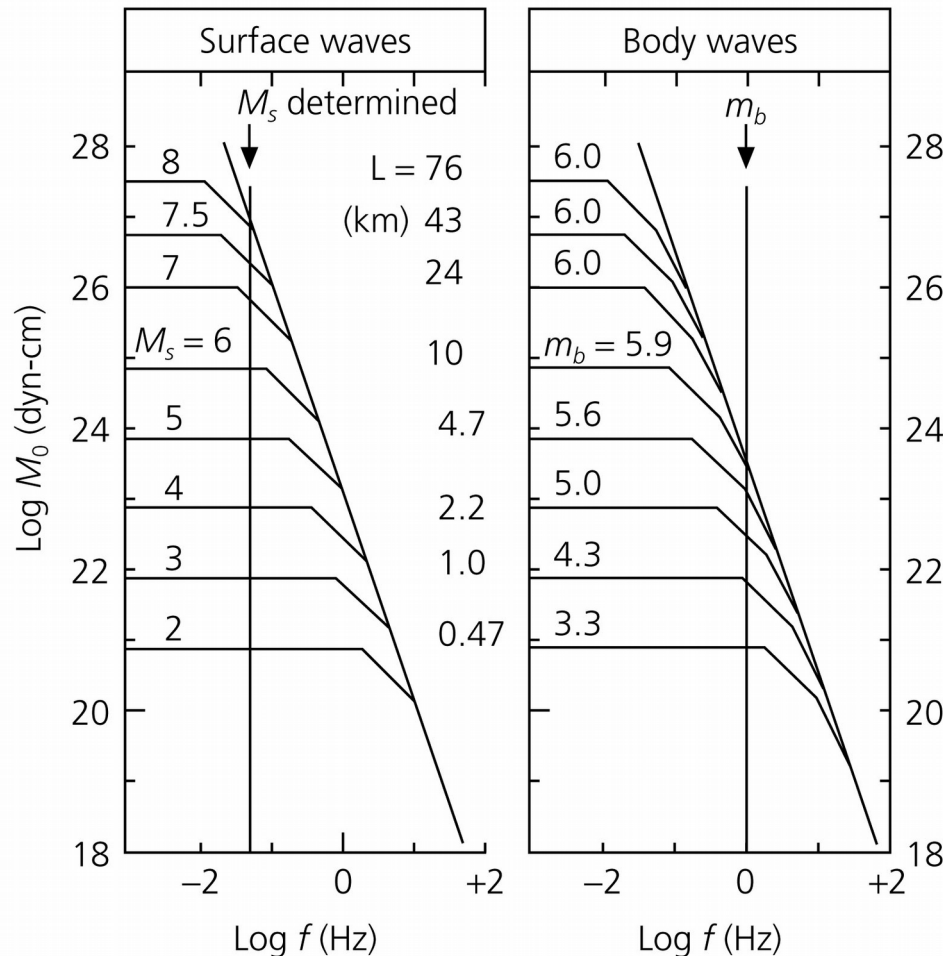
Dominant period of around **1 second**

$$m_b = \log_{10} \left(\frac{A}{T} \right)_{max} + g(\Delta, h)$$



Magnitude Saturation

The frequency (or period) at which the earthquake spectrum is “sampled” strongly controls the resolving power of a specific magnitude type.



