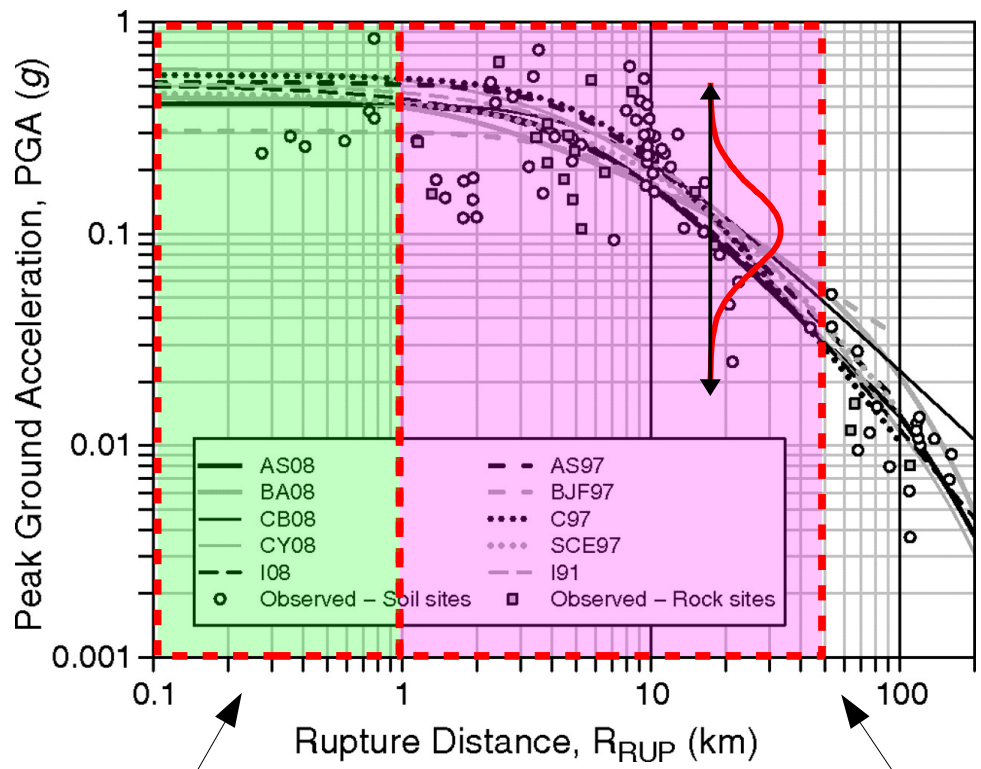


GMPE site term and Soil Proxies

GMPE - Ground Motion Prediction Equations

Given a specific source scenario (e.g. magnitude, fault mechanism...), GMPEs predict the shaking level at a given location (e.g. at distance R)

$$\boxed{\text{GM Amplitude}} = \boxed{\text{Source term}} * \boxed{\text{Path term}} * \boxed{\text{Site term}}$$



Lack of data in near field...

Important distances < 50Km

Often source, path and site terms are described by a simple **regressive model** (e.g. high order polynomials) using a merely empirical approach and **single predictors** (PGA, PGV, Intensity)

PRO: generally quite easy to use, often calibrated on world-wide datasets

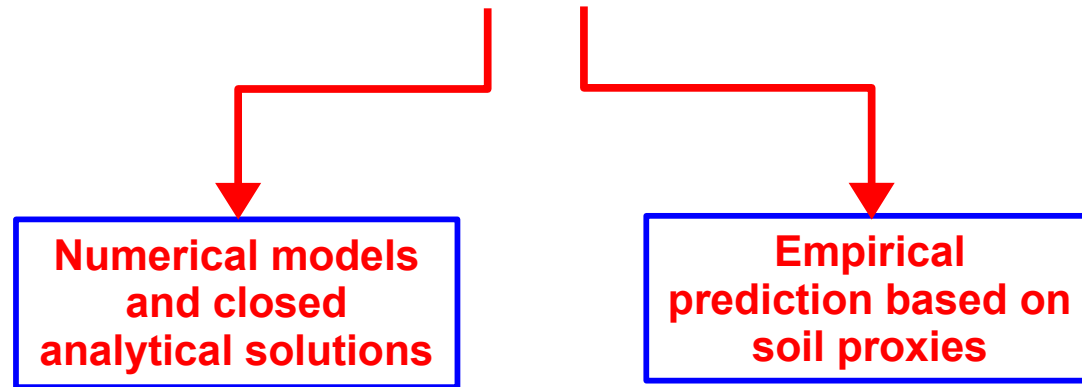
CONS: based just on observation, (little) physical justification, large epistemic uncertainty

The Generic Site Amplification Term

GMPEs represent a simple and convenient way to predict ground motion level over wide areas and sites of different characteristic

In order to predict site response for a specific site and in case of **lack of direct recordings**, a **site amplification model** is then necessary

This can be done in two ways, using:



**Numerical models
and closed
analytical solutions**

Possible, but impractical over large scales, due to high costs in obtaining detailed site parameters....

**Empirical
prediction based on
soil proxies**

Simple and convenient, although empirical models are still calibrated on **direct analysis of earthquakes**

Soil classification and proxies

Present **GMPEs** and **building codes** use simplified approaches to map the variability of local site response over wide areas by means of **statistical models** based on **ground types** (or classes) and **empirical observations**

Ground types are identified by appropriate **near-surface proxies**, such as:

- **the average velocity over the first 30 meters ($V_{s_{30}}$)**
- the fundamental frequency of resonance
- results from SPT/CPT tests
- geological/geotechnical classification...

Ground Class	Description	V_s [m/s]	N_{SPT}	s_u [kN/m ²]	S	T_B [s]	T_C [s]	T_D [s]
A	firm rock (e.g. granite, gneiss, quartzite, siliceous limestone, limestone) or soft rock (e.g. sandstone, conglomerate, Jura marl, Opalinus claystone) beneath a maximum soil cover of 5 m	> 800	–	–	1.00	0.15	0.4	2.0
B	deposits of extensive cemented gravel and sand and/or overconsolidated soils with a thickness exceeding 30 m	400...800	> 50	> 250	1.20	0.15	0.5	2.0
C	deposits of normally consolidated and uncemented gravel and sand and/or moraine with a thickness exceeding 30 m	300...500	15...50	70...250	1.15	0.20	0.6	2.0
D	deposits of unconsolidated fine sand, silt and clay with a thickness exceeding 30 m	150...300	< 15	< 70	1.35	0.20	0.8	2.0
E	alluvial surface layer of Ground Classes C or D, with a thickness of 5 to 30 m lying above a stiffer layer of the Ground Classes A or B	–	–	–	1.40	0.15	0.5	2.0
F	deposits of structurally-sensitive and organic deposits (e.g. peat, lake marl, slide material) with a thickness exceeding 10 m	–	–	–	–	–	–	–

SIA261 - Example of soil classification using $V_{s_{30}}$

Some Considerations on the Use of Soil Proxies

⇒ Proxies are a convenient way to characterize soil types of “*expected*” similar seismic response using just a single parameter

⇒ Soil proxies can be obtained by direct measure or (very often) by **indirect extrapolation** from other direct observations (e.g. geology, topography)

⇒ However, despite of their simplicity, these proxies:

- ① do not fully describe the **vertical/lateral variability** of the soil structure
- ② can hardly describe the **frequency dependent** amplification behavior
- ③ cannot account for site-specific phenomena like **soil non-linearity** and **resonance amplification**

What V_{s30} actually is?...

- V_{s30} is the **travel-time average shear-wave velocity** over the first 30m.
- It is computed in such a way:

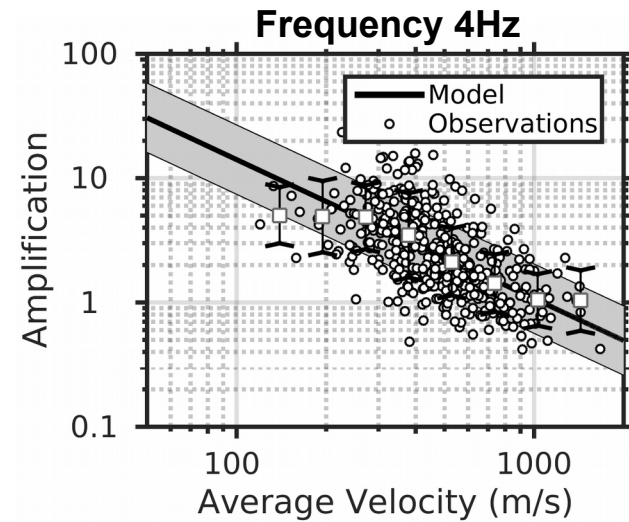
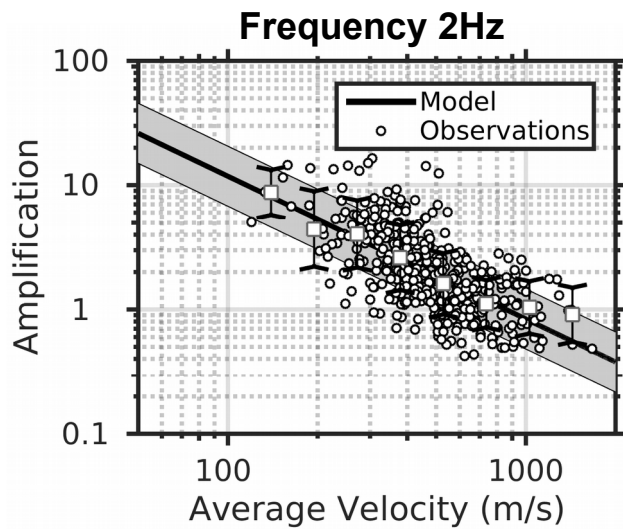
$$V_{s30} = \frac{30}{\sum_{i=1, N} \frac{h_i}{v_i}}$$

...but why using 30m, and not 10, 25 or 50m?