For instance, m_b saturates above 6, while M_s never gets above 8.2–8.3

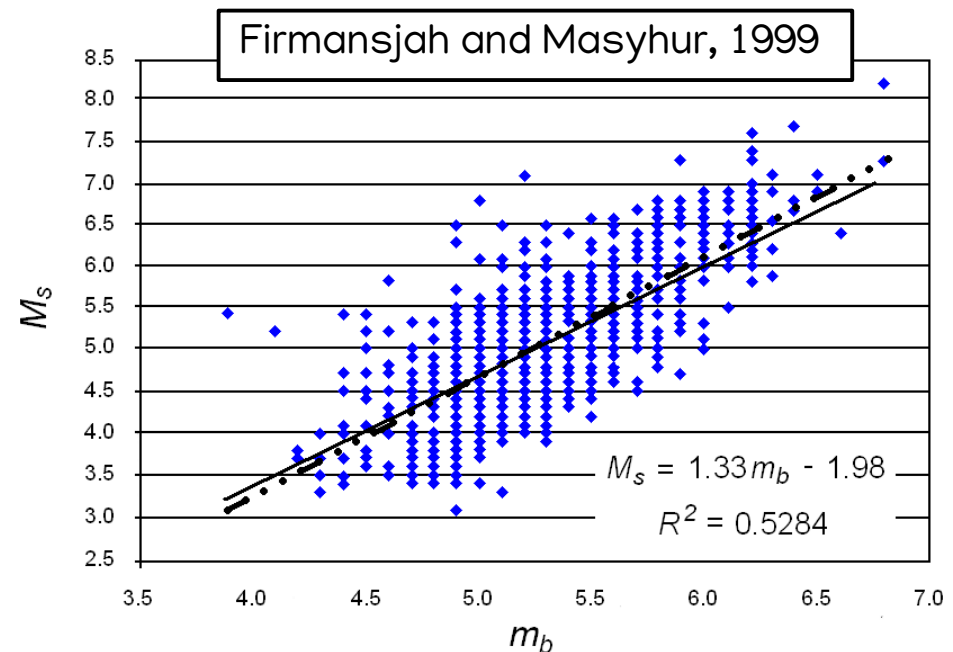
Conversion Relations

As earthquake is a complex phenomenon, different magnitude scale might provide inconsistent estimates for the same event.

Example:

- Turkey 8/17/1999: $M_s = 7.8$, $m_b = 6.3$
- Taiwan 9/20/1999: $M_s = 7.7$, $m_b = 6.6$

Magnitude conversion relations are often necessary (e.g. in hazard analysis). Although global relations exists (e.g. Di Giacomo, Weatherill), relations calibrated ad-hoc for specific region are to be preferred.



Are ML, mb and Ms useful?

These scales are still routinely used nowadays, first of all for their simplicity, but also because, being sensitive to different characteristics of the earthquake (different waves, different periods), they bring useful information in specific analysis (e.g. nuclear test verification)

| Event | Date | Time | Err | RMS | Latitude | Longitude | Smax | Smin | Az | Depth | Err | Ndef | Nsta | Gap | mdist | Mdist | Qual | Author |
|---------|------------|-------------|-------|-------|----------|-----------|------|-------|-----|-------|------|------|------|-----|-------|--------|------|--------|
| 1737346 | 2000/07/05 | 17:12:09.70 | 1.42 | | 34.9080 | 21.6260 | 27.3 | 10.5 | 165 | 33.0 | | 14 | | | | | | MOS |
| | 2000/07/05 | 17:12:20.20 | 1.100 | | 36.1300 | 21.4000 | | | | 69.0 | | | 15 | | | | | BJI |
| | 2000/07/05 | 17:12:20.50 | 1.100 | | 36.0200 | 21.9800 | 8.2 | 7.9 | -1 | 5.0 | | 17 | 224 | | | | | ATH |
| | 2000/07/05 | 17:12:21.92 | 1.23 | 0.990 | 36.0450 | 22.1210 | 10.4 | 8.3 | 213 | 49.9 | 10.6 | 33 | 33 | 86 | 5.16 | 120.64 | se | NEIC |
| | 2000/07/05 | 17:12:22.14 | | | 35.9440 | 21.7350 | | | | 10.0 | | | | | | | | THE |
| | 2000/07/05 | 17:12:23.62 | 1.240 | | 36.0200 | 22.0720 | 10.2 | 5.9 | 23 | 48.5 | 6.7 | 127 | 124 | | | | ke | EHB |
| | 2000/07/05 | 17:12:25.16 | 0.07 | | 36.4360 | 21.5310 | 66.7 | 19.0 | -1 | 9.8 | 11.1 | | 9 | 350 | | | | PDG |
| | 2000/07/05 | 17:12:26.22 | 3.30 | 0.790 | 36.1298 | 22.0459 | 19.6 | 16.6 | 64 | 67.9 | 29.9 | 18 | 17 | 101 | 9.24 | 120.71 | uk | IDC |
| | 2000/07/05 | 17:12:45 | | | 40.0000 | 27.0000 | | | | | | | | | | | | NAO |
| | 2000/07/05 | 17:12:19.80 | 0.36 | 1.470 | 35.9480 | 21.9990 | 4.2 | 3.145 | 0 | 33.0f | | 125 | 127 | 68 | 0.90 | 120.72 | m i | ISC |

| Magnitude | Err | Nsta | Author | OrigID | |
|-----------|-----|------|--------|---------|---------|
| mb | 4.7 | 4 | MOS | 3025203 | |
| mb | 4.5 | | BJI | 3019870 | |
| MD | 4.1 | 14 | ATH | 3970846 | |
| ML | 4.2 | | ATH | 3970846 | |
| mb | 3.9 | 12 | NEIC | 3665165 | |
| ML | 3.9 | | THE | 3816063 | |
| mb | 3.8 | 0.1 | 14 | IDC | 3882300 |
| ML | 3.5 | 0.1 | 2 | IDC | 3882300 |
| MS | 3.4 | 0.1 | 8 | IDC | 3882300 |
| Mb | 3.7 | | NAO | 3608388 | |
| mb | 4.3 | 23 | ISC | 4127018 | |
| MS | 3.1 | 4 | ISC | 4127018 | |

The ISC Reviewed Bulletin

Energy Magnitude Relation

MS and mb magnitudes represents different parts of the frequency spectrum of seismic waves, therefore different physical parameters of an earthquake. Gutenberg and Richter's studies suggests that, being related, they can be used to represent the fundamental physical parameter of seismic waves: **ENERGY**.