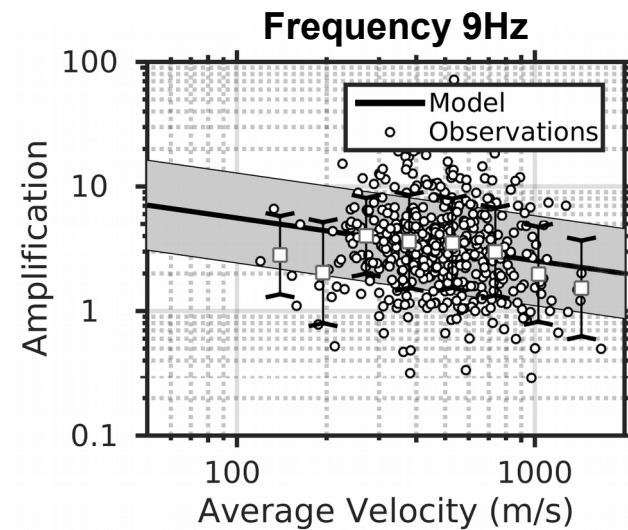
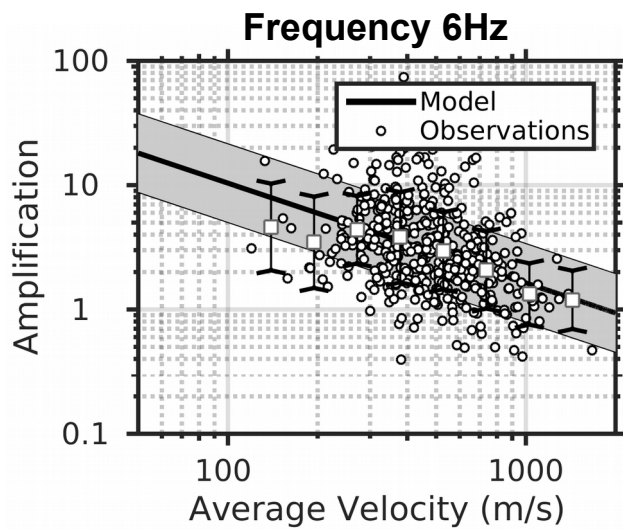
- Simply because ~30m (**100ft!**) was the standard penetration depth of most of the direct logging techniques of the past (at least in US).

Consequently...

- The large availability of log data within this depth range imposed this parameters as **de facto standard** (but without a clear **physical meaning**)



Nonetheless V_{s30} is a parameter **highly correlated** with site amplification...

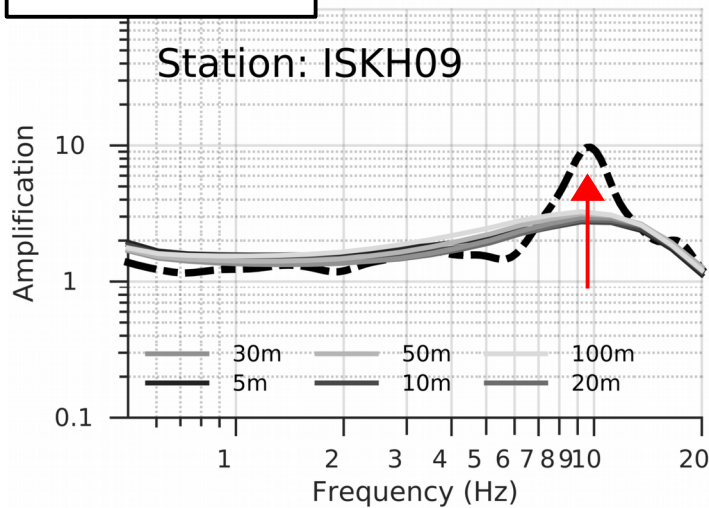


...even if prediction **uncertainty** is quite large

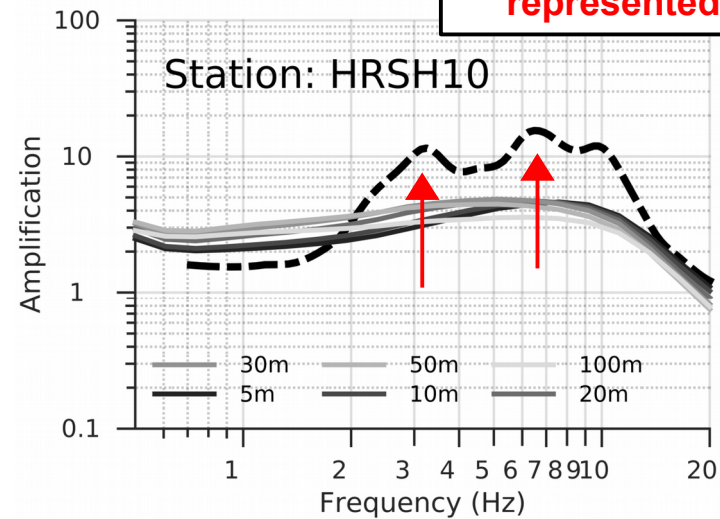
Source of Uncertainty of the Predictor

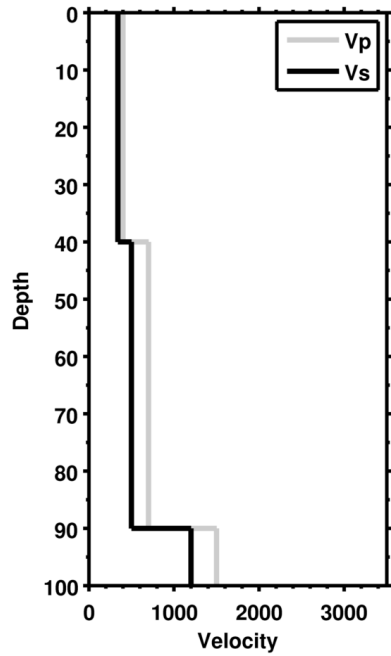
- V_{s30} is basically a proxy for the contrast of seismic impedance between the **basement** (source condition) and the **uppermost (average) soil**, which controls the average amplification level of the site
- However, V_{s30} cannot explain those complex phenomena developing “*within*” the profile...

Works nicely
with rock sites

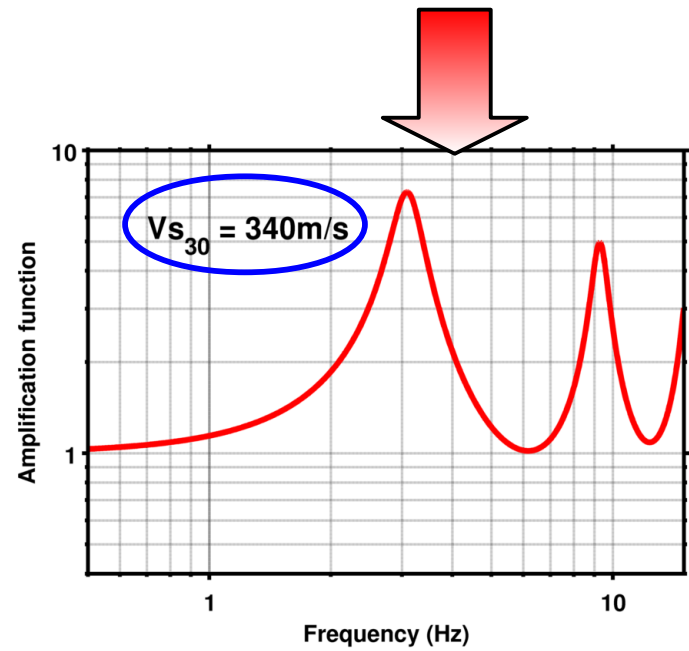
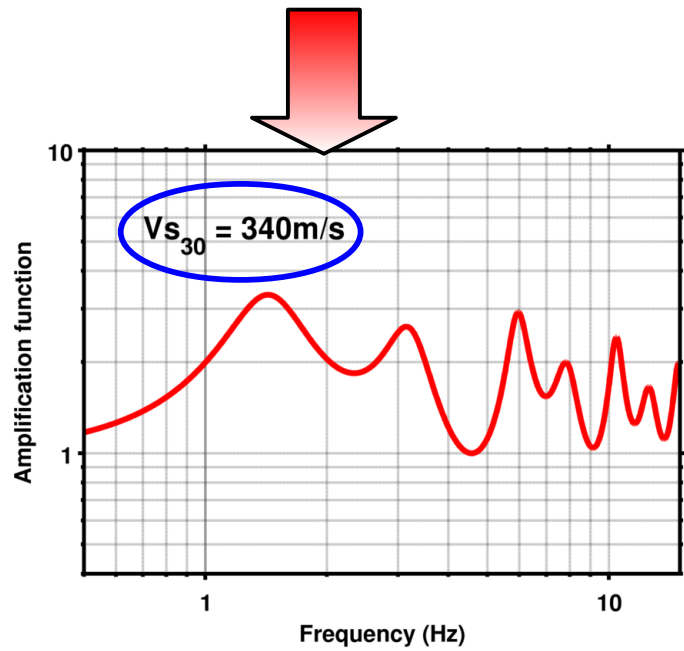
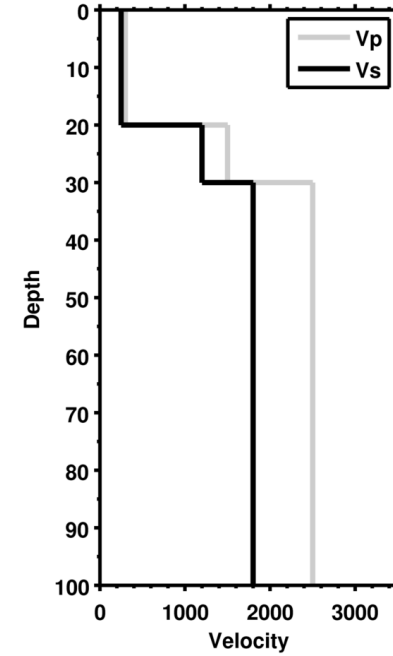