They obtain the following relationship:

$$\log E = 1.5 M_s + 11.8$$



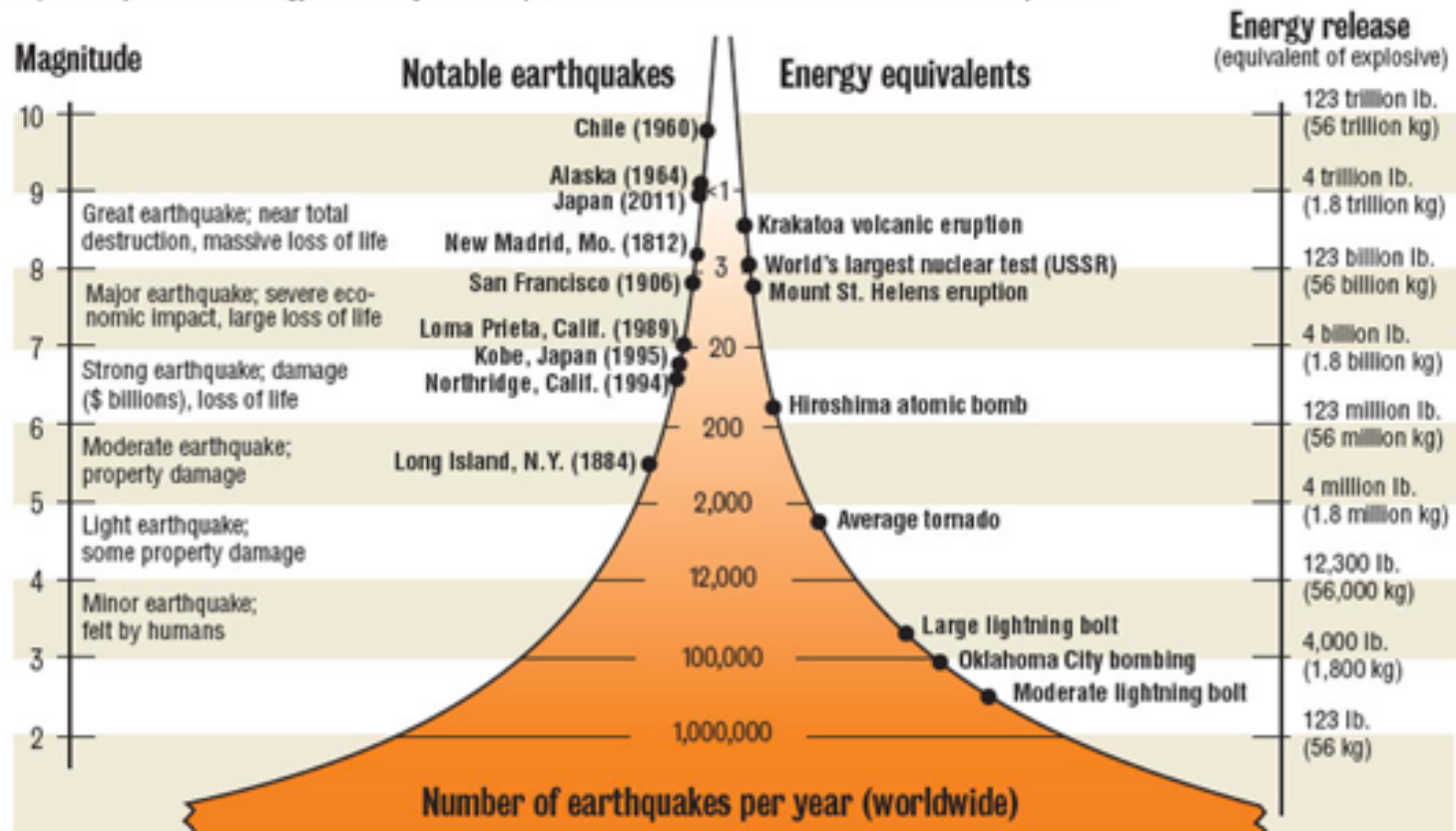
This is a rapid estimate of the energy of seismic waves associated with an earthquake.

Energy Equivalents

Note that an increase of one magnitude unit corresponds to about 32 times increase in the amount of energy released

Earthquake frequency and destructive power

The left side of the chart shows the magnitude of the earthquake and the right side represents the amount of high explosive required to produce the energy released by the earthquake. The middle of the chart shows the relative frequencies.