Resonance
amplification not
represented





A simple synthetic example:
profiles with same V_{s30}

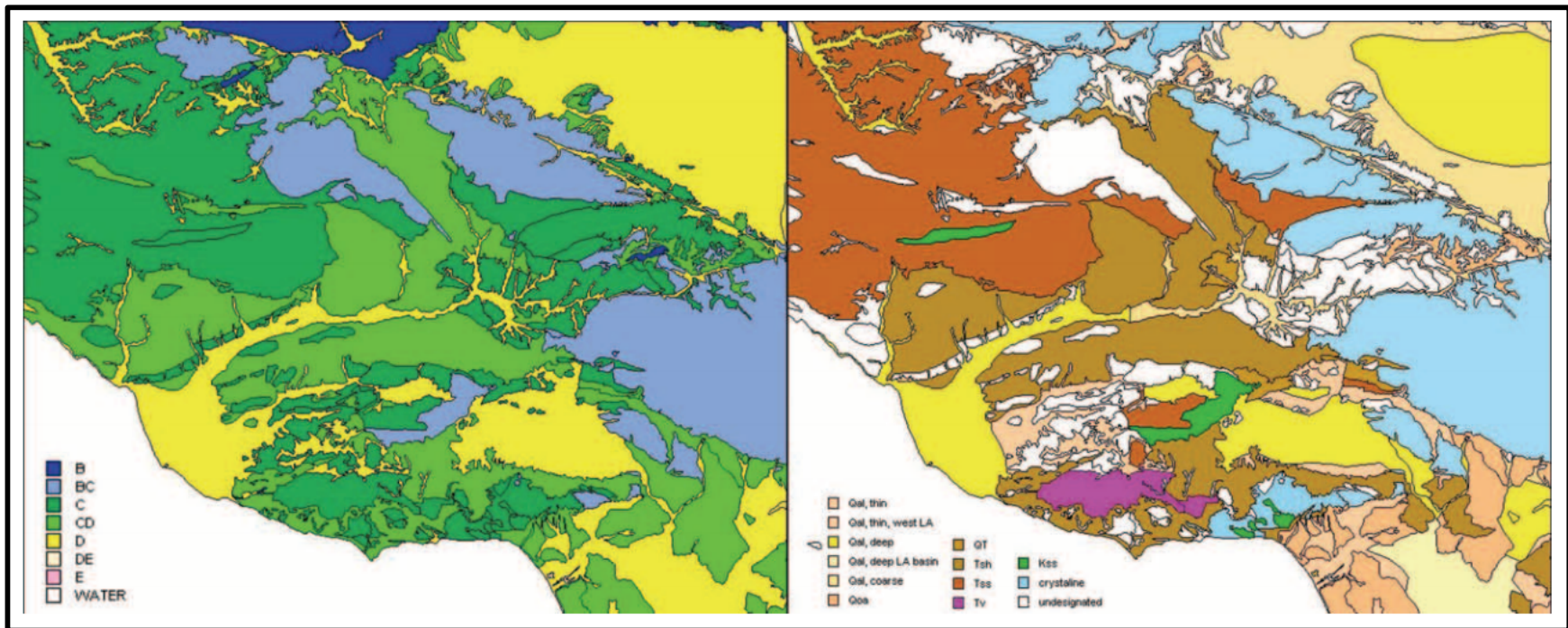


Additional Source of Uncertainty

- V_{s30} can also be biased by the way it is obtained, often not from direct measurement but **extrapolated** from other surface proxies (geology, geotechnical classification, CPT tests....)
- The conversion introduces an additional contribution to the uncertainty, which sum to the final error in the prediction

Geology

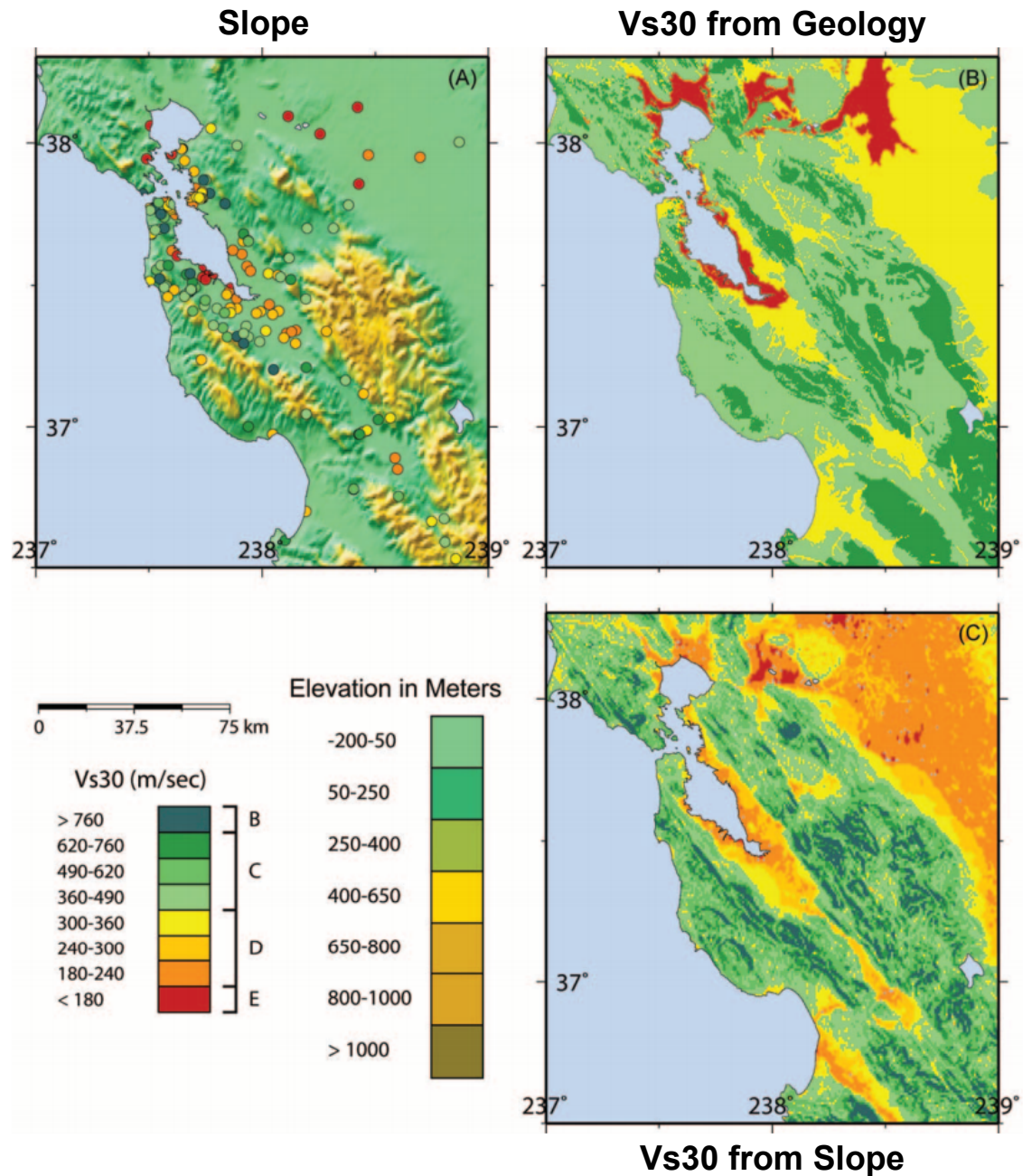
V_{s30}



Willis and Clahan (2006)

Vs₃₀ from Topography

- Nowadays, a popular way to map Vs₃₀ over large areas is the use of **topographic slope** from geodetic observations (Wald and Allen, 2007, 2009)
- The relation is based on the concept of “**depositional energy**” of the sediments



Outcropping
rock

Coarse
Sediments

Fine
Sediments

Decreasing
energy

Vs₃₀ from Topography

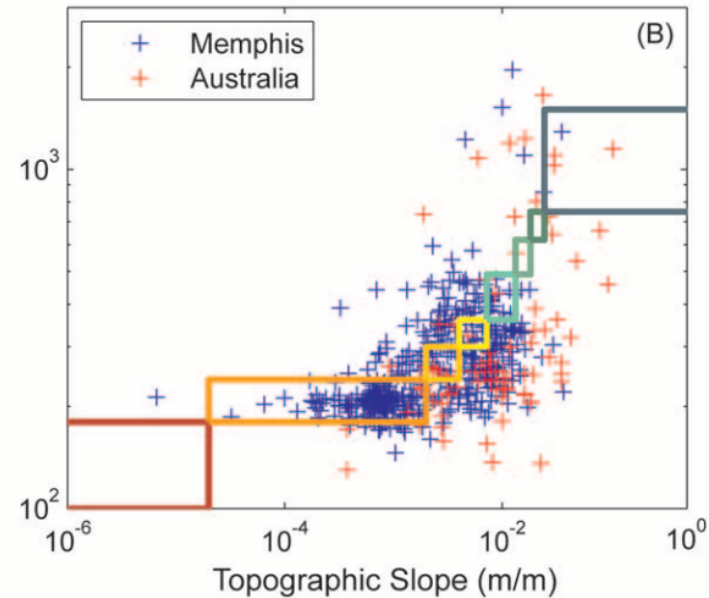
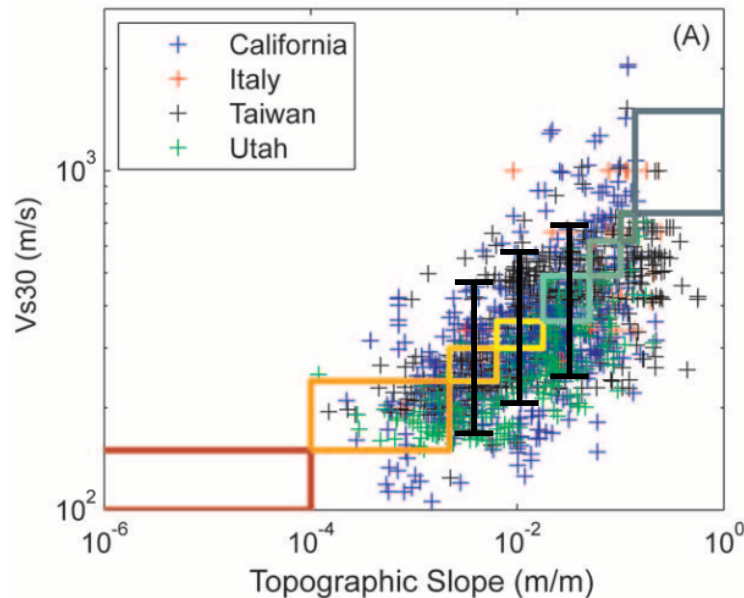
The slope-Vs₃₀ relationship is based on the **National Earthquake Hazard Reduction Program (NERHP)** Vs₃₀ boundaries (arbitrary?)