Source: U.S. Geological Survey

MCT

Seismic Moment Recap

From elastic dislocation theory (Aki 1962) we recall the concept of scalar seismic moment:

$$M_0 = \mu A D$$

Seismic moment is one of the most reliable seismological parameters that represents the 'size' of an earthquake.

M_0 does not saturate, it is therefore a more suitable parameter to represent the size of great earthquakes than the conventional magnitude scales such as M_s .

Moment Magnitude

Moment magnitude (M_w) was first introduced by Hiro Kanamori in 1977 as:

$$M_w = \frac{2}{3} \log(M_0) - 10.7$$



M_w measures the size of events in terms of seismic moment, and therefore of how much energy is released.

M_w can be easily compared to magnitude values for other events.

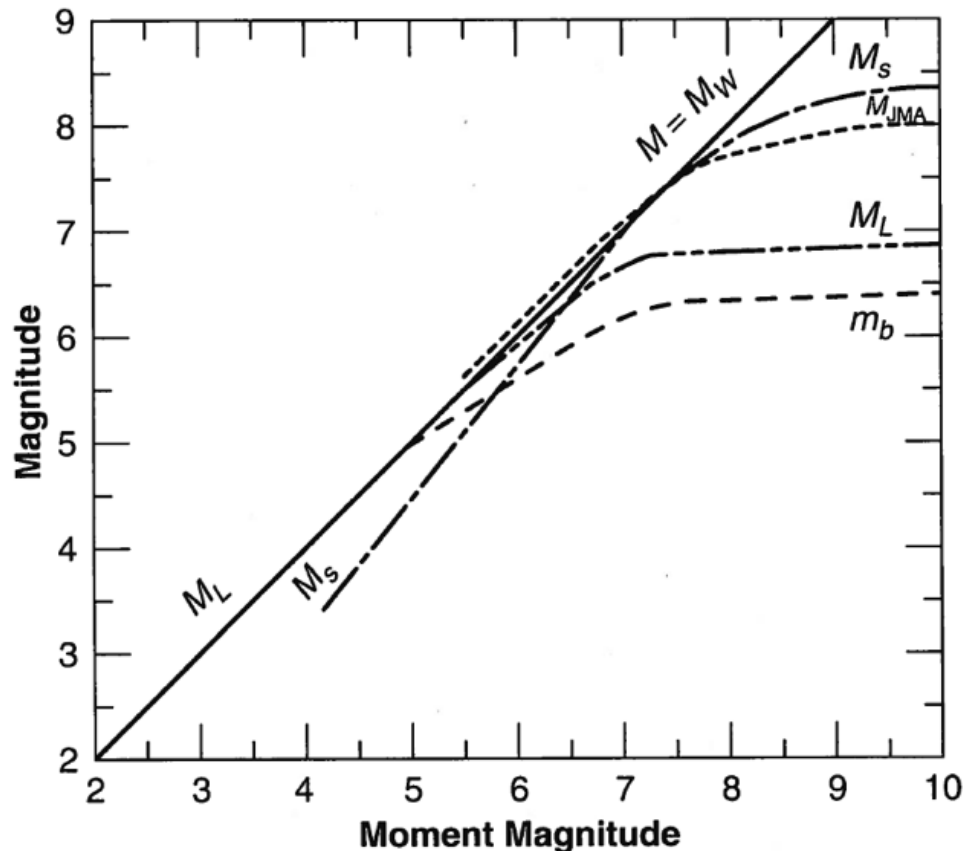
Comparing Scales to Mw

| Scale type | Author | Earthquake size | Earthquake depth | Epicentre distance (km) | Reference parameter | Applicability | Saturation |
|------------|------------------------------|-----------------|------------------|-------------------------|---------------------------|-----------------------|------------|
| M_L | Richter (1935) | Small | Shallow | <600 | Wave amplitude | Regional (California) | ✓ |
| m_b | Gutenberg and Richter (1956) | Small-to-medium | Deep | >1,000 | Wave amplitude (P-waves) | Worldwide | ✓ |
| M_S | Richter and Gutenberg (1936) | Large | Shallow | >2,000 | Wave amplitude (LR-waves) | Worldwide | ✓ |
| M_w | Kanamori (1977) | All | All | All | Seismic moment | Worldwide | n.a. |

Key: n.a. = not applicable; ✓ = saturation occurs.

Comparing Scales to Mw

Moment magnitude does not saturate because it is derived from seismic moment as opposed to an amplitude on a seismogram.



- The local magnitude M_L and the short-period body wave magnitude m_b are essentially equal to moment magnitude up to $M = 6$.
- The surface wave magnitude M_s is essentially equal to moment magnitude in the range of $M = 6$ to 8.

Measuring Mw

M_0 is proportional to the far-field earthquake spectrum at long periods. M_w can then be obtained by spectral fitting.