Summary of Slope Ranges for NEHRP V_s³⁰ Categories

Class	V _s ³⁰ Range (m/sec)	Slope Range (m/m)	
		Active Tectonic	Stable Continent
E	<180	<1.0E-4	<2.0E-5
	180-240	1.0E-4-2.2E-3	2.0E-5-2.0E-3
D	240-300	2.2E-3-6.3E-3	2.0E-3-4.0E-3
	300-360	6.3E-3-0.018	4.0E-3-7.2E-3
C	360-490	0.018-0.050	7.2E-3-0.013
	490-620	0.050-0.10	0.013-0.018
B	620-760	0.10-0.138	0.018-0.025
	>760	>0.138	>0.025

Calibration databases from different regions:

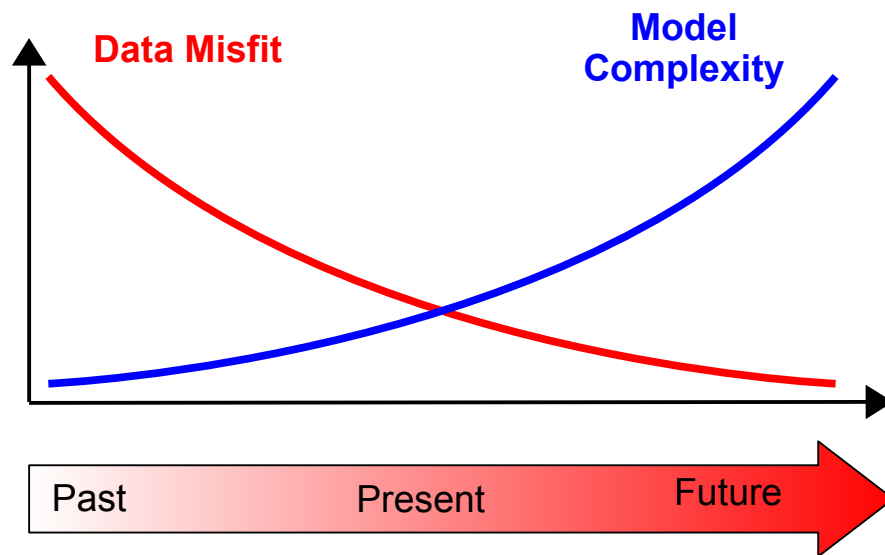
- California
- Utah
- Central U.S.
- Taiwan
- Italy
- Australia



...and the question is finally:

Is $V_{s_{30}}$ really so adequate as proxy for site amplification?

$V_{s_{30}}$ is probably not sufficient for future engineering products, as it introduces too large uncertainties



Epistemic uncertainty can be reduced at the expenses of increasing model complexity, by introducing **physics-based concepts**

Empirical models

Physics based simulations

Modeling Site-Response Into GMPEs

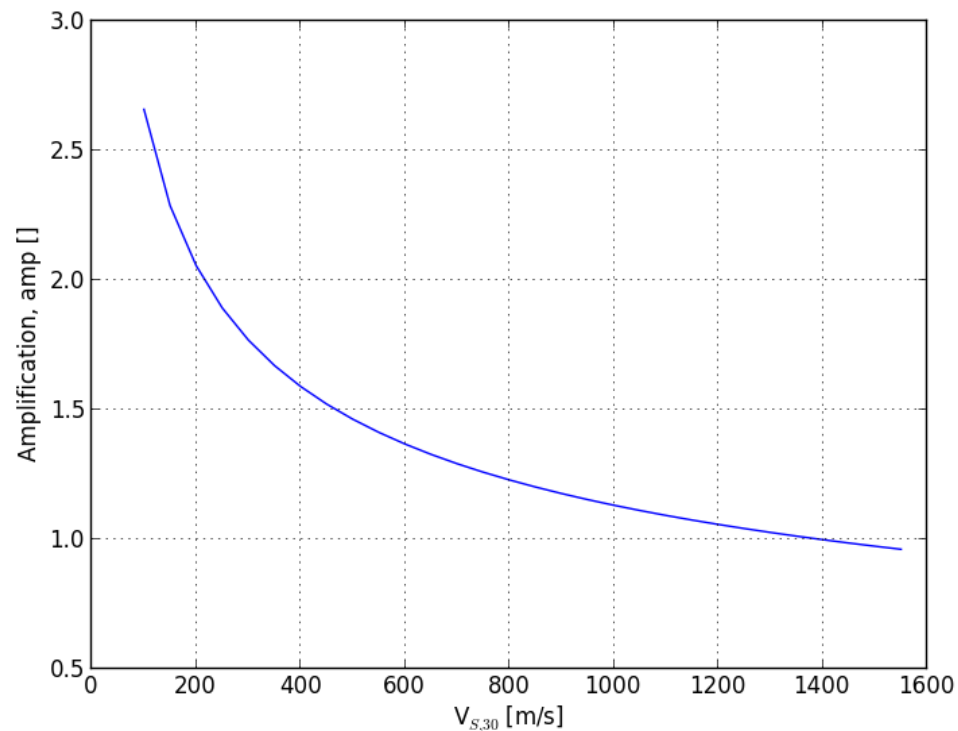
Boore et al. (1997)

Assuming a linear amplification of motion Boore et al. (1997) proposed the following formula to model site amplification using a site-specific $V_{S,30}$ value:

$$\ln(\text{Amp}) = a \ln\left(\frac{V_{S,30}}{V_{\text{Ref}}}\right)$$

For PGA the coefficients are:

- $a = -0.371$
- $V_{\text{ref}} = 1396 \text{ [m/s]}$



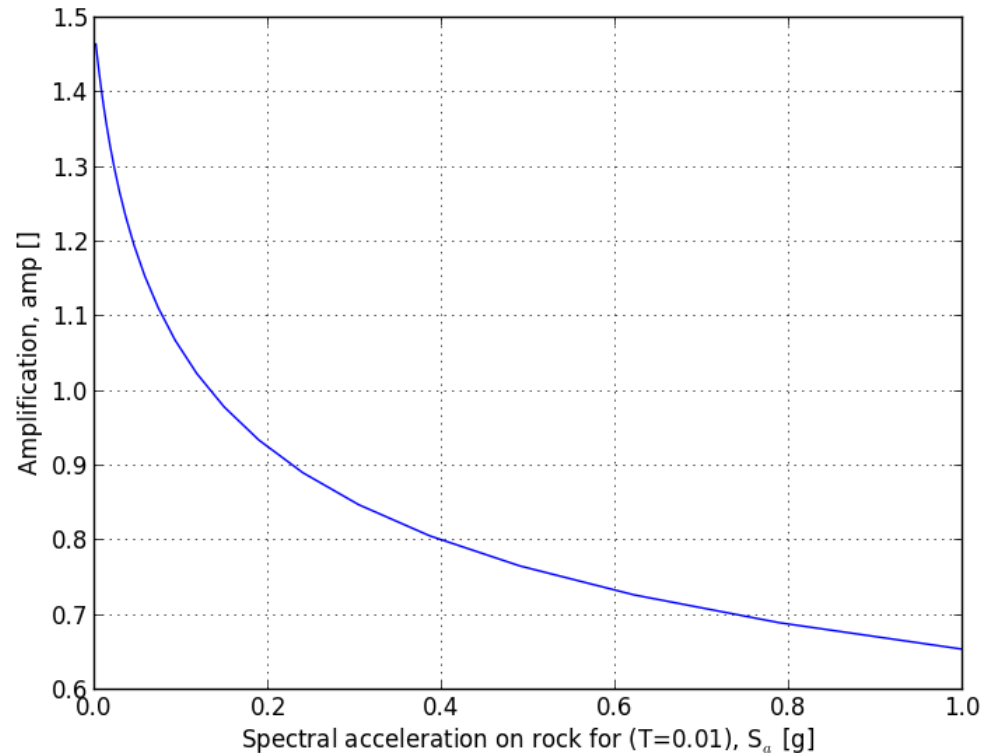
Ambramson and Silva (1997)

Ambramson and Silva (1997) using a generalized soil category developed a model for site response accounting for the non-linear behaviour of materials

$$\ln(\text{Amp}) = a + b \ln(P \hat{G}A_{\text{rock}} + c)$$

For PGA the coefficients are:

- $a = -0.417$
- $b = -0.230$
- $c = 0.03$



Choi and Stewart (2005)

Choi and Stewart (2005) proposed an empirical model for assessing the nonlinear amplification factor for spectral acceleration as a function of $V_{s,30}$. The results can be used as *Vs-30-based* site factors with attenuation relationships

$$\ln(F_{ij}) = c \ln\left(\frac{V_{s-30_{ij}}}{V_{ref}}\right) + b \ln\left(\frac{PHA_{r_{ij}}}{0.1}\right) + \eta_i + \varepsilon_{ij},$$

where:

- PHA_r peak horizontal acceleration for reference [rock] site condition [g]
- V_{ref} and c are regression parameters
- η_i is a random effect term for earthquake event i (should have zero median across all events, standard deviation is denoted as t); and ε_{ij} represents the intra-event model residual for motion j in event i (should have median near zero for well-recorded events, standard deviation is denoted as s).